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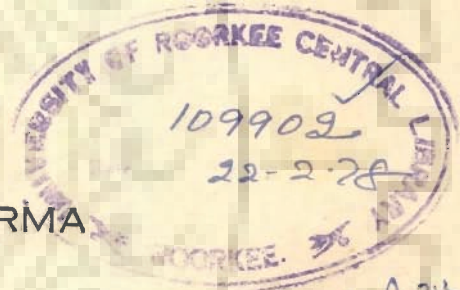
# HEAT TRANSFER STUDIES IN POOL BOILING OF LIQUIDS

A THESIS  
*submitted in fulfilment of the  
requirement for the award of the degree*  
of  
DOCTOR OF PHILOSOPHY  
in  
CHEMICAL ENGINEERING



By

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April, 1977



With Utmost Reverence

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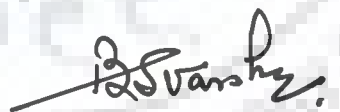
**WHOSE INCOMMUNICABLE QUALITIES**

**'WE' COULD HARDLY PERCEIVE**

# Certificate

Certified that the thesis entitled "*Heat Transfer Studies in Pool Boiling of Liquids*" which is being submitted by Sri PARASHU RAM SHARMA in fulfilment of the requirements for the award of DOCTOR OF PHILOSOPHY in Chemical Engineering of the University of Roorkee, Roorkee, is a record of candidate's own work carried out by him under my supervision and guidance. The matter embodied in this thesis has not been submitted for the award of any other degree.

This is further certified that the candidate has worked for a period of three years and three months from January 1974 for preparing this thesis.



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April 12, 1977

## A B S T R A C T

An investigation of heat transfer in nucleate pool boiling for atmospheric and subatmospheric pressures has been carried out both analytically and experimentally.

Traditionally, the study of heat transfer in nucleate pool boiling are considered empirically, without regard for bubble dynamics. But in the present investigation, following the fact that the heat transfer in nucleate boiling is characterised by the induced turbulence due to; nucleation sites on the heating surface, bubble size and their emission frequency, a mathematical analysis has led to equation for predicting the values of absolute heat transfer coefficient, Eq. (5.22). This resultant equation relates heat transfer coefficient to the wall heat flux, system pressure and the pertinent physico-thermal properties of boiling fluids through the heating surface characteristics. But this equation is useful for calculating the absolute values of heat transfer coefficient, only if, heating surface characteristics are known as required for constant  $M$  and the values of  $n_f$  for the determination of exponent  $a$ . Since the surface characteristics and the value of  $n_f$  are extremely unpredictable for industrial surfaces and they differ from surface to surface, a considerable built-in difficulty is inherited in this equation. Therefore, it appears impossible to provide a

panacea for predicting the absolute values of heat transfer coefficient. However, for a given heating surface it is possible to determine the value of constant M and exponent a empirically which can be used for the calculation of absolute values of transfer coefficients. The value of exponent a has been evaluated as 0.3683, and the expression for M are represented by the set of equations, Eq. (6.3). Thus the equation for calculating the absolute values of heat transfer coefficient is as follows: while f is obtained from the respective equation, Eq. (5.15) or Eq. (5.19) for Jakob number less and greater than 100.

$$h = M \left[ \left( \frac{\lambda^{2.5} \rho_v}{T_s^{1.5} \sigma} \right) \left( \frac{q}{k_l g} \right)^{0.3} \left( \frac{1}{C_l} \right)^{1.2} \right]^{2.33} \{ f \}^{0.3683} \quad (6.4)$$

The constant M represents the combined effects of pressure and surface-liquid combination on boiling heat transfer.

A procedure has also been devised for the calculation of  $h^*/h_1^*$  [cf. Eq(6.6)]. It has been found that the values of  $h^*/h_1^*$  depend upon wall heat flux, system pressure and pertinent physico-thermal properties of boiling fluids. They do not depend on surface-liquid combinations. Hence this equation is useful to compare the data of different investigators obtained on differing surface-liquid combinations. It was found that this equation correlated the present data and those of Cryder and Finalborgo [5], Raben, Beaubouef and

Commerford [94] within a maximum deviation of  $\pm 20$  per cent. This equation also provides the facility for the computation of absolute values of heat transfer coefficient at subatmospheric pressures, without resort to experimentation, if the value of heat transfer coefficient at normal boiling point is available. Equation (6.6) is as follows:

$$\frac{h^*}{h_1^*} = 0.95831645(P/P_1)^{-0.3997825} \left[ \left( \frac{\lambda}{\lambda_1} \right)^{2.5} \left( \frac{\rho_v}{\rho_{v1}} \right) \left( \frac{T_{sl}}{T_s} \right)^{1.5} \right. \\ \left. \left( \frac{\sigma_1}{\sigma} \right) \left( \frac{k/l}{k/l} \right)^{0.3} \left( \frac{q}{q_1} \right)^{0.3} \left( \frac{C/l}{C/l} \right)^{1.2} \left. \left( \frac{f}{f_1} \right) \right]^{0.3683} \quad (6.6)$$

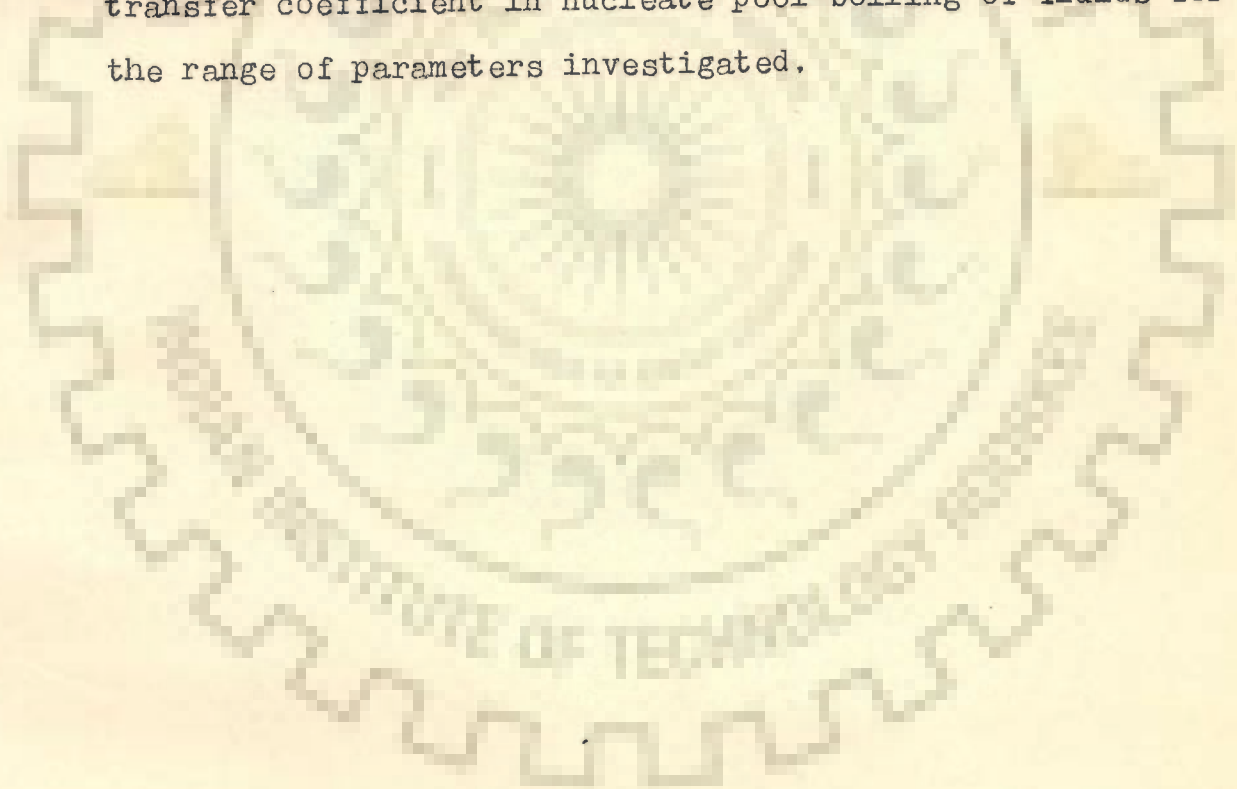
Since the present study is for atmospheric and sub-atmospheric pressures, obviously the resultant equation, Eq.(6.6) might not correlate the boiling data for higher pressures.

A computer program was written and calculations were made to compute the heat transfer coefficients from the above resultant equations.

Apart from the analytical analysis the purpose of the investigation was also to obtain experimental data in order to verify the resultant equations from the analysis and to generate the new experimental data for subatmospheric pressures which are scanty in the literature. The experimental investigation involved the determination of heat transfer coefficient from 410 ASIS stainless steel heating surface to the boiling fluids:

distilled water, isopropanol, ethanol and methanol for the pressures ranging from 11.33 kN/m<sup>2</sup> to 98.44 kN/m<sup>2</sup> and heat flux ranging from 6870 W/m<sup>2</sup> to 41730 W/m<sup>2</sup>.

The excellent consistency between the experimental data and the predicted values sufficiently proves that the present mathematical analysis based on the governing equations for nucleation sites, bubble growth, bubble size and bubble emission frequency provides an adequate procedure for heat transfer coefficient in nucleate pool boiling of fluids for the range of parameters investigated.



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## N O M E N C L A T U R E

a	exponent , defined in Eq(5.20)	
A	heat transfer area	$m^2$
C	specific heat	J/kg K
$c_0$	dimensional constant, defined in Eq(5.1)	
$c_2$	constant, defined in Eq(5,4a)	
$c_3$	constant, defined in Eq(5,20)	
$C_4$	constant, defined in Eq(6.2)	
$C_{sf}$	surface-liquid combination factor	
d	diameter of the heating surface	m
D	diameter of bubble	m
$D_b$	diameter of bubble at departure	m
f	bubble emission frequency	1/s
g	acceleration due to gravity	$m/s^2$
h	heat transfer coefficient	$W/m^2 K$
$\bar{h}$	average heat transfer coefficient	$W/m^2 K$
$h^*$	quotient at a pressure, $h/q^{0.7}$	
$h_1^*$	quotient at normal boiling point, $h/q^{0.7}$	
k	thermal conductivity	$W/m K$
$\ell$	length of the heating surface	m
M	dimensional constant, defined in Eq(5.21)	
m	exponent, defined in Eq (5,1), equal to 2.33	
n	number of active sites per unit area of the heating surface	$1/m^2$
$n_4$	exponent, defined in Eq, (6.2)	

P	pressure	$N/m^2$
$\Delta P$	pressure difference	$N/m^2$
q	heat flux	$W/m^2$
$r_c$	radius of active site	m
$r_r$	radius of site for which n would be one per unit area, defined in Eq.(5.1)	
T	temperature	K or $^{\circ}C$
$\bar{T}$	average temperature	K or $^{\circ}C$
$\Delta T$	temperature difference, $(T_w - T_s)$	K or $^{\circ}C$
$\overline{\Delta T}$	average temperature difference	K or $^{\circ}C$
$\Delta T_w$	wall superheat, $(T_w - T_s)$	K or $^{\circ}C$
$\overline{\Delta T_w}$	average wall superheat	K or $^{\circ}C$
Greek symbols		
$\sigma$	surface tension	N/m
$\rho$	density	$kg/m^3$
$\lambda$	latent heat of vaporization	J/kg
$\mu$	dynamic viscosity	$N\ s/m^2$
$\nu$	kinematic viscosity, $\mu/\rho$	$m^2/s$
$\alpha$	thermal diffusivity, $k/C\rho$	$m^2/s$
$\theta$	time	s
$\theta_d$	departure period	s
$\theta_w$	waiting period	s
$\delta$	transient thermal layer thickness	m
Dimensionless Modulii		
$G_a$	Gallilean number	$\frac{g D^3}{\nu^2 b}$
$J_a$	Jakob number	$\frac{C \rho \ell \Delta T_w}{\rho_v \lambda}$

$K_P$	Criterion for pressure term in boiling	$\frac{P}{\sqrt{g \sigma (\rho_l - \rho_v)}} \frac{1}{(\rho_v \lambda)^2}$
$K_t$	Criterion for bubble break off frequency	$C_l t_s \rho_l \sqrt{g \sigma (\rho_l - \rho_v)}$
$Nu_B$	Nusselt number for boiling	$\frac{h D_b}{k_l}$
$Pe_B$	Peclet number for boiling	$\frac{q}{\rho_v \lambda \alpha} \sqrt{\frac{\sigma}{g(\rho_l - \rho_v)}}$
$Pr$	Prandtl number	$C_l \mu_l / k_l$
$Re_B$	Reynolds number for boiling	$\frac{q \rho_l}{\lambda \rho_v \mu_l} \sqrt{\frac{\sigma}{g(\rho_l - \rho_v)}}$

Subscripts

i	inside
l	liquid
o	outside
s	saturation
v	vapour
w	wall
l	normal boiling point
lv	liquid-vapour
ls	liquid-solid
vs	vapour-solid
Predt	predicted
Exptl	experimental

## CHAPTER 1

### I N T R O D U C T I O N

The largest present day use of boiling of fluids is found in chemical, petro-chemical, power plant and refrigeration industries. Boiling heat transfer is advantageous in respect of enhancing heat transfer coefficient and thus reducing the weight of heat transfer equipment and consequently the cost of the equipment. This consideration has led to the use of boiling heat transfer in space vehicles also. In a nut shell, the applications of boiling heat transfer are ever-increasing with the advancement of modern technology. Keeping in view the vast number of equipment dealing with boiling heat transfer, this field of study has been the subject for active research for the last three decades in order to evolve suitable design procedures for these equipment.

A large number of empirical correlations have been recommended for the determination of boiling heat transfer coefficients. These correlations are not of general applicability for the wide range of parameters. One of the reasons of their limited applications is that these correlations have not been derived by considering the governing behaviour of bubble dynamics and

surface characteristics on the boiling heat transfer which as a matter of fact, have pronounced effects on the boiling phenomenon. Obviously, these correlations have been attempted to relate heat transfer coefficient with the pertinent physico-thermal properties of the boiling fluids alone.

The effects of heating surface characteristics and bubble dynamics on heat transfer coefficient were accounted by Jakob and Linke [4] under the assumption that there exists a linear relationship between heat flux and number of active sites per unit area. They also assumed that the product of bubble emission frequency and departure diameter was a constant value. However, their correlating equation is not of general applicability. Recent studies have shown that the assumptions made by Jakob and Linke are not valid. Investigators [26], [46] [52] concluded that the relationship between heat flux and number of active sites per unit area is governed by a power law.

Until recently in all the empirical correlations and correlations due to Jakob and Linke [4] and Rohsenow [14], the bubble departure diameter was calculated by the Fritz equation [15]. Several investigations have been carried out for the determination of bubble departure diameter taking into consideration the dynamic effects of bubble [87], [88], [90], [92], [123]. It seems that

its frequency and the number of active sites per unit area. A consequence of this would be that the heat transfer coefficient in nucleate pool boiling will be affected by the changes in these quantities. Therefore, an analytical model consistent with the requirements of nucleate boiling heat transfer would include the adequate determination of bubble departure diameter, its frequency and the number of active sites per unit area.

The heat transfer rate in the boiling of liquids is also influenced by the degree of superheat. In electrically heated heating surfaces, the surface temperature varies with heat flux, system pressure, physico-thermal properties of the boiling fluids and surface characteristics. Therefore, it will be of engineering interest to relate wall superheat with these parameters.

In chemical and petro-chemical industries there are many situations where boiling is carried out at atmospheric and sub-atmospheric pressures. Design data for boiling heat transfer at subatmospheric pressures are very scarce.

The considerations as above led to the present investigation with the following objectives:



Cole and Shulman [95] have conducted a careful investigation for recommending equation for bubble departure diameter at atmospheric and subatmospheric pressures. They have shown that the Fritz equation [15] is not valid for subatmospheric pressures.

Experimental investigations for bubble emission frequency using high speed photography have been made by many investigators [3], [70], [112 -116] for different boiling conditions. However, these studies do not yield expressions for direct calculations of bubble emission frequency. Besides, there is a scarcity of the bubble emission frequency relationships for subatmospheric pressure conditions. However, there exists adequate information of bubble growth rate and bubble departure diameter at subatmospheric pressures which can be used for developing analytical expressions for bubble emission frequency.

It is seen from these investigations that no single correlation for  $f$  and  $D_b$  can be used for the wide range of degree of superheat and system pressures. Accordingly, care should be exercised when using them for a specific situation of boiling of fluids on heating surfaces.

It is certain that the turbulence in the superheat layer adjacent to the heating surface is markedly influenced by the bubble departure diameter,

1. To apply the appropriate governing equations of vapour bubble growth rate, bubble departure diameter, bubble emission frequency and number of active sites per unit area with a view to provide analytical equations representing the effects of wall heat flux, system pressure, physico-thermal properties of boiling fluids and surface characteristics on nucleate boiling heat transfer.
2. To experiment with a wide range of subatmospheric pressures in nucleate pool boiling of fluids of widely differing physico-thermal properties for determining the extent of validity of the present analytical model for the solution of practical problems.
3. To scrutinize the earlier analyses and empirical correlations with the help of present and existing experimental data.
4. To recommend a simplified procedure for calculating boiling heat transfer coefficients.

## CHAPTER 2

### LITERATURE REVIEW

During the last three decades a large effort has been made to researches in order to achieve basic understanding of boiling processes. An examination of investigations carried out in all these years reveals that the boiling of liquids represents the least understood form of heat transfer. No investigation has been conducted to study the boiling phenomena as a whole from the first principles. However, the various aspects of boiling heat transfer have been attempted as discrete studies. As a result of these studies, the underlying thermodynamic and hydrodynamic principles involved in the vapour bubble formation and growth and their effects on heat transfer rates are becoming known.

Keeping the aims of the present investigation in view, the literature on nucleate pool boiling heat transfer has been reviewed under the following sections:

#### 2.1 EMPIRICAL CORRELATIONS

The heat transfer to the nucleate pool boiling of liquids has been the subject of active research in the past three decades. A great deal of experimental work has been done, and a large number of correlations

for heat transfer coefficient have been proposed based on experimental data; however, no correlation has been proposed which possesses general applicability for wide ranges of pressure and heat flux, and for fluids of varying physico-thermal properties. In this section empirical correlations have been described with pertinent experimental variables.

The heat transfer coefficient has been related to the wall heat flux, the system pressure, the saturation temperature and the pertinent fluid properties in the following forms:

- (1) In the dimensional form, nucleate boiling heat transfer coefficient may be expressed by the equation :

$$h = A q^n p^m \quad (2.1)$$

Kutateladze and Borishanskii [ 1 ] have made an exhaustive survey of these correlations for wide ranges of heat fluxes, pressures, heating surfaces and fluids of differing properties. The survey shows that each equation is applicable only to a particular range of parameters for which it was derived. Some of the correlations have been attempted in the form:

$$h = A q^n ( t''/B)^m \quad (2.2)$$

where  $t''$  is the temperature range for which they are applicable.

(2) For many situations, the correlations for boiling heat transfer were obtained in the form of dimensionless groups, the exponents of the dimensionless groups were determined experimentally.

The general form of this type of correlations has been expressed in the following form:

$$Nu = B Re^{n_1} Pr^{n_2} Ga^{n_3} Kp^{n_4} Kt^{n_5} \quad (2.3)$$

The values of constant and exponents depend on the system conditions.

Cryder and Gilliland [2] using the methods of dimensional analysis established the correlation between variables as follows:

$$\frac{hD}{k_\ell} = 0.38 \left( \frac{C_\ell z}{k_\ell} \right)^{0.425} \left( \frac{\Delta T S^2 D^2 k_\ell}{z^3} \right)^{2.39} \left( \frac{z^2}{S D \gamma} \right)^{1.65} \quad (2.4)$$

D = diameter of heating unit, inches

z = liquid viscosity, cp

S = specific gravity

$\gamma$  = surface tension, poundals / ft

$C_\ell$  = specific heat of liquid, Btu/lb  $^{\circ}$ F

The exponents in equation (2.4) were calculated from the experimental data for liquids, namely; water, carbon-tetrachloride, methanol, 1-butanol, gasoline, kerosene, glycerol and solutions of various inorganic salts.

Cryder and Finalborgo[5] have determined heat transfer coefficients for eight different liquids at boiling points both above and below atmospheric pressure experimentally. The liquids investigated by them differed in their physico-thermal properties. The heat rate varied from 439 to 2360 Btu/hr. Based on their experimental data they have concluded the following equations for heat transfer coefficient:

$$\log h = a + 2.5 \log \Delta t + bt \quad (2.5)$$

$$\log \frac{h}{h_n} = b(t-t_n) \quad (2.6)$$

Where  $h_n$  denotes the heat transfer coefficient at the normal boiling point of a liquid,  $t$  is a temperature of boiling liquid,  $t_n$  is normal boiling point of the liquid, and  $a$  and  $b$  are constants (their values depend on the nature of liquid as given in Table 2.1).

Table 2.1 Values of constants  $a$  and  $b$  in Eqs. (2.5 and 2.6)

Liquid	$a$	$b$
Water	- 2.05	0.014
Methanol	- 2.23	0.015
Carbon tetrachloride	- 2.57	0.012
Normal butanol	- 4.06	0.014
26.3% Glycerol solution	- 2.65	0.015
Kerosene	- 5.15	0.012
10.1% Sodium sulphate solution	- 2.62	0.016
24.2 % Sodium chloride solution	- 3.61	0.017

Akin and McAdams [6] carried out an experimental investigation on a chrome-plated horizontal cylinder of diameter  $1.905 \times 10^{-4}$  m immersed in liquids, namely; water, isopropanol, isobutanol and n-butanol at atmospheric pressure. They also investigated the boiling of distilled water at subatmospheric pressures ranging from 0.16 - 0.68 kg/cm<sup>2</sup>.

Insinger and Bliss [7] conducted an experimental investigation with water, carbon tetrachloride, isopropanol and 40% sucrose solution at atmospheric pressure. They used a vertical heating cylinder of 6 in. length and about 1.25 in. diameter. A simplified form of the Insinger-Bliss correlation is given by:

$$\frac{h}{\sqrt{k\ell}} \times \frac{\sqrt{\sigma}}{\rho^{0.82} \ell} = 4 J^{0.41} g^{-0.09} 10^{-3.2} \left( \frac{q^{0.68} c^{0.5}}{\rho^{0.5} \lambda^{0.27}} \right) \quad (2.7)$$

Where J is mechanical equivalent of heat equal to 778 ft.lb/Btu.

This equation was found to satisfy the experimental results of Jakob and Linke [4] on water and carbon tetrachloride, of Linden and Montillon [8] and Dunn and Vincent [9] on water, and of Akin and McAdams [6] on water, isopropanol, isobutanol and n-butanol along with his own experimental data.

Bonilla and Perry [10] under-took an experimental investigation to obtain a method of interpolation between pure liquids to give boiling heat transfer

coefficients for their binary mixtures. They used two heaters of effective diameter 3.58 in. and 2.62 in. respectively each consisted of 3/4 in. copper disk with copper fins 3/16 in. thick and 2 in. high welded to the bottom. The 1/4 in. spaces between fins contain flat elements wound with 1/8 in. wide nichrome ribbon, 0.283 ohm/ft, on mica cores, with asbestos insulation. The pure liquids studied were water, ethanol, n-butanol and acetone. They examined the high range Jakob and Linke equation, Eq. (2.22) as discussed later-on. The ethanol curves at pressures other than atmospheric were corrected for pressure by plotting

$$\left( \frac{v_a}{v} \right)^{1.37} \left[ \frac{\sigma}{\sigma_a} \frac{\rho_{l,a}}{\rho_l} \frac{q}{\rho_{v,a} \lambda_a w_{b,a}} \right]$$

as abscissa. The average slope of 0.73 compares with Jakob and Linke of 0.80 (cf. equation 2.22). The modification to the equation due to Jakob and Linke as suggested by these authors consists in changing the exponent from 0.80 to 0.73, inclusion of Prandtl number raised to the power of 1/2, and changing the constant from 31.6 to 16.6. Thus, the proposed equation was:

$$\frac{h}{k_l} \sqrt{\frac{\sigma}{\rho_l}} = 16.6 \left[ \frac{v_a}{v} \right] \left( \frac{\sigma}{\sigma_a} \frac{\rho_{l,a}}{\rho_l} \frac{q}{\rho_{v,a} \lambda_a w_{b,a}} \right)^{0.73} \left( \frac{C_l \mu_l}{k_l} \right)^{0.5} \quad (2.8)$$



They have also attempted to determine the effect of pressure on heat transfer coefficient for a heat flux value of 50,000 Btu/hr ft<sup>2</sup>. They found that heat transfer coefficient is directly proportional to the pressure raised to the power of 0.25. In other words it can be concluded that boiling surface does not change the ratios of the coefficients obtained at different pressures.

Cichelli and Bonilla [11] investigated the boiling of pure liquids: water, ethanol, benzene, propane, n-pentane and n-heptane; and binary mixtures: 50 mole per cent water-ethanol and 33 and 67 mole per cent propane-pentane. They observed that coefficient of heat transfer increased with pressure continuously until at critical pressure the nucleate boiling ceased to be stable. The apparatus used was an electrically heated horizontal plate. The surface was a thick copper plate with 0.002 in. of polished electroplated chromium.

Addoms [12] conducted the boiling heat transfer investigations experimentally. He used degassed distilled water on electrically heated horizontal platinum wire of diameter  $6.096 \times 10^{-4}$  m. The pressure varied from 14.7 psia to 2465 psia. Addoms' data have been used extensively by other investigators for sake of comparison.

Farber and Scorah [13] also used the horizontal wire of  $1.016 \times 10^{-4}$  m diameter in a pool of distilled water to carry out the investigations for nucleate boiling at atmospheric pressure.

McNelly [20] included five dimensionless groups in his correlation. The exponents and the coefficients were selected to give a reasonable fit with the experimental data from the boiling of 14 liquids. He recommended the following correlation:

$$\frac{hD}{k_\ell} = 0.255 \left[ \frac{Qd}{A\lambda\mu_\ell} \right]^{0.69} \left[ \frac{Pd}{\sigma} \right]^{0.31} \left[ \frac{p_\ell}{p_v} - 1 \right]^{0.33} \left[ \frac{C_\ell \mu_\ell}{k_\ell} \right]^{0.69} \quad (2.9)$$

Where,

- D = diameter of heating unit, inches
- d = characteristic length of heating surface, ft.
- Q = heat transfer rate, Btu/hr.
- $\lambda$  = heat of vaporization, Btu/lb.
- P = ambient pressure on liquid, lb/sq.ft.

Averin & Kruzhilin [21] correlation is of the following form:

$$\frac{h}{k_\ell} \sqrt{\frac{\sigma}{p_\ell - p_v}} = 0.082 \left[ \frac{q}{\rho_v \lambda} \sqrt{\frac{\sigma}{p_\ell - p_v}} \right]^{0.7} \left[ \frac{C_\ell \mu_\ell}{k_\ell} \right]^{-0.5} \left[ \frac{J (\rho_v \lambda)^2}{C_\ell^t \rho_\ell \sqrt{\sigma (\rho_\ell - \rho_v)}} \right]^{0.377} \quad (2.10)$$

Gilmour [23] presented an expression for nucleate boiling which resembles those for convective heat transfer and condensation heat transfer. He claims that his method is in contrast to the usual methodical approach for correlating the boiling heat transfer data. In his correlation, along with three familiar dimensionless groups (St, Pr and Re) he included an additional new dimensionless group to account for pressure and surface tension effects. His expression can be represented in the following form:

$$\left[ \frac{h}{CG} \right]^a \left[ \frac{C\mu}{k} \right]^b \left[ \frac{\rho \ell \sigma}{P^2} \right]^c = \frac{\phi}{(DG/\mu)^d} \quad (2.11)$$

The left hand side of the above expression is termed as Colburn j- function for nucleate boiling. The exponents on Stanton number is assumed to be unity and that on the Prandtl number for liquid heating is 0.6. The exponents on the pressure group and Reynold number have been computed by plotting the data of Cichelli and Bonilla [11] and Cryder and Finalborgo [5] for high pressures and subatmospheric pressures respectively. Both the data yielded the same magnitude of exponents.

The final correlation thus assumes the form:

$$\left( \frac{h}{CG} \right) \left[ \frac{C\mu}{k} \right]^{0.6} \left[ \frac{\rho \ell \sigma}{P^2} \right]^{0.425} = \frac{0.001}{(DG/\mu)^{0.3}} \quad (2.12)$$

Where  $G = \frac{V \rho_l}{A \rho_v}$  and  $D$  is the diameter of tube.

Gilmour [23] could correlate the existing experimental data for differing liquids of various investigators with his correlation satisfactorily.

Sternling and Tichacek [28] in their attempt to generate the experimental data for binary mixtures of large relative volatility also provided the nucleate boiling heat transfer data for pure fluids: benzene, methyl chloroform, carbon tetrachloride, isopropanol, methanol and water. They measured the heat transfer coefficients at atmospheric pressure for these fluids in a pool boiler for a wide range of heat flux.

Labuntsov [36] proposed the following correlation for nucleate pool boiling. The Nusselt group in his correlation has been calculated by taking the Fritz expression for bubble diameter.

$$\frac{h}{k_l} \sqrt{\frac{\sigma}{(\rho_l - \rho_v)g}} = 0.125 \left[ \frac{q}{\rho_v \lambda \alpha} \sqrt{\frac{\sigma}{(\rho_l - \rho_v)g}} \right]^{0.65} \left[ \frac{C_p \mu_l}{k_l} \right]^{-0.32} \left[ \frac{(\rho_v \lambda)^2}{(t_s + 273) \rho_l C_p \sqrt{\sigma(\rho_l - \rho_v)g}} \right]^{0.35}$$

(2.13)

Hughmark [38] made a statistical analysis of nucleate pool boiling data. The exponents of several variables were determined from an analysis of the data of 23 liquids. The expression so derived is as follows:

$$q = 2.67 \times 10^{-7} \left[ \frac{(\Delta p)^{1.867} (\rho_L - \rho_V)_w^{2.27} (C_L)_w^{0.945} T_s^{1.618}}{(\rho_V)_w^{1.385} (\mu_L)_w^{1.630} (\lambda)_w^{1.15} (P/P_c)^{0.202}} \right] \quad (2.14)$$

subscript w represents that the properties evaluated at wall surface temperature.

P is the ambient pressure on liquid, lb/sq.ft

P<sub>c</sub> is critical pressure, lb/sq.ft

ΔP is vapour pressure difference corresponding to ΔT, lb/sq.ft

Kutateladze [39] included the pressure term in his correlation. He recommended the correlation of the following form:

$$\frac{h}{k_l} \sqrt{\frac{\sigma}{(\rho_L - \rho_V) g}} = 7.0 \times 10^{-4} \left[ \frac{q}{\rho_V \lambda \alpha} \sqrt{\frac{\sigma}{(\rho_L - \rho_V) g}} \right]^{0.7} \left[ \frac{C_L \mu_L}{k_l} \right]^{-0.35} \left[ \frac{P}{\sigma(\rho_L - \rho_V) g} \right]^{0.7}$$

(2.15)

Kichigen and Tobilevich [39] obtained the boiling heat transfer correlation by analyzing the data for a number of fluids. Their correlation is of the following empirical form:

$$\frac{h}{k \ell} \sqrt{\frac{\sigma}{(\rho_l - \rho_v)g}} = 1.04 \times 10^{-4} \left[ \frac{q}{\rho_v \lambda \alpha} \sqrt{\frac{\sigma}{(\rho_l - \rho_v)g}} \right]^{0.7} \left[ \frac{P}{\sqrt{\sigma(\rho_l - \rho_v)g}} \right]^{0.7} \left[ \frac{g}{z \ell} \left( \frac{\sigma}{(\rho_l - \rho_v)g} \right)^{3/2} \left( 1 - \frac{\rho_v}{\rho_l} \right) \right]^{0.125} \quad (2.16)$$

Drayer [40] extended the nucleate boiling correlations to the nucleate boiling of cryogenic fluids-hydrogen. He examined 11 existing correlations, where three appeared directly applicable for the prediction of heat transfer coefficient for liquid hydrogen over limited ranges. The Forster-Zuber [22], Forster-Grief [33] and Cryder-Gilliland [2] relations yield heat flux values in good agreement with experimental data at temperature difference in the neighbourhood of 1°F. The correlations of Hughmark [38] Gilmour [23] and McNelly [20] were fair; and those of Levy [24], Jakob-Linke [4], Insinger-Bliss [7], Miyauchi-Yagi [37] and Nishikawa [26] were poor. Drayer advocates that several of these correlations could be made to agree with the experimental data merely by a readjustment of some of the arbitrary constants used.

Science et al [41] have studied the pool boiling of saturated hydrocarbons - ethane, propane, and n-butane outside a horizontal gold-plated cylinder. They succeeded in correlating all the data of the hydrocarbons except ethane by modifying the Rohsenow equation [14] in the following form:

$$\frac{q \sqrt{\frac{\sigma}{\rho_L - \rho_V}}}{\lambda \mu_l} = C \left[ \frac{C_f \Delta t}{\lambda} \left( \frac{1}{Pr} \right)^{1.18} (T_r)^{1.18} \right]^n \quad (2.17)$$

The constant  $C$  and exponent  $n$ , are given in Table 2.2

Table 2.2 Values of Constant  $C$  and Exponent  $n$  in Eq.(2.17)

Liquid	$C \times 10^{-5}$	$n$
Methane	3.25	2.89
Propane	5.77	2.60
n-Butane	2.33	2.84

Borishanskii et al [42] have studied heat transfer from a tube to water and ethanol in nucleate pool boiling. The tests were performed on three tube sizes having ID/OD equal to 6.12/6.94, 4.00/4.99 and 4.00/6.00. The majority of tests were made on first two tubes. The pressure range was 1.03 to 200  $\text{kg}_f / \text{cm}^2$  and heat flux range from  $50 \times 10^3$  to approximately  $1 \times 10^6$   $\text{kcal/hr m}^2$  for water. For ethanol the pressure ranged from 1 to 60  $\text{kg}_f / \text{cm}^2$  and heat flux from  $22 \times 10^3$  to  $700 \times 10^3$   $\text{kcal/hr m}^2$ . These investigators

concluded that the effect of pressure on heat transfer rate in nucleate boiling is expressed by a complex relationship and cannot be represented by a simple power law with a constant exponent on the pressure term.

Kosky and Lyon [35] have measured the nucleate pool boiling heat transfer data for pure nitrogen, oxygen, argon, methane and carbon tetrafluoride on a horizontal, flat, circular, platinum plated disk for saturation pressures ranging from 1 atm. or less to the immediate vicinity of the critical pressure. They compared all their experimental results for various fluids with several suggested nucleate boiling correlations [14], [20], [22], [23], [33], [39], [42]. These authors drew the conclusion that the Gilmour, McNelly, Kutateladze, and Borishanskii-Minchenko correlations are all superior to the Rohsenow and Forster-Zuber/Forster-Greif correlations with the following exceptions: (i) The degree of success for the Gilmour correlation holds only for nitrogen. (The order of success for the Gilmour correlation was  $N_2 > Ar > O_2 > CH_4 > CF_4$ ). (ii) The Forster-Zuber/Forster-Greif correlation was roughly as successful for the methane and carbon tetrafluoride data as any correlation tested by Kosky and Lyon but their emphasis is that those data are the poorest obtained in their work.



Frost and Li [47] attempted to evaluate the constant  $C_{sf}$  and exponent  $r$  in the Rohsenow pool-boiling correlation [14] for subatmospheric pressures. The range of vacuum pressure selected by these investigators was 0.92 psia - 14.45 psia. The test-pool consisted of distilled water filled in a vacuum tank made of pyrex. The heat transfer surface was electrically heated platinum wire of 0.008 in. diameter and 3 in. length.

The authors with the method of least squares fit found that the exponent  $r$ , varied from a minimum of 0.300 to a maximum of 0.377 in comparison to the value of 0.33 obtained by Rohsenow. The value of the constant of proportionality  $C_{sf}$  was obtained 0.01134 for a pressure of 14.45 psia compared to a value of 0.013 obtained by Rohsenow at atmospheric and higher pressures. However, the investigations of these authors indicate a significant effect of vacuum pressure on this constant. The values of constant  $C_{sf}$  and  $r$  are listed in Table 2.3 for the vacuum pressures investigated by these investigators. An examination of Table 2.3 shows that the vacuum pressure has little influence on the exponent  $r$  while it has a significant effect on the constant  $C_{sf}$  in the Rohsenow pool-boiling correlation.

Table 2.3 Values of Constant  $C_{sf}$  and Exponent  $r$  from [47]

Pressure psia	Constant $C_{sf}$	Exponent $r$
14.45	0.01134	0.325
4.12	0.00959	0.300
1.53	0.00902	0.377
0.92	0.00754	0.341

Rice and Calus [48] have carried out experimental investigations for calculating heat transfer coefficient during pool boiling. The liquids used were toluene, carbontetrachloride, methanol, n-propanol, isopropanol, water and water-isopropanol azeotrope at atmospheric pressure. The test surface was a 0.0315 cm. diameter nickle-aluminium wire 15.3 cm. long of which the 8.9 cm. midlength was used for heat transfer measurements. The wire was mounted horizontally under slight tension in a stainless steel yoke. The range of operating variables is given in Table 2.4.

The results of their investigation are correlated by the equation:

$$\frac{Nu}{K_p^{0.7}} \left[ \frac{T_s}{T_{sw}} \right]^4 = EP_e^{0.7} \quad (2.18)$$

Where  $T_s$  denotes absolute boiling point at system pressure,  $T_{sw}$  absolute boiling point of water at system pressure.

Table 2.4 Range of Operating Variables in [48]

	Atmospheric boiling point °C	Range of $\Delta T$ °C	Range of $q/A$ , $W/m^2$
Toluene	110.8	9.6-33.2	9,150-419,560
Carbon tetrachloride	76.8	11.9-24.7	35,330-307,570
Methanol	64.7	7.7-14.4	82,330-574,130
N-propanol	97.8	12.2-28.9	9,780-441,000
Isopropanol	82.5	6.8-15.1	22,710-401,900
Water	100.0	7.8-21.7	63,720-706,630
Water-isopropanol azeotrope	80.4	7.7-16.7	37,220-507,890

Equation (2.18) is a modification of the Borishanskii-Minchenko correlation [42]. The value of constant  $E$  is  $6.30 \times 10^{-4}$  for the surface used in their work. This correlation correlated experimental data of Cichelli and Bonilla [11] when the value of constant  $E$  was taken to be  $3.92 \times 10^{-4}$ . The different value of  $E$  has been explained due to different surfaces used by Cichelli and Bonilla. The experimental data of Borishanskii et al for water from stainless steel surface were also correlated by equation, Eq. (2.18) with constant  $E = 8.9 \times 10^{-4}$ .

## 2.2 SEMITHEORETICAL CORRELATIONS

Amongst the many other factors, number of nucleation sites on heating surface and their characteristics play a significant role in achieving high transfer rates in boiling of liquids. The vapour bubbles, during the course of their birth, growth, collapse or break-off the heating surface, give rise to large turbulence which accounts for high heat transfer rates. It can also be noted that the nucleation sites on heat transfer surface are effective in reducing the average wall superheat required for boiling and, hence, high boiling coefficients are realised.

A survey of literature demonstrates that several investigators, basing their conclusions on theoretical considerations or experimental evidence or both, have attempted to determine exactly how heat transfer rate, heat transfer coefficient, wall superheat and the number of nucleation sites are related.

Some of the investigators [49], [14], [50] have proposed a linear relationship between the heat flux and the number of active sites on a horizontal surface. This relationship was originally propagated by Jakob[49]. However, recent investigations [26],[46],[51],[52] raise doubts on the validity of the linear relationship.

Jakob and Linke [3],[4] were perhaps the first to develop a semitheoretical model for heat transfer coefficient considering the effects of turbulence caused due to birth, growth, collapse and break-off of vapour bubbles on the heating surface. In their model the influence of number of nucleation sites is accounted by  $nA_{b,1}/A$ . This ratio represents the fraction of heating surface which becomes vacant due to bubble break-off. The influence of the continual displacement of liquid which develops a circulation of liquid along each vapour column is taken into account by a quantity  $V_{b,2}/V_{b,1}$ . Hence they related heat transfer coefficient to these ratios, bubble diameter at break-off and thermal conductivity of the fluid in the following functional form:

$$\frac{h D_{b,1}}{k_f} = \Psi \left( \frac{n A_{b,1}}{A} \cdot \frac{V_{b,2}}{V_{b,1}} \right) \quad (2.19)$$

Using a linear relationship between the heat flux and the number of active sites on heating surface, equation, Eq.(2.19) has been reduced to the following form:

$$\frac{h D_{b,1}}{k_f} = \Psi \left( \frac{q}{\rho_v \lambda} \cdot \frac{1}{D_{b,1} f} \right) \quad (2.20)$$

Later, Jakob [3] from his photographic studies concluded that  $f D_{b,1}$  was nearly same for boiling water and carbon tetrachloride and approximately equals to 280 m/hr. Jakob and Linke [4] using photographic measurements reduced the Fritz equation [15].

Finally, using  $D_{b,1}$  from the reduced Fritz equation and  $fD_{b,1}$  equal to 280 m/hr these investigators showed that equation, Eq. (2.20) represented in the form given by Eq. (2.21)

$$\frac{h}{k_{\ell}} \sqrt{\frac{\sigma}{\rho_{\ell}}} = 30 \left( \frac{q}{\rho_v \lambda D_{b,1} f} \right)^{0.8} \quad (2.21)$$

Jakob [3] in 1938 reconsidered the above model with a view to provide general applicability for pressures other than atmospheric pressure. The modified form of Eq. (2.21) was obtained and is given by Eq. (2.22).

$$\frac{h}{k_{\ell}} \left[ \frac{\sigma}{(\rho_{\ell} - \rho_v)g} \right] = 31.6 \frac{v_{\ell,a}}{v_{\ell}} \left[ \frac{\rho_{\ell,a}}{\rho_{\ell}} \frac{\sigma}{\sigma_a} \frac{q}{\rho_{v,a} \lambda_a D_{b,a} f} \right]^{0.8} \quad (2.22)$$

Where the subscript 'a' denotes a physical property at the normal boiling point  $v_{\ell,a}/v_{\ell}$  has been included empirically. In the derivation of this equation  $D_{b,1}$  and  $f$ , and their product were considered to depend upon the pressure.

Jicina-Molozhin and Kutateladze [19] have scrutinized Jakob and Linke correlation [4] and Jakob correlation [3] for the experimental data for nucleate pool boiling of carbon tetrachloride, 26% water-glycerine solution, 24% aqueous sodium chloride solution, water and mercury. The pressure range for these experimental data was from 0.15 to 10.0 kg/cm<sup>2</sup>. These authors observed

that the Jakob correlation, Eq. (2.22), does not correlate the experimental data satisfactorily. The possible reason for the reported deviation has been that the Jakob correlation does not account for the effect of pressure on  $fD_b$ . Jakob assumed the value of  $fD_b$  a constant. These authors have related  $fD_b$  with pressure and physical properties of the liquid by the following expression:

$$fD_b = C_{sf} \sqrt{\frac{g \rho_l \sigma}{P \rho_v}} \quad (2.23)$$

Where  $C_{sf}$  represents liquid-solid combination factor and depends upon the wetting property of the liquid. Further, they found that their experimental data and those of Cryder and Finalborgo [5] are well-represented by the following equation:

$$\frac{h^*}{h_a^*} = \frac{k}{k_a} \frac{D_{b,a}}{D_b} \left[ \frac{\lambda_a \rho_{v,a}}{\lambda \rho_v} \right]^{0.7} \left[ \frac{f_a D_{b,a}}{f D_b} \right]^{0.7} \quad (2.24)$$

where  $h^* = \frac{h}{0.7}$ , and subscript a denotes a physical property at the pressure of 1 kg/cm<sup>2</sup>.

In 1952 Rohsenow [14] also attempted to derive equation for nucleate boiling heat transfer theoretically. He developed a correlation of Nusselt-Reynold-Prandtl type. Rohsenow defined the bubble Reynold number and bubble Nusselt number. The quantities needed for these dimensionless groups such as bubble diameter and product of bubble diameter and frequency were inserted from Fritz [15] and Jakob [3], [16]. Nevertheless, he

introduced a new dimensionless group  $C_{\ell} T_x / h_{fg}$  in place of bubble Nusselt number which represents the ratio of liquid superheat enthalpy at the surface temperature to the latent enthalpy of evaporation. The basic assumptions involved in this correlation are; (i) heat transfer rate per unit heating surface area,  $q$ , is proportional to the heat transfer rate to bubble per unit heating surface area while bubble remains attached to the surface  $(q)_b$ , (ii) the product of frequency and bubble diameter is constant as in the investigation of Jakob and Linke [4], and (iii) contact angle  $\beta$  remains independent of pressure and its effect has been considered through surface-liquid combination factor  $C_{sf}$ ;  $C_{sf} = \text{constant } (\beta)^r$ ,  $r = 0.33$ .

Rohsenow obtained the values of exponents over  $Re_b$  and  $Pr_b$  and value of  $C_{sf}$  by applying the proposed correlation to the data of Addoms [12] which cover the pressure range of 14.7 psia to 2465 psia. His correlation thus assumes the following form:

$$\frac{C_{\ell} T_x}{h_{fg}} = C_{sf} \left[ \frac{q/A}{\mu_{\ell} h_{fg}} \sqrt{\frac{g_0 \sigma}{g(\rho_{\ell} - \rho_v)}} \right]^{0.33} \left[ \frac{C_{\ell} \mu_{\ell}}{k_{\ell}} \right]^{1.7} \quad (2.25)$$

Equation (2.25) may be rewritten in the form:



$$\frac{h_x}{k_f} \sqrt{\frac{g_o \sigma}{g(\rho_f - \rho_v)}} = \frac{1}{C_{sf}} \left[ \frac{q}{\mu_f \lambda} \sqrt{\frac{g_o \sigma}{g(\rho_f - \rho_v)}} \right]^{0.667} \left( \frac{C_{sf} \mu_f}{k_f} \right)^{-0.7}$$

(2.26)

$$\text{or } Nu, b = \frac{1}{C_{sf}} (Re, b)^{0.667} (Pr)^{-0.7}$$

The value of  $C_{sf}$  in equation (2.25) are different for each of the surface-fluid combination and are given in Table 2.5 for the data of various investigators.

Table 2.5 Values of Constant  $C_{sf}$  in Eq. (2.25)

Surface-fluid combination	$C_{sf}$
Water-Nickle [17]	0.006
Water-Platinum [12]	0.013
Water-Copper [18]	0.013
Water-Brass [5]	0.006
$CCl_4$ - Copper [18]	0.013
Benzene - Chromium [11]	0.010
n-pentane-Chromium [11]	0.015
Ethanol-Chromium [11]	0.0027
Isopropanol-Copper [18]	0.0025
35% $K_2CO_3$ - Copper [18]	0.0054
50% $K_2CO_3$ - Copper [18]	0.0027
n-Butyl Alcohol-Copper [18]	0.0030

Forster and Zuber [22] expression is a modification of the Rohsenow correlation [14]. They developed their correlation based on a study of bubble dynamics. In this case the bubble growth rate was assumed to be the dominant mechanism. The bubble diameter used was:

$$D_b = \frac{(\Delta T) C_{\ell} \rho_{\ell} \sqrt{\pi \alpha}}{\lambda \rho_v} \left[ \frac{\rho_{\ell} R_i^3}{2\sigma} \right]^{1/4}$$

Their relationship between variables in the nucleate boiling regime is as follows:

$$\frac{C_{\ell} \rho_{\ell} \sqrt{\pi \alpha} Q}{k_{\ell} \lambda \rho_v A} \left( \frac{2\sigma}{\Delta P} \right)^{0.5} \left( \frac{\rho_{\ell}}{g \Delta P} \right)^{0.5} = 0.0015 \left[ \frac{\rho_{\ell}}{\mu_{\ell}} \left( \frac{C_{\ell} \rho_{\ell} \Delta T \sqrt{\pi \alpha}}{\lambda \rho_v} \right)^2 \right]^{0.62} \left( \frac{C_{\ell} \mu_{\ell}}{k_{\ell}} \right)^{0.33} \quad (2.27)$$

This rather formidable expression has not been extensively tested.

Levy [24] employed a simplified model of the boiling mechanism close to the heated surface. By utilising the bubble growth rate equation of Forster and Zuber [25] he deduced the following correlation:

$$q = \frac{k_{\ell} C_L \rho_L^2}{\sigma T_s (\rho_L - \rho_v)} \frac{1}{B_L} (\Delta T)^3 \quad (2.28)$$

The coefficient  $B_L$  was determined empirically employing the data of various investigators [11], [12], [18] and was found to be a function only of the product  $\rho_v h_{fg}$ .

To prove the validity of the recommended equation it was applied to the experimental data of several investigators [11], [12], [18] and they indicated that the proposed equation is of a generalised nature applicable to a widely differing fluids from low to very high pressures. He concluded that proposed equation is independent of heating surface-liquid combination. However, Levy noticed several deviations from the proposed equation and these were probably attributable to the evaluation of coefficient  $B_L$ .

Nishikawa et al [26], [32], [51] undertook a comprehensive investigation to determine the effect of surface nucleation sites on heat flux, heat transfer coefficient and wall superheat quantitatively. Based on their experimental data the following relationships have been concluded:

$$q \propto n^{1/2} \quad (2.29)$$

$$h \propto (fD_b^3 n)^{1/3} \quad (2.30)$$

$$\Delta T_w \propto q^{2/3} n^{-1/6} \quad (2.31)$$

Where  $n$  denotes the number of nucleation sites per unit area of the heating surface.

The applicability of these relationships has been reported for a pressure range of  $0.4 \text{ kg}_f/\text{cm}^2$  to

1.03 kg<sub>f</sub>/cm<sup>2</sup>, a heat flux range upto 66,000 kcal/hr m<sup>2</sup> and a maximum population count of 8 active sites per square inch.

The Nishikawa relationship for heat transfer coefficient has been successful in correlating experimental data of Kurihara and Myers [52] for water and four organic liquids at heat fluxes upto 92,500 kcal/hr m<sup>2</sup> and 28 active sites per square inch. Kurihara and Myers [52] have concluded that neither the degree of surface roughness nor the nature of liquid had an effect on the Nishikawa relationship between heat transfer coefficient and active-site population.

Nishikawa and Urakawa [26], [27], [29-32] undertook an investigation of nucleate boiling of water under reduced pressure ranging from 0.4 kg/cm<sup>2</sup> to atmospheric pressure both experimentally and analytically. The mechanism of boiling heat transfer has been discussed theoretically and the following expressions in dimensionless form have been recommended for heat transfer coefficient.

For laminar flow:

$$\frac{hR}{k_{\ell}} = 6.35 \left[ \left( \frac{1}{M_s^2 P} \frac{C_{\ell} \rho_{\ell}^2}{k_{\ell} \sigma \lambda \rho_v} \right)^{1/2} R^{3/2} q \right]^{2/3} \quad (2.32)$$

For turbulent flow:

$$\frac{hR}{k_{\ell}} = 8.26 \left[ \left( \frac{1}{M_s^2 P} \frac{C_{\ell} \rho_{\ell}^2}{k_{\ell} \sigma \lambda \rho_v} \right)^{1/2} R^{3/2} q \right]^{8/11} \quad (2.33)$$

Where;

$$M_s = 900, \text{ m}^{-1}$$

$$P = 1,699, \text{ kcal/h}$$

R = characteristic dimension of the heating surface.

The average line for experimental points can be represented by the following equation:

$$\frac{hR}{k_\ell} = 8.0 \left[ \left( \frac{1}{M_s^2 P} \frac{C_\ell \rho_\ell^2}{k_\ell \sigma \lambda \rho_v} \right)^{1/2} R^{3/2} q \right]^{2/3} \quad (2.34)$$

Eq. (2.34) is valid only for clean smooth heating surface under atmospheric pressure. This equation has been further generalised by including foamability factor,  $\frac{z}{z_s}$ , for the dirty or rough surface and pressure factor,  $\left(\frac{p}{p_s}\right)^{1/2}$ , pressures higher and lower than atmospheric. The final general correlation assumes the following form:

$$\frac{hR}{k_\ell} = 8.0 \left[ \left( \frac{z}{z_s} \right)^{1/2} \left( \frac{p}{p_s} \right)^{1/2} \left( \frac{1}{M_s^2 P} \frac{C_\ell \rho_\ell^2}{k_\ell \sigma \lambda \rho_v} \right)^{1/2} R^{3/2} q \right]^{2/3} \quad (2.35)$$

where;

$z$  = coefficient of foaming ability for any combination of surface and liquid.

$z_s$  = coefficient of foaming ability for the combination of clean smooth surface and pure liquid

$p$  = pressure

$p_s$  = atmospheric pressure

Forster and Greif [ 33 ] have analyzed the various proposed heat transfer mechanisms. They concluded that a vapour-liquid exchange mechanism can explain the rate of heat transfer in boiling. Two different correlations relating the boiling heat flux with superheat, system pressure and properties of the fluid have been proposed as follows:

$$q = c_1 \frac{k_\ell}{2\sigma} \Delta P \Delta T_1 \left( \frac{\rho_\ell}{\mu_\ell} A^2 \right)^{1/5} \left( \frac{\mu_\ell c_\ell}{k_\ell} \right)^{1/3} \quad (2.36)$$

and

$$q = 1.2 \times 10^{-3} \frac{\alpha c_\ell \rho_\ell (t_s + 273)}{\lambda \rho_v \sigma^{1/2}} \left( \frac{c_\ell (t_s + 273) \alpha}{(\lambda \rho_v)^2} \right)^{1/4} \left( \frac{\rho_\ell}{\mu_\ell} \right)^{5/8} \left( \frac{\mu_\ell c_\ell}{k_\ell} \right)^{1/3} \Delta P^2 \quad (2.37)$$

constant  $c_1$  was evaluated from the experimental data of Gunther and Kreith [34] and Cichelli and Bonilla [11] for water, the coefficient  $c_1$  was found to be  $0.7 \times 10^{-2}$ . Data only at pressures of 50 atm and 1 atm were compared. Eq. (2.36) was also tested for other liquids including mercury. The equation predicted the heat flux correctly for high and low pressure once the coefficient  $c_1$  was determined. From a measurement at atmospheric pressure, the coefficient  $c_1$  varied (from water to mercury) by a factor of 2.

Eq. (2.37) was tested by comparing with experimental data for the liquids: water from 1 to 50 atm, n-butyl alcohol for 50 psia, aniline for 35 psia and mercury for 1 and 3 atm.

It is important to note that the above equations assume the following relationship:

$$\left[ \frac{d(\log \Delta T_1)}{d(\log p)} \right]_{q = \text{constant}} = -\frac{1}{4}$$

The above relationship holds true for low pressures. Obviously these correlations might not correlate the boiling heat transfer data for high pressures. This has been pointed out by Leinhard in his private communication to Kosky and Lyon [35]. Another point can also be noted that these authors did not use the value of  $D_b$  as its determination was not known to these authors. Therefore, they have argued from physical considerations the important parameters and dimensionless groups which can be used to describe the heat transfer based on vapour-liquid exchange mechanism.

Miyauchi and Yagi [37] studied the relationship between heat transfer coefficient and the population of active nucleation sites. Their resulting expression, which has two dimensionless groups is ;

$$\frac{h}{k_{\ell}} = c_1 \left( \frac{q \rho_{\ell}}{\lambda \rho_v \mu_{\ell}} \right)^{0.74} \left( \frac{\rho_v}{\rho_o} \right)^{0.69} \left( \frac{c_{\ell} \mu_{\ell}}{k_{\ell}} \right)^{0.63} \quad (2.38)$$

Coefficient  $c_1$  depends on the roughness of the heating surface and on the liquid employed.  $\rho_o$  is the vapour density at atmospheric pressure in lb/cu. ft.

Gaertner and Westwater [46] carried out photographic investigation to determine the effect of population of active sites on boiling heat transfer rates. The experimental facility used by them consisted of 20% aqueous solution of nickel salt boiling at atmospheric pressure on a horizontal, flat, copper surface 2 in. in diameter. The heat flux was varied from 7,680 to 535,000 Btu/hr sq. ft and the  $\Delta T$  from 17.3°F to 218.8°F. Based on experimental data the following relationships for heat flux and heat transfer coefficient in terms of active-site population have been proposed:

$$q = 1400 n^{0.47} \quad (2.39)$$

$$h = 49 n^{0.33} \quad (2.40)$$

In 1969 Mikic and Rohsenow [43] have studied boiling heat transfer analytically. Starting with the basic mechanism for a single active cavity site, these authors have related average heat flux from the heated surface to the active-site density, the average frequency for bubble departure, the bubble diameter at departure and



wall superheat. They have used the results of Brown [53] for determining the number of active-sites. The number of active-sites is first related to the surface cavity distribution and then to fluid properties and the wall superheat by the following expression:

$$n = c_1 r_s^m \left( \frac{\lambda \rho_v}{2T_s \sigma} \right)^m \Delta T^m \quad (2.41)$$

Where  $r_s$  is a radius for which  $n$  would be one per unit area, and  $c_1$  is dimensional constant (1/unit area). The value for  $m$  was taken to be 2.5 for water and 3.0 for n-pentane, benzene, and ethanol.

The heat flux is related to the pertinent quantities by the following functional equation:

$$q = c_1 \frac{r_s^m}{\sqrt{\pi} 2^{m-1}} (k \rho C)^{1/2} \left( \frac{\lambda \rho_v}{T_s \sigma} \right)^m \sqrt{f} D_b^2 \Delta T^{m+1} \quad (2.42)$$

Equation (2.42) was derived by assuming that the main mechanism of heat transfer in nucleate boiling is transient heat conduction to, and subsequent replacement of, superheated layer around boiling sites associated with bubble departure. The correlation incorporates effects of heat transfer surface characteristics through the quantities  $c_1$  and  $r_s$  and thus allows for direct forms of  $q$  vs  $\Delta T$  relations.

Following the model as above the heat flux due to the boiling alone from the heated surface has been related to the wall superheat and pertinent fluid properties by the equation:

$$(q)_b = c_1 \frac{c_2 c_3^{1/2} r_s^m}{\sqrt{\pi} 2^{m-1}} (k \rho c)^{1/2} \left( \frac{\lambda \rho_v}{T_s \sigma} \right)^m$$

$$\left[ \frac{\sigma g_0 g (\rho_\ell - \rho_v)}{\rho_\ell^2} \right]^{1/8} \left[ \frac{\sigma g_0}{g (\rho_\ell - \rho_v)} \right]^{3/4} (Ja^*)^{15/8} \Delta T^{m+1}$$

$$(2.43)$$

Where,  $c_1$  = dimensional constant (1/unit area)

$c_2 = 1.5 \times 10^{-4}$  for water

$= 4.65 \times 10^{-4}$  for other liquids

$c_3 = 0.6$  is chosen as an average value

$Ja^*$  = Modified Jakob number  $\left[ \frac{C_\ell \rho_\ell T_s}{\rho_v \lambda} \right]$

$m = 2.5$  for water

$= 3.0$  for liquids: n-pentane, benzene and ethyl alcohol

or normalising heat flux:

$$\frac{(q)_b}{\mu_\ell \lambda} \sqrt{\frac{\sigma}{g (\rho_\ell - \rho_v)}} = B (\phi \Delta T)^{m+1} \quad (2.44)$$

Where,

$$\phi^{(m+1)} = \frac{k_\ell^{1/2} \rho_\ell^{17/8} c_\ell^{19/8} \lambda^{(m - \frac{23}{8})} \rho_v^{(m - \frac{15}{8})}}{\mu_\ell \left[ (\rho_\ell - \rho_v) \right]^{9/8} \sigma^{(m - \frac{11}{8})} T_s^{(m - \frac{15}{8})}}$$

and B is a dimensional constant which depends on boiling surface properties and gravity and is given by

$$B = \left( \frac{\gamma_s J}{2} \right)^m \frac{2}{\sqrt{\pi}} \frac{(g_o)^{11/8}}{(g)^{9/8}} c_2^{5/3} c_3^{1/2} c_1$$

In order to derive equation, Eq.(2.43) the diameter of bubble size at departure was calculated from the expression of Cole and Rohsenow [44] and  $fD_b$  as recommended by Cole [45].

The validity of this equation, Eq.(2.43) was tested by using the experimental data of Addoms [12], and Cichelli and Bonilla [11]. The proposed correlation was also found to be consistent with the low heat flux data of Gaertner and Westwater [46].

Wiebe and Judd [54] conducted an experimental investigation of temperature profiles in water boiling on a horizontal copper surface for incipient boiling conditions. They used 20,000, 50,000 and 100,000 Btu/hr.ft<sup>2</sup> heat flux while changing the subcooling from 0 to 105 °F. The temperature profiles obtained enabled the extrapolated superheated layer,  $\delta$  to be evaluated as follows:

For values of  $(N/A) f < 55 \times 10^3$  bubbles/in<sup>2</sup>-sec.

$$\delta \propto [(N/A) f]^{-1/2} \quad (2.45)$$

For  $(N/A) f > 55 \times 10^3$  bubbles / in<sup>2</sup>- sec

$$\delta \propto [(N/A) f]^{-1/3} \quad (2.46)$$

They have also deduced the following respective equations for heat flux as function of active site density,  $N/A$  and frequency of bubble emission, for the above two conditions:

$$\frac{Q}{A} \propto [(N/A) f]^{1/2} (T_w - T_\infty) \quad (2.47)$$

and

$$\frac{Q}{A} \propto [(N/A) f]^{1/3} (T_w - T_\infty) \quad (2.48)$$

Aladev [55] has studied the mechanism of heat transfer in nucleate boiling. Among many other aspects, he has attempted, the procedure for determining the heating surface temperature from which heat is transported to the boiling liquid. He has successfully correlated the experimental data for pool boiling of distilled water only for pressure range 0.09 to 200 atmospheres by the following equation:

$$\frac{\Delta T_w}{T_s} = 4.7 \times 10^{-3} \left[ \frac{10^{-6} q \lambda}{k_f T_s g} \right]^{0.3} \left[ \frac{\lambda}{C_f T_s} \right]^{1.2} \quad (2.49)$$

### 2.3 SELECTED CORRELATIONS FOR POOL BOILING

Preceding sections contain a chronological literature survey of nucleate pool boiling of liquids. It shows that a large number of correlations for computing boiling heat transfer coefficients have been obtained. These correlations have been found suitable for given boiling liquids and boiling situations namely; wall heat flux, system pressure, surface -liquid combination and boiling fluids. Therefore, in order to compare the present and existing experimental data with the predictions from correlations, it is necessary that these correlations satisfy the following:

- (i) The correlations are to be for boiling from the outer surface of a horizontal tube immersed in a pool of fluid.
- (ii) The correlations are to be for low heat flux values.
- (iii) The correlations are to be for the system at atmospheric and/or subatmospheric pressures.
- (iv) The correlations are to be for the boiling liquids whose physico-thermal properties were similar to those of distilled water, isopropanol, ethanol and methanol.
- (v) The correlations are to be typical to represent the different major approaches, namely; based on empirical methods, based on the Jakob Linear

Relationship between heat flux and number of active-sites, based on non-linear relationship between heat flux and number of active sites.

The selected correlations are listed in Table 2.6.

TABLE 2.6 Selected Correlations\* for Pool Boiling

Author	System Parameter		Type of correlation	Remarks
	Fluids	Pressure Range		
Jakob and Linke[3]	Water and carbon tetra-chloride	Atmospheric and greater than atmospheric	Semi-analytical	Refer Eq.(2.22)
Labuntsov [36]	-	Atmospheric	Empirical	Refer Eq. (2.13)
Kutateladze [39]	-	0.2-10 atm.	Empirical	Refer Eq. (2.15)
Kichigen and Tobilevich [39]	Many fluids	Atmospheric	Empirical	Refer Eq.(2.16)
Forster and Greif [33]	Water, n-butyl alcohol, Aniline, Mercury	1-50 atm 50 psia 35 psia 1-3 atm	Vapour-liquid exchange mechanism	Refer Eq.(2.37)
Mikic and Rohsenow [43]	Water, ethyl-alcohol, n-pentane, & benzene	Wide range of pressure (atmospheric and greater than atmospheric)	Analytical	Refer Eq.(2.44)

\* Equations transformed to as per SI units requirements

## 2.4 SURFACE CHARACTERISTICS AND BUBBLE DYNAMICS

Attempts to correlate nucleate boiling heat transfer data through fluid properties alone have failed, because the surface characteristics have a pronounced effect on the boiling phenomenon. Boiling heat transfer is characterized by the formation of small vapour bubbles at the active-sites and the bubble dynamics - growth rates, frequencies, bubble sizes at departure and interaction with the bulk liquid directly determine the amount of heat transferred. The mechanism of bubble growth rates has been extensively investigated [56-58],[25],[59-86]. The mechanism of bubble departure was investigated originally by Fritz [15] based on a static balance between the buoyant force and the surface tension force at the bubble base. Subsequently, it has been found that the Fritz equation is not of general applicability. With various ramifications the mechanism of bubble departure diameter has been reported successively by many investigators [87-100].

Recently, some attempts have been made to derive theoretical equations for predicting boiling heat transfer rates based on heating surface characteristics, bubble dynamics and boiling mechanisms.

In this section, some of the investigations pertaining to the heating surface characteristics, the bubble growth rate, the bubble diameter at departure and

the bubble emission frequency have been dealt with.

#### 2.4.1 Surface Characteristics

Kurihara and Myers [52] developed an equation which relates the temperature difference and surface conditions with the active site density. Their correlation failed to predict the active site density at a particular set of conditions. However, it could predict the difference in active site density between two different conditions.

Gaertner [101] undertook the study to relate the active site density to the surface temperature. His study concluded the following equation for site density:

$$(N/A) = N_0 \exp(-k/T_w^3) \quad (2.50)$$

where,  $k$  is a constant which is a function of fluid properties and surface conditions.  $N_0$  is a constant.

Griffith and Wallis [102] undertook a study to investigate the role of surface conditions in nucleate boiling. For their investigation they made single cavities on different copper surfaces finished with emery paper and obtained boiling data for water, methanol and ethanol. They concluded that the mouth diameter of the cavity determines the superheat needed to initiate boiling, and its shape determines its stability once boiling has begun. On the basis of single-cavity nucleation theory, they proposed that the gross nucleation properties of a



given surface for all fluids under all conditions can be characterized with a single group having the dimensions of length. This group  $r_c = [ 2 \sigma T_s / \rho_v (T_w - T_s) \lambda ]$  when plotted against active site density  $N/A$  for a particular surface gave a single plot. Consequently, it was concluded that the nucleation characteristics of a surface would be known if the size distribution of active sites on the surface were known.

Brown [53] used different surfaces with various surface finishes in his studies for bubble nucleation. Brown found that a number of active sites per unit area with radii larger than  $r_c$  could be correlated by the following equation:

$$N/A = c_1 \left( \frac{r_s}{r_c} \right)^m \quad (2.51)$$

where  $r_s$  is a radius for which  $n$  would be unity per unit area and  $c_1$  is a dimensional constant having dimensions of  $(\text{unit area})^{-1}$  and  $r_c$  is critical radius equal to  $[ 2 \sigma T_s / \rho_v \lambda (T_w - T_s) ]$ .

Shoukri and Judd [103] have shown that Brown relationship could correlate their experimental data. The parameter group  $[ 2 \sigma T_s / \rho_v \lambda (T_w - T_s) ]$  is recommended for predicting the minimum nucleation cavity radius and therefore, the usage of this parameter group with Brown correlation is recommended as a sufficient method for describing the nucleation characteristics of a boiling surface.

### 2.4.2 Bubble Growth Rate

The process of nucleate boiling is the sum total of the processes of bubble initiation, growth and departure. Bubble growth rates have been investigated quite extensively for fluids such as water and methanol boiling from solid surfaces under conditions of atmospheric pressure or greater corresponding to Jakob numbers less than 50 [88], [104-106]. However, considerably little attention has been paid to growth rates at subatmospheric pressure conditions.

Zuber [62] studied the bubble growth rate on solid surfaces. Zuber expression for bubble growth is as follows:

$$D = \phi_c \frac{L}{\pi} J_a \sqrt{\pi \alpha t} \left[ 1 - \frac{q \sqrt{\pi \alpha t}}{2k_f(T_w - T_s)} \right] \quad (2.52)$$

Hsu and Graham [105] recommended the following bubble growth equation in a non-uniform temperature field:

$$D = \frac{\pi}{\lambda \rho_v} \left\{ \frac{qt}{2\pi} + \frac{2q \delta^2}{\alpha \pi^2} \left( \frac{\pi^2}{6} \sum_{n=1}^{\infty} \frac{1}{n^2} \exp \left[ -\left(\frac{\pi n}{\delta}\right)^2 \alpha t \right] \right) \right\} \quad (2.53)$$

Han and Griffith [106] took into consideration the curved surface of the bubble covered by a hot liquid microlayer. Their growth equation is as follows:

$$D = \frac{\phi_s \phi_c}{\phi_v} \frac{2k}{\lambda \rho_v} \left\{ \frac{2(T_w - T_s)}{\sqrt{\pi \alpha}} t^{1/2} - \frac{(T_w - T_o)}{\delta} \frac{\delta^2}{4\alpha} \right. \\ \left. \left( \frac{4\alpha t}{\delta^2} \operatorname{erf} \frac{\delta}{\sqrt{4\alpha t}} + \frac{2}{\sqrt{\pi}} \frac{\sqrt{4\alpha t}}{\delta} \exp \left[ -\frac{\delta^2}{4\alpha t} \right] - \operatorname{erf} C \frac{\delta}{\sqrt{4\alpha t}} \right) \right\} \quad (2.54)$$

Mikic and Rohsenow [74] developed the following equation for bubble growth in non-uniform temperature field:

$$R^+ = (\tau^+)^{1/2} \left[ 1 - \theta_1 \left\{ \left(1 + \frac{\tau_w^+}{\tau^+}\right)^{1/2} - \left(\frac{\tau_w^+}{\tau^+}\right)^{1/2} \right\} \right] \quad (2.55)$$

Cole and Shulman [66] have scrutinized the existing theories for bubble growth in a non-uniform temperature field for subatmospheric conditions. Comparison of all of the non-uniform temperature field growth equations [62] [63], [105], [106] with the experimental data indicates them to be less satisfactory than the uniform superheat expression given by  $D = Ja \sqrt{\pi \alpha t}$ . As a matter of fact the reasonable agreement with the magnitude of the growth data is obtained only for Jakob numbers less than 100. Above this value these authors obtain increasingly greater discrepancy between theory and experiment. Finally they recommended two separate expressions for bubble growth in an non-uniform temperature field as follows:

For  $Ja < 100$

$$D = Ja \sqrt{\pi \alpha t} \quad (2.56)$$

For  $Ja > 100$

$$D = 5 Ja^{3/4} \sqrt{\alpha t} \quad (2.57)$$

Stewart and Cole [83] have investigated the bubble growth rates experimentally in order to determine the effect of high Jakob number conditions. In their studies Jakob number ranged from 955 to 1112. This study concludes that liquid inertia is a major factor restricting the rate of growth of vapour bubbles at low pressures.

van Stralen et al [85] have investigated experimentally the growth rate of vapour bubbles upto departure in water boiling at pressures varying from 26.7 to 2.0 kPa which correspond to Jakob number range from 108 to 2689. During initial growth the results of Stewart and Cole [83] as regards the influence of liquid inertia are established. Experimental bubble growth is in quantitative agreement with the van Stralen et al theory [84].

#### 2.4.3 Bubble Departure Diameters at Subatmospheric Pressure

Cole and Shulman [95] conducted a careful literature review for the expressions for bubble departure diameter [15], [87-94] which were developed either

theoretically or empirically. They recommended that none of the correlations tested were able to satisfactorily represent subatmospheric departure diameter data. As a result of the fact that none of the correlations are very satisfactory, it is recommended that the following equation of dimensionless departure diameter with pressure be employed to obtain order of magnitude estimates of the departure diameter:

$$\frac{D_b}{\left[ \frac{\sigma}{g(\rho_l - \rho_v)} \right]^{1/2}} = \frac{133.3}{P} \quad (2.58)$$

where  $P$  is in  $\text{kN/m}^2$ .

This expression covers the widest range of experimental conditions and does not require a knowledge of heat flux level or wall superheat. In addition it also satisfies the equation recommended by Nishikawa and Urakawa [89]. Their equation is as follows:

$$D_b = 0.672 P^{-0.575} \quad (2.59)$$

Where  $D_b$  is in inches and  $P$  is in psia.

Departure equation proposed by Cole [45] shows that the departure diameter is directly proportional to wall superheat. The equation is:

$$\frac{D_d}{\sqrt{\frac{\sigma}{g(\rho_l - \rho_v)}}} = 4 \times 10^{-2} Ja \quad (2.60)$$

Recently Cole and Rohsenow [44] have attempted to modify the previous correlations, proposed by Cole and Shulman [95] and Cole [45] for bubble departure diameter. These investigators argued that wall superheat, which appears in Jakob number, was not available for high pressure data and thus previous correlations could not be tested for the pressures greater than one atmospheric due to the lack of this information.

In this attempt Cole and Rohsenow have proposed a modified Jakob number which is free from the wall superheat term:

$$Ja^* = \frac{\rho_l c_l T_s}{\rho_v \lambda}$$

and they have recommended the correlations for bubble departure diameter by using this modified Jakob number. In their support to delete the wall superheat term they have mentioned the previous work [104], [107], [108], where it was found that corresponding to wall superheats ranging from 20° to 30°F, the arithmetic mean departure diameter to be approximately constant. The work of Preckshot and Denny [96], where wall superheat range was 40 to 70 °F,

found an increase in departure diameter with increase in wall superheat and a decrease in this diameter with increase in active nucleation site density. Thus a surface consisting of natural nucleation sites, where both the wall superheat and bubble population density increase with heat flux level, would essentially yield a constant departure diameter due to the counteracting of each others effect. Cole and Rohsenow thus advocate that either the effect of bubble population density should be taken into account or the variation with a wall superheat term should be removed to define the bubble departure diameter. Because of the fact that no detailed experimental studies for the effect of bubble population on departure diameter is available, the Jakob number has been modified in a manner as mentioned above.

Based on the experimental departure diameter data of various workers they have proposed two different correlations for water and other liquids.

The correlation for water is based on the experimental departure data of Semeria [91] for pressures 2 to 140 atmospheres, Tolubinskii and Ostrovsky [70] for pressures ranging from approximately 0.2 to 10 atmospheres, Cole [45] for pressures ranging from 0.066 to 0.470 atmospheres, Hatton and Hall [108] for pressures ranging from 0.12 to 1 atmosphere and Siegel and Keshock [109] for 1 atmosphere.

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The correlation is:

$$\frac{D_d}{\sqrt{\frac{\sigma g_c}{g(\rho_l - \rho_v)}}} = 1.5 \times 10^{-4} (Ja^*)^{5/4}; \text{ for } Pr \leq 0.2 \quad (2.61)$$

And the correlation for other liquids is based on the experimental departure diameter data of Wanninger [110] for propane at pressures of 8.5, 11 and 14 atmosphere and iso-pentane at 1 atm; Cole [45] for toluene, n-pentane methanol, carbon tetrachloride and acetone at pressures ranging from 0.066 to 1 atm; Tolubinskii and Ostrovsky [70] for benzene, n-butyl alcohol and Freon-12 at 1 atmosphere; McFadden and Grassmann [111] for nitrogen at 1 atmosphere; Perkins and Westwater [114] for methanol at 1 atmosphere; Preckshot and Denny [96] and Jakob [3] for carbon tetrachloride at 1 atm. The correlation is:

$$\frac{D_d}{\sqrt{\frac{\sigma g_c}{g(\rho_l - \rho_v)}}} = 4.65 \times 10^{-4} (Ja^*)^{5/4}; \text{ for } Pr \leq 0.2 \quad (2.62)$$

The deviation of experimental data from either equation is approximately  $\pm 50\%$ . The authors point out that the deviation is due to result of neglecting the bubble population density, dynamic contact angle, active



cavity size and wall superheat.

#### 2.4.4 Bubble Emission Frequency at Subatmospheric Pressures

The availability of accurate and precise correlations for bubble emission frequency,  $f$ , and bubble departure diameter,  $D_b$  provides a good opportunity for deriving equations for heat transfer coefficient analytically. The determination of relationship between  $f$  and  $D_b$  has been a subject of active research. Consequently a good amount of information [3],[19],[70],[87],[88],[106],[108],[109],[111-120] exists which contains results based on one or other approaches. Recently Ivey [118] has attempted to scrutinize all the available investigations and put them in a rational form. He concludes that a single expression may not adequately correlate bubble frequency with bubble diameter for all bubble diameters in nucleate boiling. He suggests three separate regions with which the experimental data are better correlated. The regions are hydrodynamic, transition and thermodynamic.

It seems that exclusive correlations for bubble emission frequency are non-existent but for the correlations due to Han and Griffith [106], Hatton and Hall [108] and Saini [86].

Han and Griffith [106] have studied the mechanism of heat transfer in nucleate pool boiling. In addition to bubble initiation, growth and departure they recommended

the calculation of bubble emission frequency by the following equation:

$$f = \frac{1}{\theta_d + \theta_w} \quad (2.63)$$

In equation (2.63) waiting period  $\theta_w$  is expressed by the following expression:

$$\theta_w = \frac{\delta^2}{\pi \alpha} = \frac{g}{4 \pi \alpha} \left[ \frac{(T_w - T_\infty) R_c}{T_w - T_{\text{sat}} [1 + (2\sigma/R_c \rho_v \lambda)]} \right]^2 \quad (2.64)$$

and departure time  $\theta_d$  can be obtained by solving following equations:

$$R_d = 0.4251 \phi \left[ \frac{2\sigma}{g(\rho_l - \rho_v)} \right]^{1/2} \quad (2.65)$$

$$R - R_c = \frac{\phi_s \phi_c}{\phi_v} \frac{\alpha c \rho}{\rho_v \lambda} \left[ \frac{2\theta_w}{(\pi \alpha)^{1/2}} t^{1/2} - \frac{\theta_w - \theta_\infty}{\delta} \frac{\delta^2}{4\alpha} \left( \frac{4\alpha t}{\delta^2} \operatorname{erf} \frac{\delta}{(4\alpha t)^{1/2}} + \frac{2}{(\pi)^{1/2}} \frac{(4\alpha t)^{1/2}}{\delta} \exp[-\delta^2/4\alpha t] - 2 \operatorname{erfc} \frac{\delta}{(4\alpha t)^{1/2}} \right) \right] + \frac{\phi_h h_v \theta_w}{\phi_v \rho_v \lambda} t \quad (2.66)$$

Hatton and Hall [108] used the bubble growth equation of Plesset-Zwicky [57] for departure time,  $\theta_d$  and

Hsu [121] and Han - Griffith [106] expression for bubble nucleation for calculating the bubble emission frequency under the assumption of  $\theta_w = 0$ . The final form of the equation is as follows :

$$f = \frac{1}{\theta_d} = \frac{3}{\pi \sigma} \left[ \frac{16 k \sigma T_s}{(\lambda \rho_v)^2 D D_c} \right]^2 \quad (2.67)$$

Cole [45] has proposed the expressions for bubble frequencies and departure volumes for nucleate pool boiling of liquids at subatmospheric pressures. His expressions are the modifications over the expression which have been proposed by previous workers, who have not taken into account the effect of pressure and heat flux over the volumetric vapour flow rate ( $f D_b^3$ ). Recent experimental investigations [120] has determined that the volumetric vapour flow rate for the isolated bubble region in nucleate boiling is a function of both the heat flux and pressure. Thus in establishing the expressions for  $f D_b^3$  or  $f D_b$  these variables should be taken into account. Since the heat flux is proportional to the degree of superheat, and system pressure can be taken into account through vapour density term, the Jakob number can be included while developing the expressions for  $f D_b^3$  or  $f D_b$ .

With the aid of his own experimental data and the data of other workers Cole proposed the following expressions:

$$fD_b^3 \propto \left[ \frac{\sigma^{5/3}}{g \rho_\ell^{2/3} (\rho_\ell - \rho_v)} \right]^{3/4} \left[ \frac{\rho_\ell C_\ell \Delta T}{\rho_v \lambda} \right]^2 \quad (2.68)$$

where,

$$\frac{\rho_\ell C_\ell \Delta T}{\rho_v \lambda} = Ja$$

and the volumetric vapour flow rate per cross section is

$$fD_b \propto \left[ \frac{g(\rho_\ell - \rho_v)\sigma}{\rho_\ell^2} \right]^{1/4} \quad (2.69)$$

which is independent of Jakob number.

Based on the bubble departure diameter expressions of Saini et al [122] Saini [123] developed three different expressions for bubble emission frequency. His expressions for different range of Jakob number are as follows:

For  $Ja \leq 16$

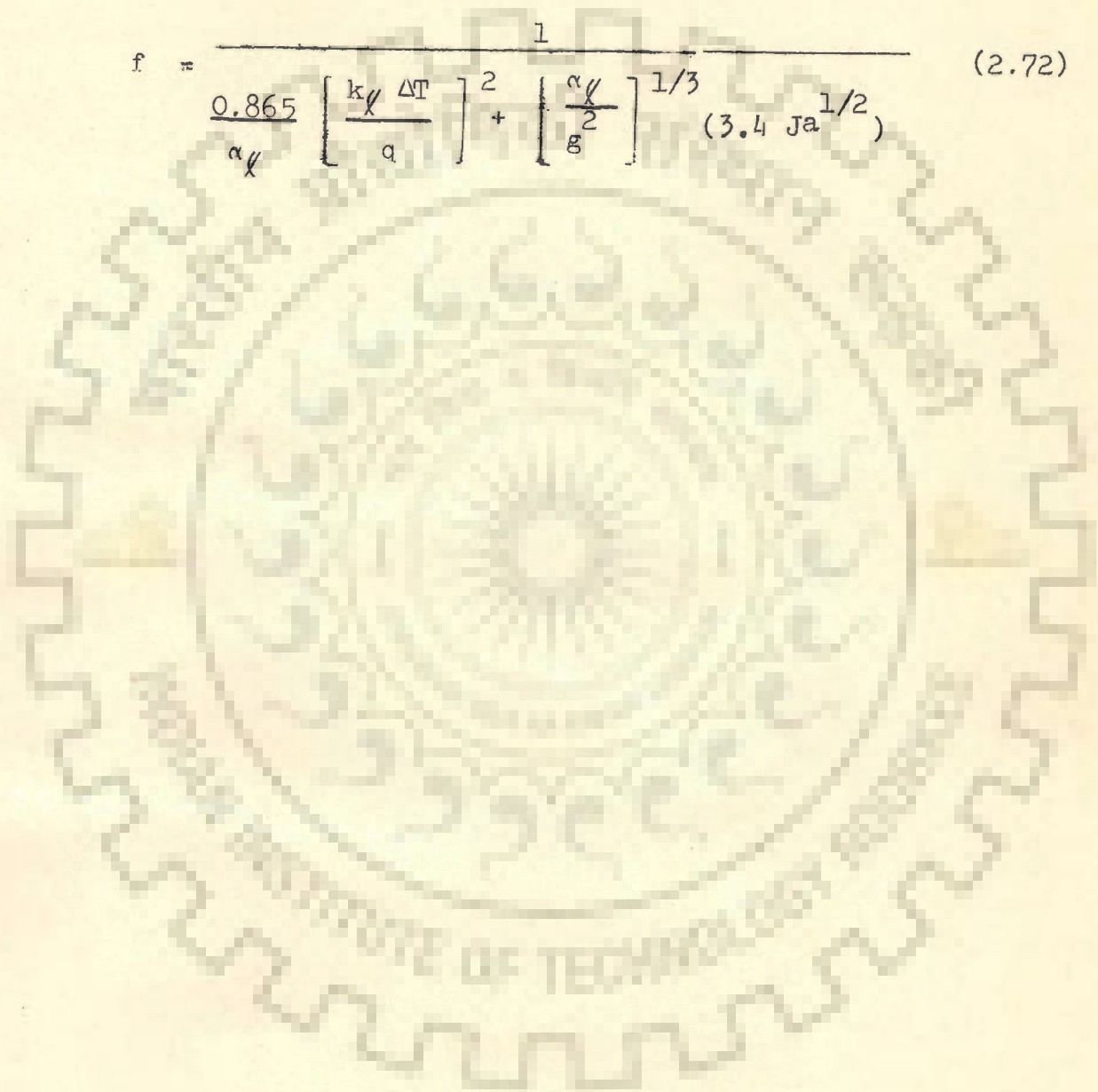
$$f = \frac{1}{\frac{0.865}{\alpha_\ell} \left[ \frac{k_\ell \Delta T}{a} \right]^2 + \left[ \frac{\alpha_\ell}{g^2} \right]^{1/3} \left[ \frac{6.6 C_\ell \Delta T \sigma}{\alpha_\ell a} \right]^{2/3} / (\pi Ja^2)} \quad (2.70)$$

For  $16 < Ja < 100$

$$f = \frac{1}{\frac{0.865}{\alpha_\ell} \left[ \frac{k_\ell \Delta T}{a} \right]^2 + \left[ \frac{\alpha_\ell}{g^2} \right]^{1/3} \left[ 0.578 Ja^{2/3} \left\{ 1.22 + \sqrt{1 + 2.67 \frac{C_\ell \Delta T \sigma}{\alpha_\ell a Ja}} \right\} \right]^{4/3}} \quad (2.71)$$

For  $Ja \gg 100$

$$f = \frac{1}{\alpha_f \left[ \frac{k_f \Delta T}{q} \right]^2 + \left[ \frac{\alpha_f}{g} \right]^{1/3} (3.4 Ja^{1/2})} \quad (2.72)$$



## CHAPTER 3

### EXPERIMENTAL APPARATUS

#### 3.1 DESIGN CONSIDERATIONS

As a large diameter heating surface was employed in the present investigation, it was expected that the variation in surface temperature around the circumference of the heating surface might exist. This could also be able to furnish the information about the changes in local values of heat transfer coefficient. Therefore, an important consideration was the location of surface thermocouples at different circumferential positions. Considering the bubble dynamics on the heating surface it would be required that the temperatures are measured at least at the top, at the side and at the bottom positions of the surface. This information can also be utilised for averaging the surface temperature by the method of mechanical quadrature.

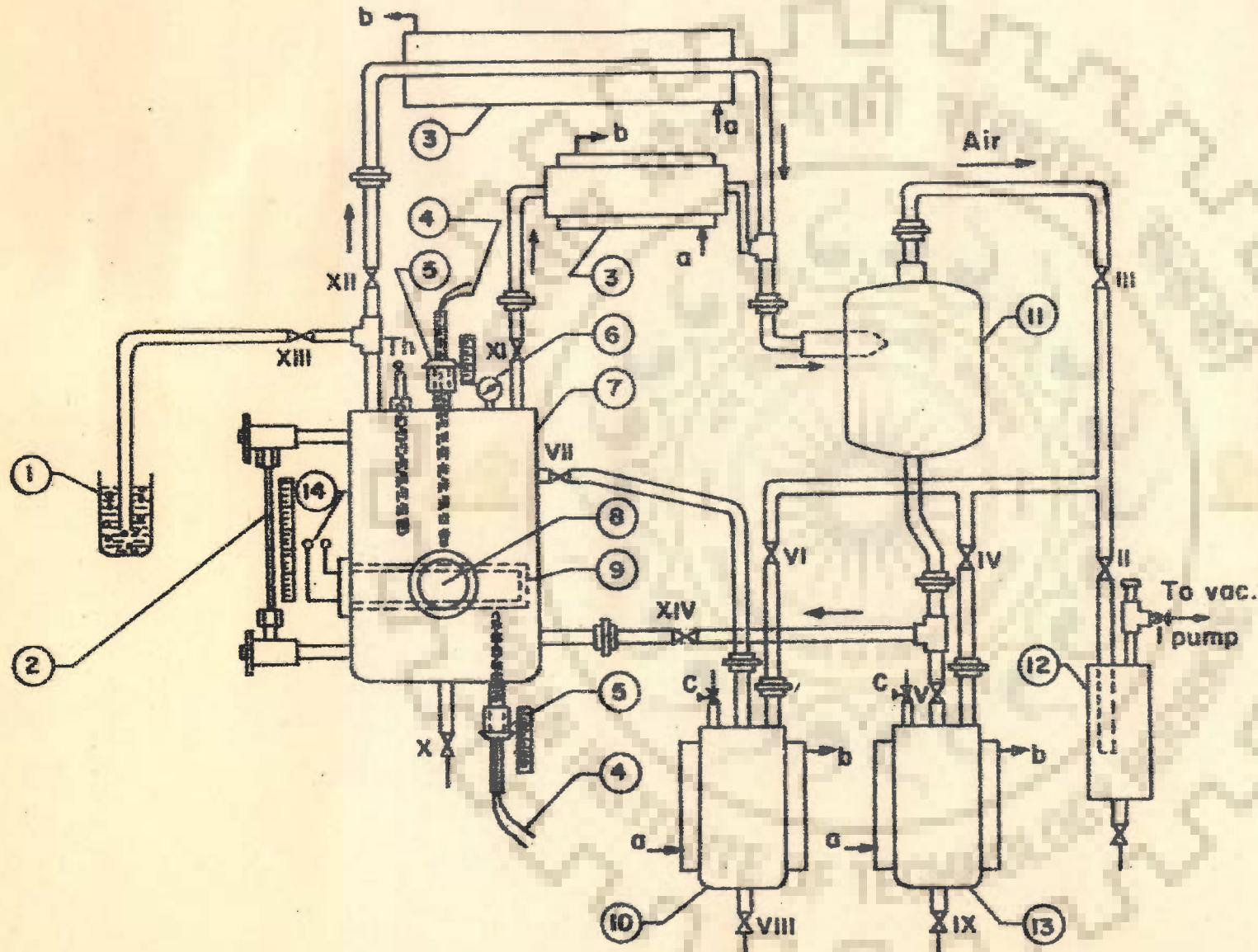
Boiling fluid temperature changes around the heating surface and the heating surface is enveloped by the superheated layer of the liquid. Therefore, another important consideration was as to where measure the temperature of the boiling fluid. It was also necessary to measure liquid temperature corresponding to three above mentioned positions of wall thermocouples so that local values of

heat transfer coefficient could be calculated. For calculating heat transfer coefficient, the temperature of the fluid was measured at a point outside the superheated layer. It is important at this stage to mention that the thickness of superheated liquid layer does not remain constant and it changes with the parameters namely; heat flux, pressure and properties of boiling fluids. Therefore, it was required to vary the position of the fluid thermocouples depending upon system parameters and conditions. To meet these requirements movable thermocouple probes are required.

The apparatus used in the present study was designed to conduct experiments on binary liquid mixtures as well. Therefore, design consideration was made for drawing the liquid sample and the equilibrium vapour-condensate. To keep the composition of boiling mixture at a given value it was necessary to return the vapour condensate from the condensers back to the pool of boiling fluid. The vapour condensate return line and the liquid sampling line could alter the hydrodynamic conditions in the neighbourhood of the heating surface. Therefore, special care was taken to keep these lines sufficiently away from the heating surface.

### 3.2 EXPERIMENTAL FACILITY

An experimental facility for studies in nucleate pool boiling was designed and fabricated. It is depicted schematically in Figure 3.1 and a photographic view is shown in Figure 3.2. The facility comprises mainly of



1. Bubbler
  2. Liquid level indicator
  3. Condensers
  4. Thermocouple leads
  5. Micrometer
  6. Vacuum gauge
  7. Test vessel
  8. Inspection window
  9. Heating surface
  10. Liquid sampling unit
  11. Air-liquid separator
  12. Oil seal
  13. Vapour sampling unit
  14. Electrical leads
- ▷ Valve  
 ⊥ Tee  
 ≡ Union  
 a. Coolant inlet  
 b. Coolant outlet  
 c. Vacuum breaker  
 Th. Thermometer

Fig 3-1 Schematic diagram of the experimental facility





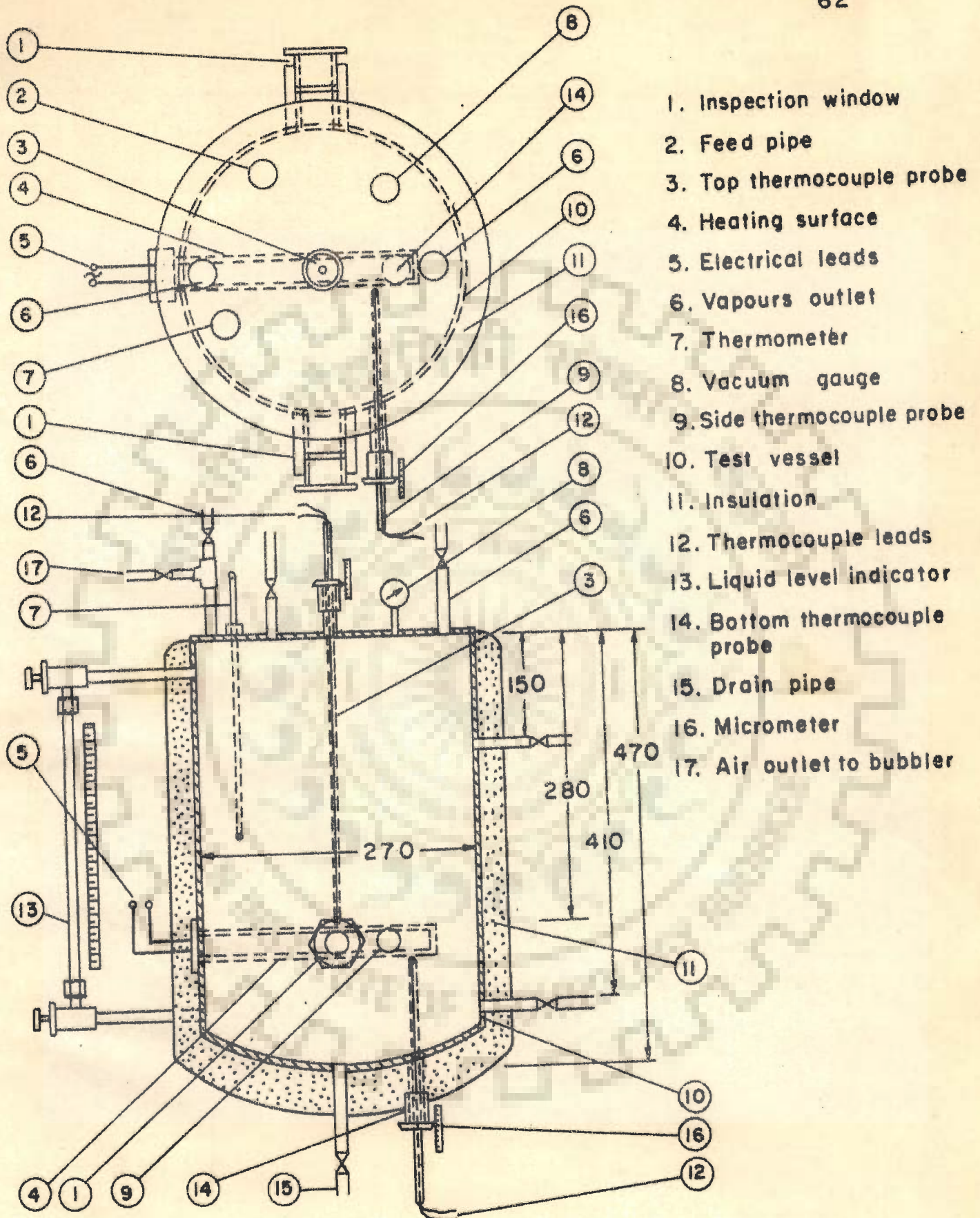
Fig. 3-2 Photographic view of the experimental facility

following components:

- Test vessel
- Heating surface
- Liquid thermocouple probes
- Vacuum and condensing system
- Air-liquid separator and sampling units

### 3.2.1 Test Vessel

The details of the test vessel are shown in Figure 3.3 and a photographic view in Figure 3.4. It was a cylindrical vessel made out of 304 ASIA stainless steel sheet having a welded flat top and dished bottom. The diameter of the vessel was 240 mm and height 470 mm. The vessel was filled upto a capacity of  $0.017 \text{ m}^3$ . Figure 3.3 shows the locations of the thermocouple probe (3), the thermometer (7) and the vacuum gauge (8) which were mounted on the vessel top (8). It also had provisions (2),(6) and (17), for charging the test fluid into the vessel, for carrying the vapours from the test vessel to the condensers, and for removing the dissolved air from the boiling liquid, respectively. A liquid level indicator (13) was attached to the left side of the vessel. The heating surface (4), over which boiling occurred, was installed horizontally within the vessel at a submergence depth of about 280 mm as photographed in Figure 3.4. The heating surface (4) was fitted to the



All dimensions in mm

Fig. 3-3 Details of test vessel

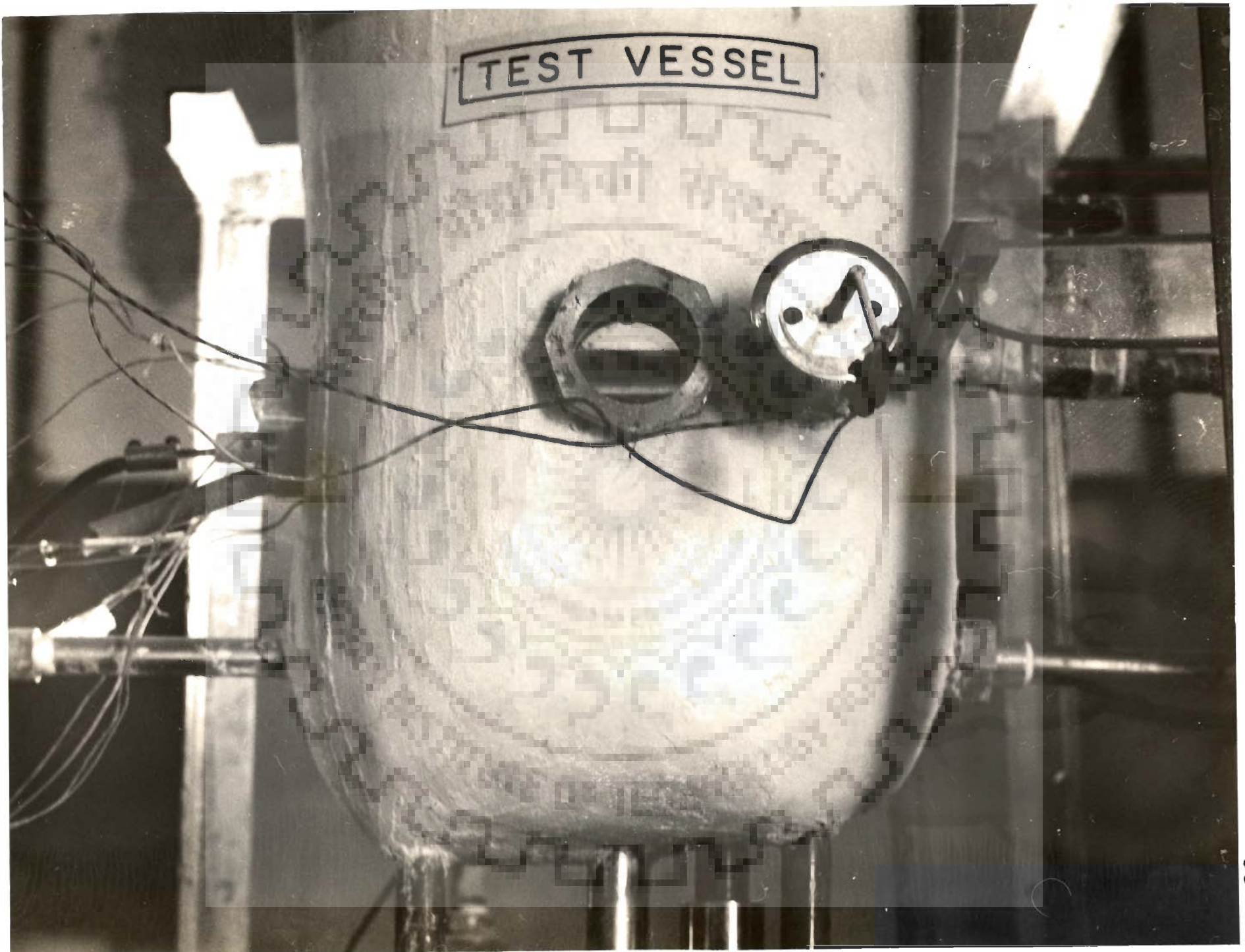
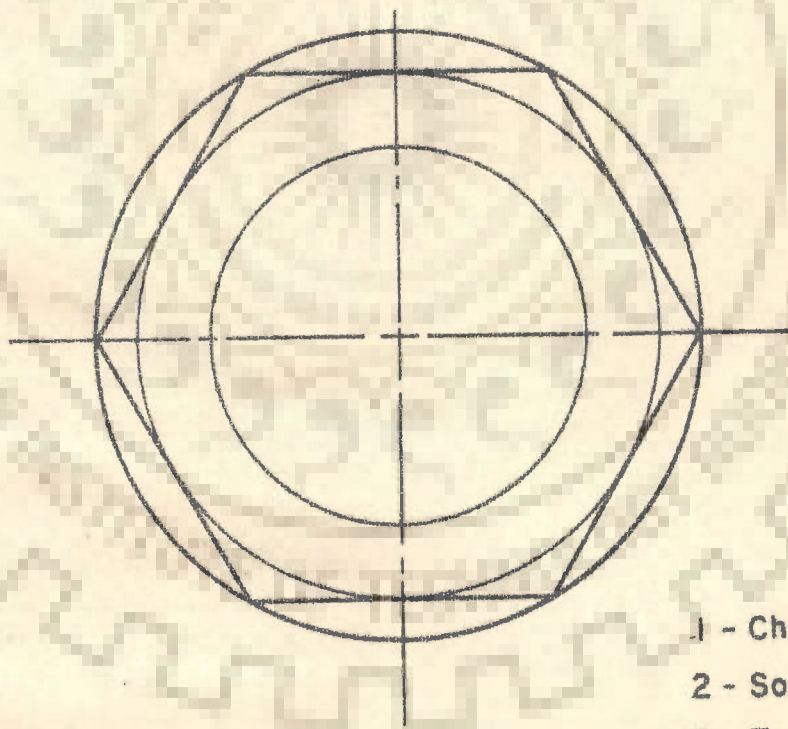
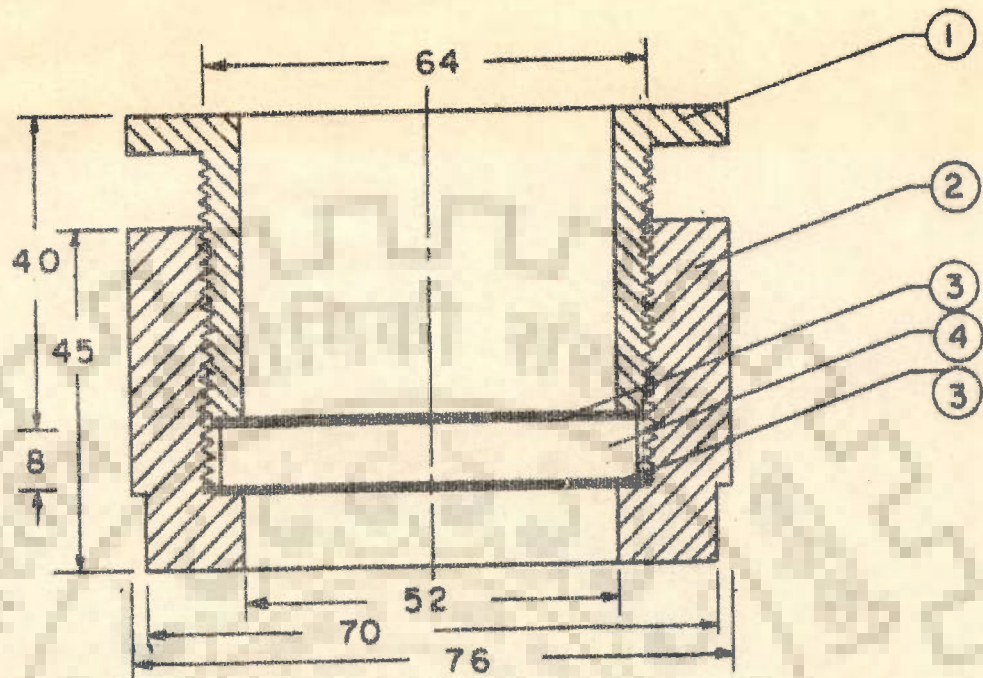


Fig. 3-4 Photographic view of the test vessel and the heating surface

test vessel (10) from the left of the vessel as shown in Figure 3.3. The details of the arrangement for holding it in horizontal position is shown in Figure 3.6. Two diametrically opposite inspection windows (1) were provided at the front and rear side of the vessel for viewing the bubble dynamics. The details of the inspection window assembly is shown in Figure 3.5. Liquid thermocouple probes at the side (9) and the bottom (14) positions were attached to the vessel as depicted in Figures 3.3 and 3.4. The details of the thermocouple probes are described in Section 3.2.3. To minimize the heat losses to surroundings the vessel body except the top flange was thoroughly insulated by means of glass wool and a mixture of 85% magnesia powder and plaster of paris(11). To drain the liquid from the test vessel a drain pipe(15) with a valve was provided at the bottom of the vessel. Suitable pipe lines and control valves were also provided for liquid sampling and return of vapour condensate to the vessel as shown in Figures 3.1 and 3.3.

### 3.2.2 Heating Surface

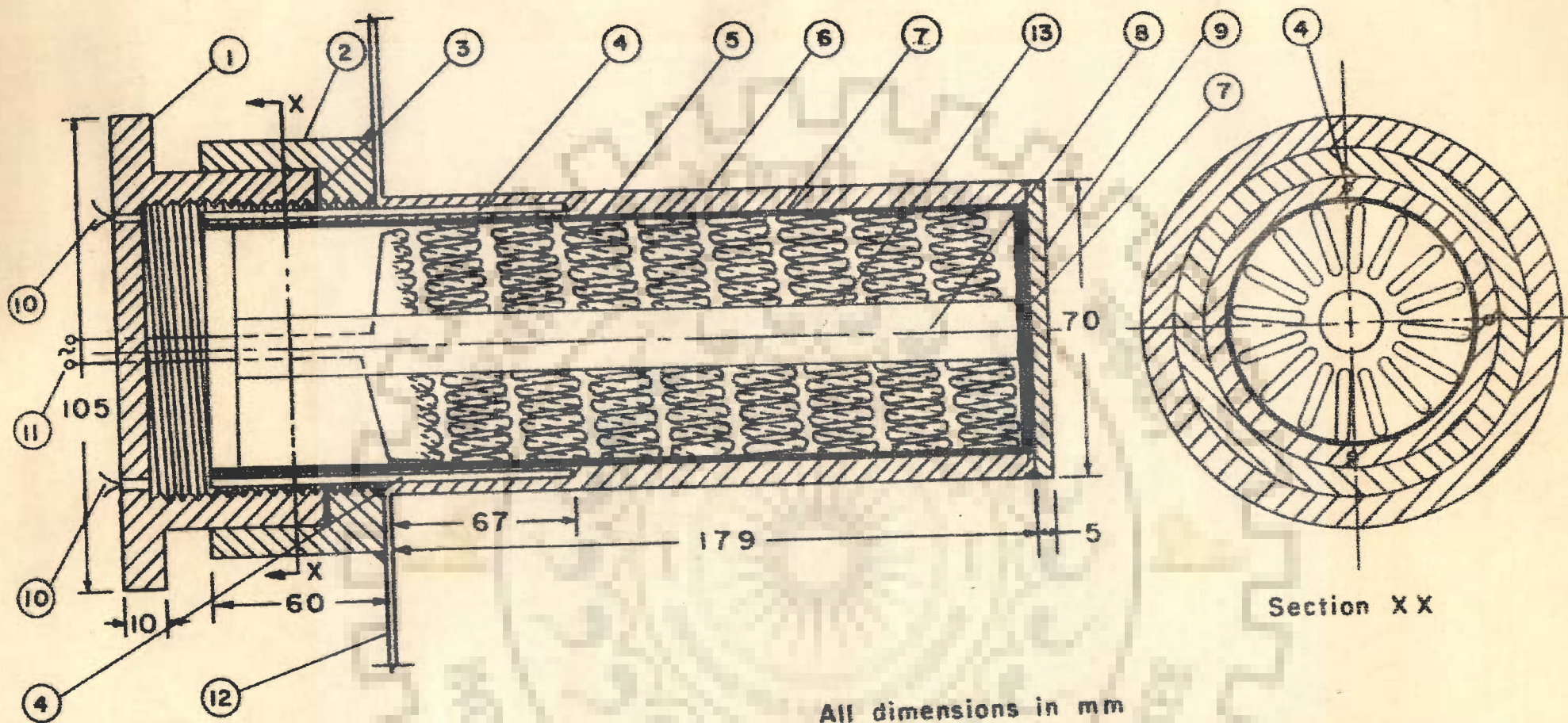
Figure 3.4 provides a photographic view of the heating surface submerged in the pool of boiling fluid. Figure 3.6 shows the details of the heating surface. It consists of a 410 AISI stainless steel cylinder (6) 70 mm outside diameter and 4 mm thick. The total



- 1 - Check nut
- 2 - Socket
- 3 - Teflon gasket
- 4 - Sight glass

All dimension in mm

Fig. 3.5 Inspection window assembly



All dimensions in mm

1. Check nut
2. Socket
3. Lead gasket
4. Thermocouple
5. Heating element
6. Heating surface
7. Mica sheet

8. Porcelain core
9. End plate
10. Thermocouple leads
11. Electrical leads
12. Test vessel wall
13. Asbestos rope

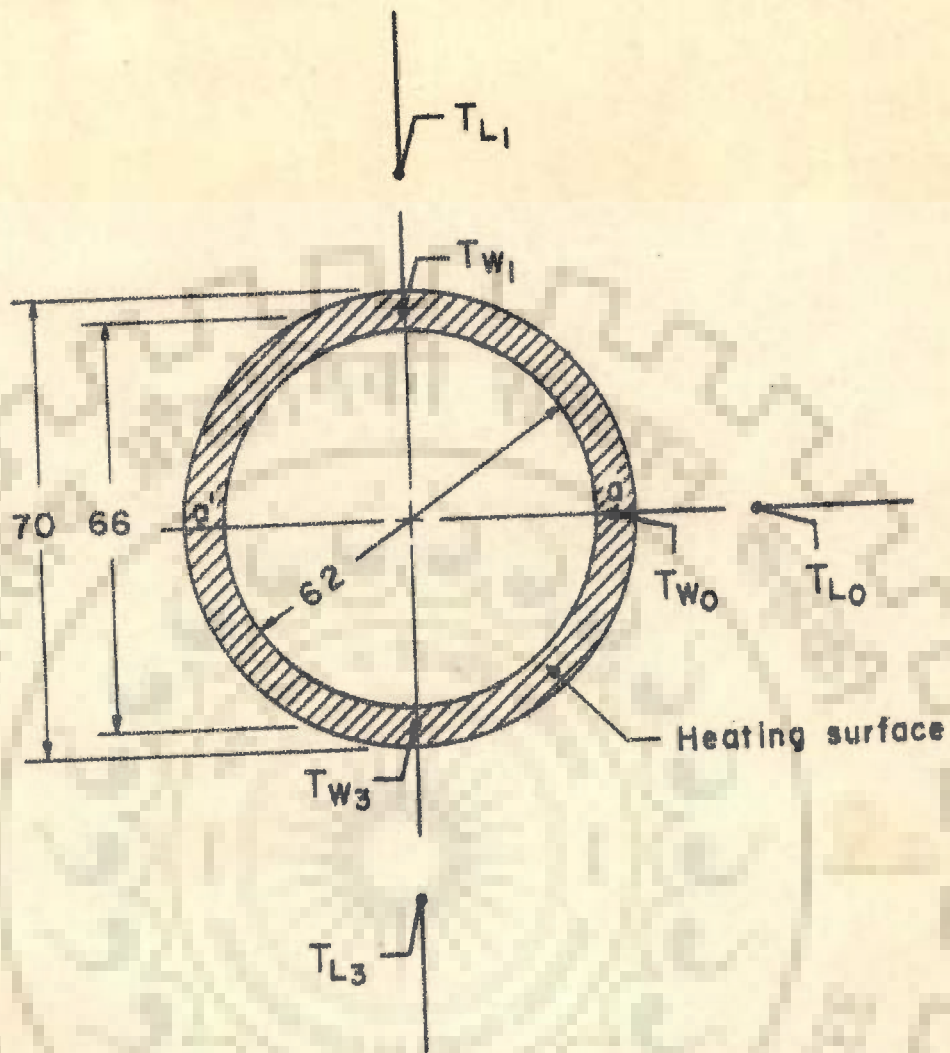
Fig. 3-6 Details of heating surface

length of the heating surface was 244 mm, out of which 60mm was threaded portion and 5 mm end plate (9) thickness. The outer surface of the heating surface was uniformly turned and polished by rubbing it against 0/0 emery paper. It was supported horizontally in the test vessel by means of a socket (2) welded at the left side of the vessel. A check nut (1) with lead gasket (3) was also provided to make the system leak proof.

Design considerations, as detailed in Section 3.1 dictate that three thermocouples were sufficient to know the variation of heat transfer coefficient circumferentially and to have average values of the surface temperatures. Figures 3.6 and 3.7 show the locations of these thermocouples at the side, at the top and at the bottom of the heating surface. The temperature at a' was not measured since it is equal to temperature at a, due to the symmetry of boiling conditions about the horizontal mid-plane a-a'. In Figure 3.7 the respective positions of liquid thermocouple probes are also depicted. Three axial holes of 127 mm depth were drilled in the wall of heating surface at the above mentioned positions to place the thermocouples. Calibrated fibre-glass insulated copper constantan thermocouple wires of 24 gauge were used.

The heating surface was heated by an electric heater. A cartridge heater was designed and fabricated which provided a heat flux upto a value of  $45,000 \text{ W/m}^2$ . Nickle-Chrome





All dimensions in mm

T - Thermocouple  
 W - Wall  
 L - Liquid  
 0, 1 and 3 represent the  
 side, top and bottom  
 positions respectively

Fig. 3.7 Thermocouples layout on heating surface and in boiling liquid

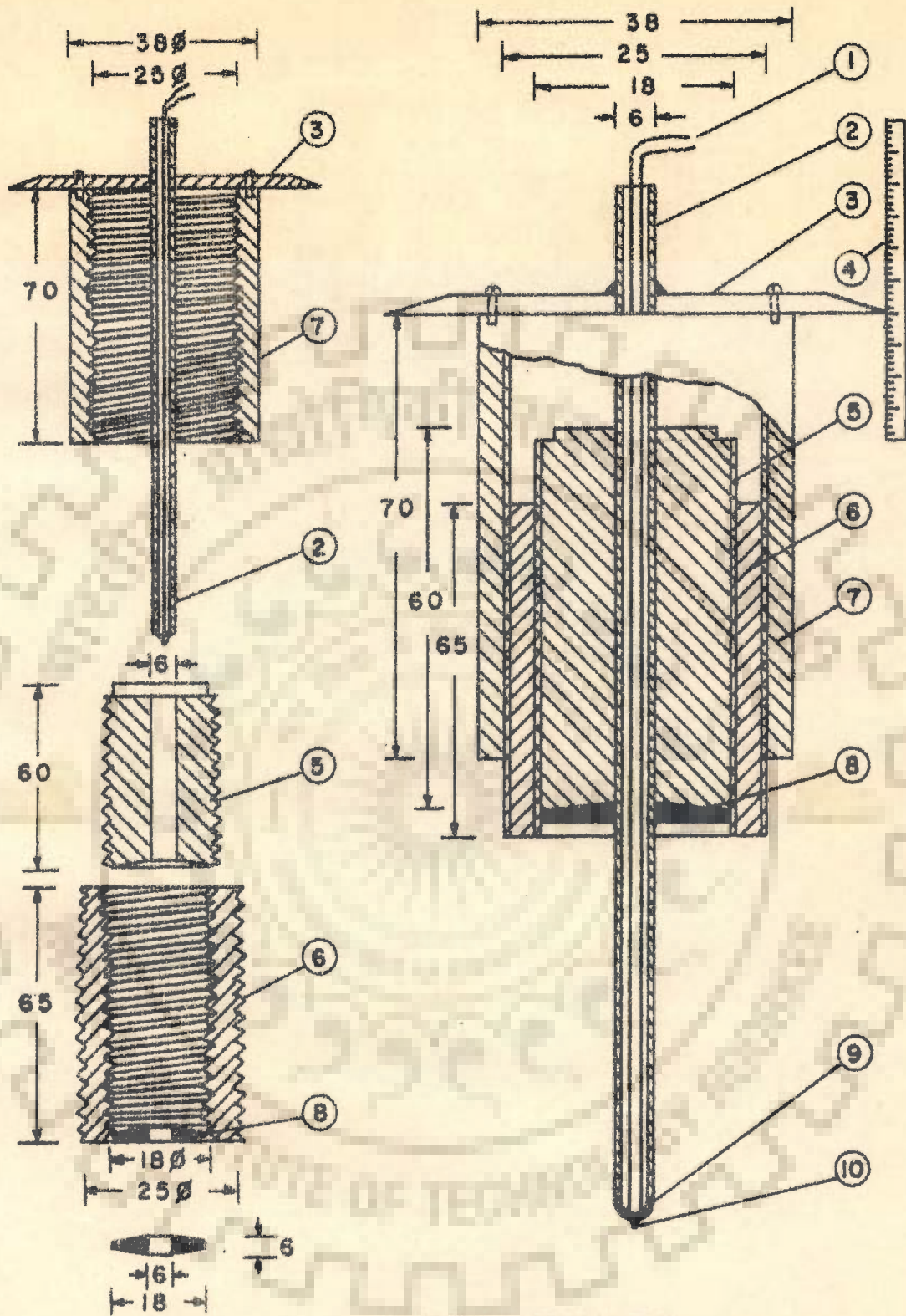
wire of 14 gauge having a maximum current carrying capacity of 24 amperes constituted the heating element (5). The coil (5) made of this element was wound on a porcelain core (8) of 16 mm diameter. A fine asbestos rope (13) was provided between the two successive turns of the heating element for insulating them. The entire heating coil (5) was then thoroughly wrapped in a thin mica sheet (7) which ensured a complete electric insulation between the element and the heating surface. This cartridge heater was then placed inside the heating surface.

### 3.2.3 Liquid Thermocouple Probe

Design considerations, as detailed in Section 3.1 necessitated the measurements of fluid temperatures by moving thermocouple probes.

The details of the main components of the probe and the assembled probe are shown in Figure 3.8. The various components were the nipple (6), the check nut (5), the thermocouple carrying tube (2), the movable socket (7) with a graduated circular disc (3) and the fixed scale (4). All these components were made of stainless steel.

The nipple (6) was 65.0 mm long having 25.0 mm outside diameter and 18.0 mm inside diameter. It had full threads on its outer and inner surfaces. The outer surface was fine threaded having a pitch of 1 mm. The diameter of the vessel-end of the nipple was reduced to 6 mm, equal to



All dimensions in mm

- |                               |                     |
|-------------------------------|---------------------|
| 1. Thermocouple leads         | 6. Nipple           |
| 2. Thermocouple carrying tube | 7. Movable socket   |
| 3. Circular scale disc        | 8. Teflon gasket    |
| 4. Vertical scale             | 9. Silver soldering |
| 5. Check nut                  | 10. Bead            |

Fig. 3-8 Details of liquid thermocouple probe

the outer diameter of the thermocouple carrying tube. In order to eliminate the leakage of the fluid through the vessel- end of the nipple, the check nut (5) with inside diameter of 6 mm and having threads on its outer surface matching with inner threads of the nipple (6) was fitted. The gasket (8) made of teflon was used to press against the thermocouple carrying tube (2) and thus making the system leak proof.

The thermocouple carrying tube was of 6 mm outside diameter. It had copper constantan thermocouple wires(1) of 24 gauge passing through it. The bead end (10) of the tube was silver soldered (9). The entire lengths of the thermocouple wires were sheathed with twin bored porcelain tube of 4 mm diameter having bore diameter of 0.8 mm. This ensured against any possibility of secondary junction of thermocouples inside the tube. The thermocouple wires were taken out of the other end of the tube. The thermocouple carrying tube was welded to the movable socket (7) and thus the tube traversed within the pool by means of the movable socket.

The movable socket was cylindrical in shape having fine threads of 1 mm pitch at its inner surface and having a graduated circular disc at its top. These threads matched with those on the outer surface of the nipple (6). Thus the movable socket (7) could move along the nipple and thereby

thermocouple tube (2) traversed in the pool of boiling liquid. The traversed distance of the thermocouple carrying tube was measured by means of graduated movable circular scale (3) and the fixed scale (4) as shown in photograph 3.4. The circular disk had 200 graduations on its periphery and thus a distance upto  $7.5 \times 10^{-3}$  mm could be read.

### 3.2.4 Vacuum and Condensing System

The vapours from the boiling fluids condensed externally and returned back to the pool of liquid. The condensation of the vapours was carried out in two countercurrent water-cooled condensers with the condensing vapour in the inner pipe and coolant in the annulus. These condensers(3) were located at the top of the vessel as shown in Figure 3.1. They were pitched towards the air-liquid separator and were connected in parallel as shown in Figures 3.1 and 3.9. The condensers were designed to cause total condensation of the vapours. The separated condensate from the separator (11) flowed through a pipe and returned to the pool of boiling fluid.

Vacuum was created by means of a vacuum pump of a "HV" series Hindustan Rotary two-stage oil immersed type with suction capacity of  $125.025 \times 10^{-5} \text{ m}^3/\text{s}$ . The pump was driven by a 0.37 kW motor having 1450 rpm. One of the essential features of the pump was an air Ballast which enabled the pump to attain high vacuum even when a lot of moisture and organic vapours were sucked in by the

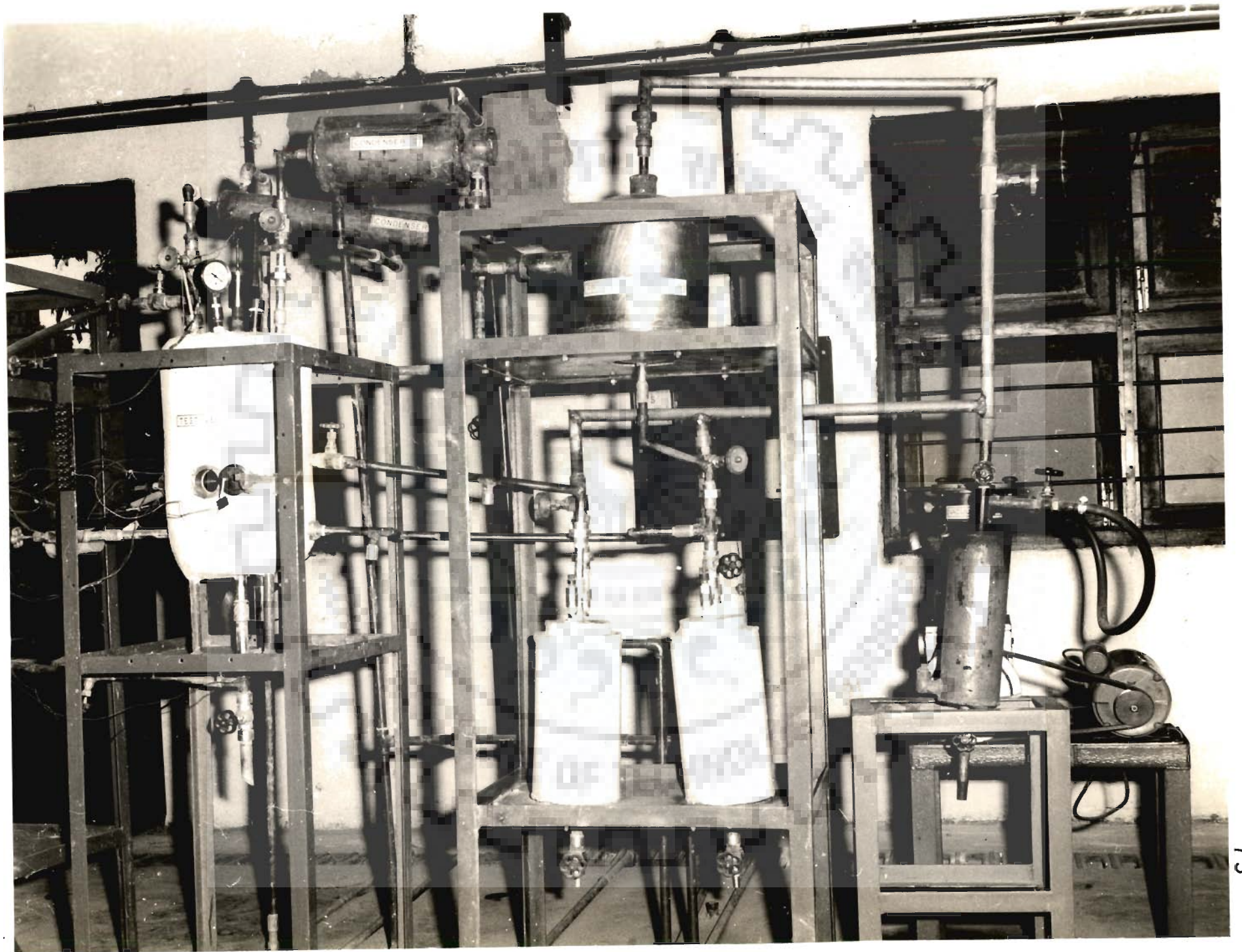


Fig. 3.9 Photographic view of the vacuum, condensing system and sampling units

pump. Drops of water particles which were released under high compression ratios, of the order of 1:700 and collected underneath the main valves were completely eliminated by the introduction of fresh atmospheric air through the air Ballast vent. The pump was protected from the organic vapours and moisture by means of an absorbent placing in suction inlet. An oil seal (12) was also provided for this purpose. To check the back flow of oil into the apparatus, valves (I) and (II) were provided at suitable locations. Pressure regulation was done with a fine needle valve (III).

### 3.2.5 Air-Liquid Separator and Sampling Units

An air-liquid separator (11) was placed between the condensers (3) and the vacuum unit as shown in Figures 3.1 and 3.9 . It was a cylindrical vessel made of stainless steel having a tangential entry for the air-liquid mixture from the condensers. The separated air passed to the vacuum pump through the pipe at the top of the separator while the condensate to the pool of boiling fluid.

Provision was made in this experimental facility for drawing out the samples of boiling fluid and the equilibrium vapours. The sampling vessels (10)& (13) had jacketted wall for the coolant to flow through the jacket in order to cool the hot samples of the fluid. A vent cock (C) provides the facility to break the vacuum in these vessels

in order to take the samples from these units. Liquid sampling unit was connected to the pool of the boiling fluid with a precise control valve (vii) and the vapour sampling unit to the separator with a control valve (v). By closing the valves (iv), (v), (vi) and (vii) these units could be isolated from the rest of the apparatus. The liquid sample could be drawn by opening valve (vii) and the condensate sample by valve (v). Cool samples could be drawn out from the bottom of the vessels with the help of valves (viii) and (ix).

### 3.3 INSTRUMENTATION

The photographic view of the instrumentation used is shown in Figure 3.10. The heat to the heating surface was supplied by means of single-phase 50 c/s alternating current. Electric power input to the heating element was measured by means of calibrated precision grade ammeter and voltmeter of accuracy less than 1 per cent. The range of ammeter was from 0 to 5 amperes and that of voltmeter from 0 to 300 volts. In the present investigation the current exceeded 5 amperes. Therefore, current transformer was employed. The power supply to the element was modulated by an autotransformer. The arrangement of the electric circuit is shown in Figure 3.11. The readings of voltmeter and ammeter were noted in order to calculate the power input to the element. The power divided by the heat transfer area of the heating surface represented the heat flux.



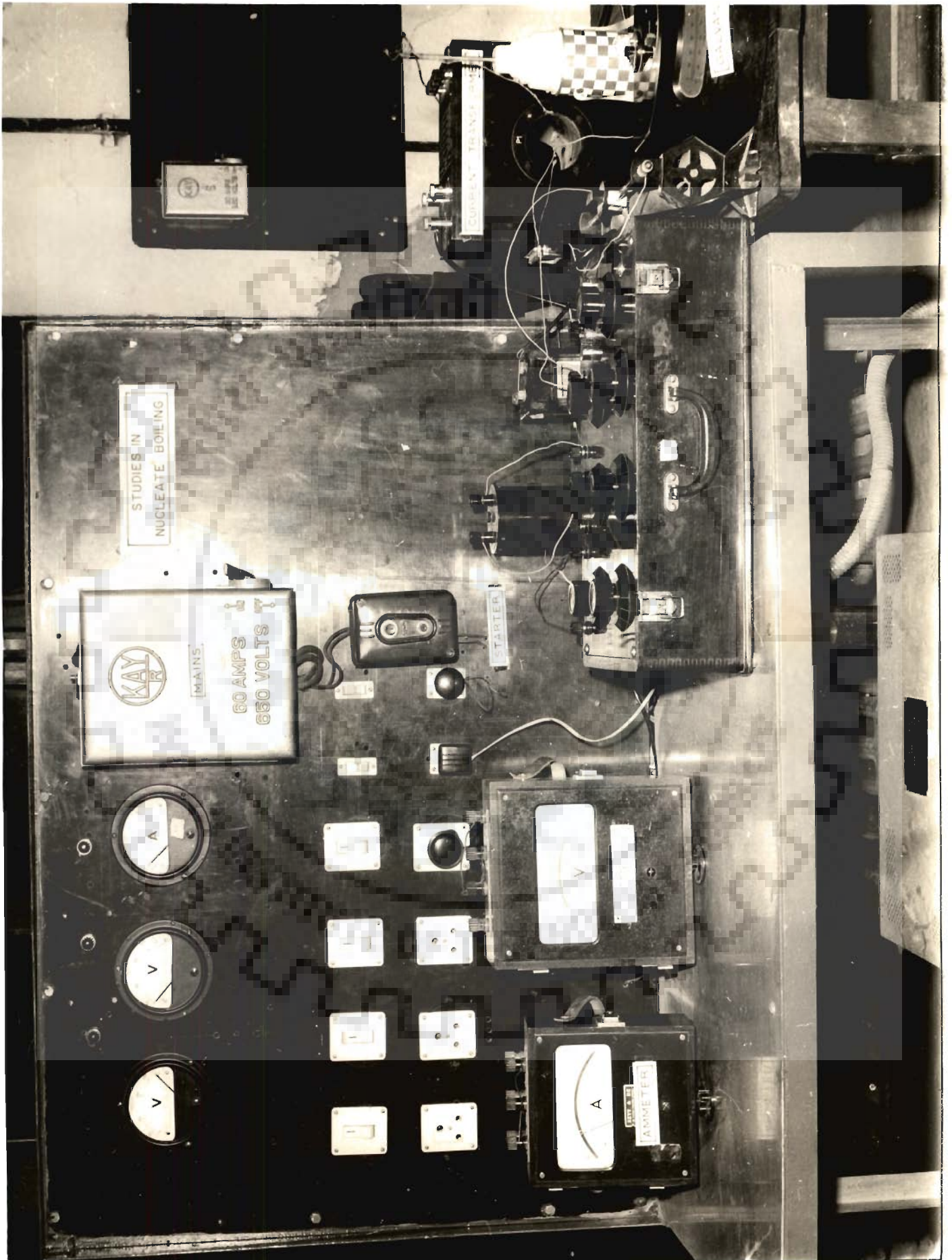


Fig. 3-10 Photographic view of the instrumentation

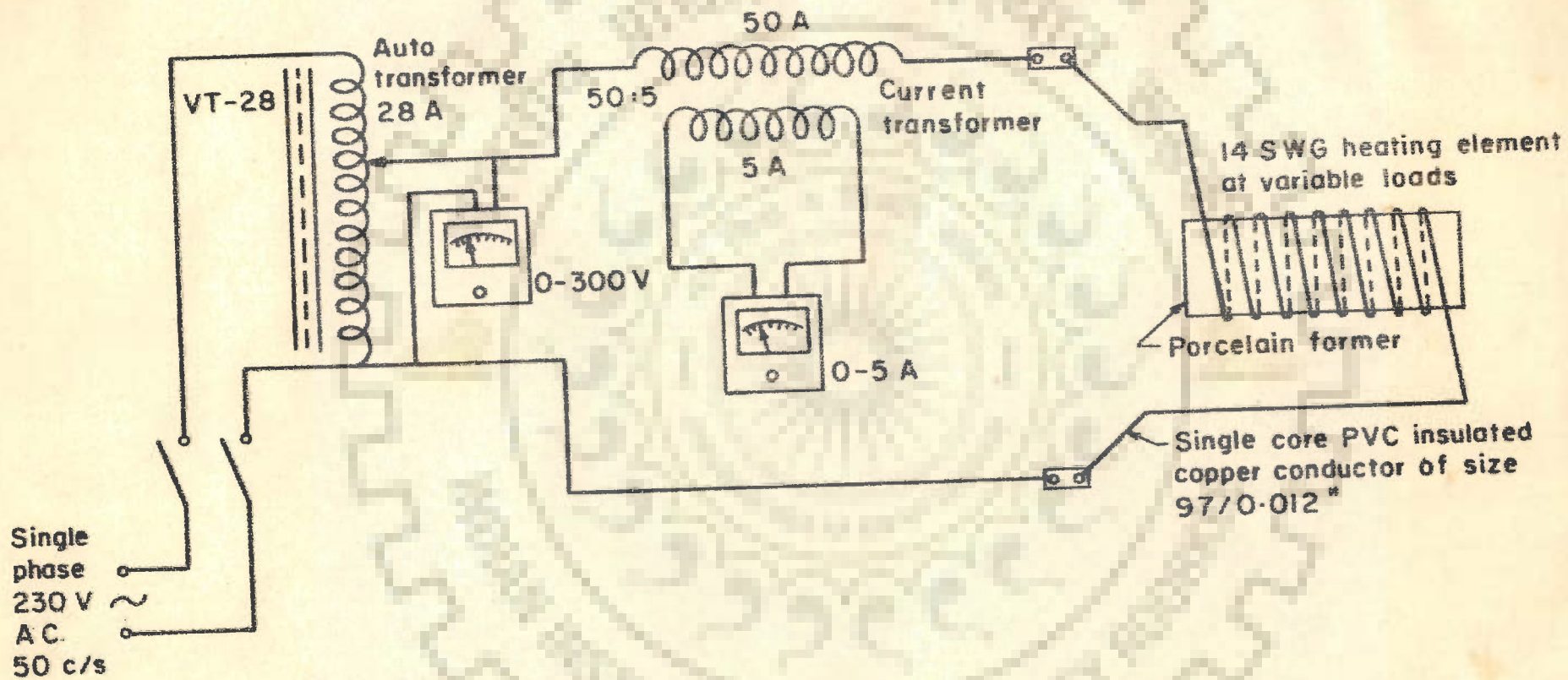


Fig. 3-11 Electric circuit for the heating element

The electromotive force of thermocouples was measured by a vernier potentiometer with a sensitive spot galvanometer. The potentiometer could read e.m.f. upto 0.001 mV with an accuracy of 0.01 per cent. A multipoint selector switch supplied by M/S Toshniwal was used to connect the thermocouples to the potentiometer. A distilled water-ice bath provided a reference temperature.

To accomplish the measurements of vacuum in the system a calibrated precision grade vacuum gauge was mounted on the top of the vessel. This pressure determines the saturation temperature of the system.

## CHAPTER 4

### EXPERIMENTAL PROCEDURE

#### 4.1 TESTING OF THE EXPERIMENTAL FACILITY

A series of tests were conducted to ensure the successful operation of the various components of the experimental facility after they were fabricated and assembled. The details of these tests are:

##### 4.1.1 Vacuum

As the experiments were conducted under vacuum it was necessary to establish the vacuum integrity of each of the components of the apparatus. To accomplish this, first, the individual components were tested against pressure integrity. All the exit valves were closed and compressed air was introduced to the individual components. The compressed air was charged upto a pressure of  $689.5 \text{ kN/m}^2$ . All seals, connections and fittings were then checked for leaks using a soapy water solution. The components were deemed pressure tight, if, when isolated from air supply, they would maintain the  $689.5 \text{ kN/m}^2$  pressure for atleast 24 hours. Finally entire experimental facility, when assembled, was tested in the similar manner for pressure integrity. After conducting the pressure tests the assembly was evacuated to  $5.332 \text{ kN/m}^2$  and this was also

maintained for a period of 24 hours. No change in vacuum gauge reading ensured the total assurance against any leakage.

Obviously, along with , check against any leakage, the condensers were ensured against any fluid interchange between annulus and condensing side. The sampling units were also ensured against any leakage with the jacket fluid.

#### 4.1.2 Calibration of Measuring Devices

Before the thermocouples were installed, each one was checked for continuity and calibrated by means of standard mercury-in-glass thermometer of 0.1°C least count. The maximum deviation of 0.20 per cent between the readings of thermocouples and the thermometer was observed. A similar calibration was done when they were mounted on their respective positions.

The voltmeter and ammeter were calibrated against Substandard ammeter and voltmeter. The maximum deviation was less than 1 per cent.

## 4.2 DISCUSSION OF OPERATION

### 4.2.1 Initial Difficulties

Prior to commissioning of the experimental facility certain difficulties were confronted with. The major problem encountered is discussed here.

Problem, which was immediately experienced was the unsatisfactory performance of condensers. At high values of heat flux (more than  $25,000 \text{ W/m}^2$ ) and at low values of pressures (less than  $67 \text{ kN/m}^2$ ) the condensers started showing unsatisfactory performance. To solve this problem the heat transfer surface for condensation was increased by installing fins over outside surface of the inner pipe and by increasing the diameter of inner pipe within physical limitations. This could mitigate the problem to quite an extent and it was possible to obtain the lowest limit of pressure as  $11.33 \text{ kN/m}^2$  at a heat flux value of nearly  $42,000 \text{ W/m}^2$  for the case of distilled water.

#### 4.2.2 Operating Procedure

Before conducting the experiments for the boiling of a fluid the following steps were taken:

1. The experimental facility was connected to an air-compressor. The compressed air was supplied to the facility, to blow - off all the hold-up of fluid in the test vessel and connecting pipe lines. Thus, before charging the fresh fluid to the test facility it was completely free of the traces of previous fluid.
2. The test vessel was then rinsed with the fluid to be charged for the experimentation.

3. The heating surface was cleaned with distilled water, acetone and the fluid in which it was to be immersed prior to each experiment.
4. The exit valve (x) was closed (Refer Figure 3.1)
5. The liquid sampling valve (vii) was also closed.
6. The feed valve was opened and the test fluid was charged into the test vessel.
7. All the connections and fittings were checked against any leakage of the fluids .
8. Valves (xi) and (xii) were closed so that dissolved air did not circulate in the system.
9. Valve (xiii) was opened to remove the dissolved air.

After these initial operations, prior to filling of each test fluid to the test vessel, the pool of the liquid was boiled-off for six to seven hours to remove the dissolved air completely. When the bubbling ceased in bubbler(1), valve (xiii) was closed. The coolant circuits of condensers were started and valves (xi) and (xii) for vapour were opened.

Before conducting the series of experimental runs it was necessary to age and stabilize the heating surface. This was done as follows: the heating surface was submerged in the pool of fluid for a period of 24 hours followed by a boiling of 8 hours. This process was repeated till the heating surface was stabilized.

There was a consideration about the location of the liquid thermocouples. These thermocouples were to be located outside the superheated layer around the heating surface. The extent of superheated layer was found by noting the thermocouple readings at various positions away from the heating surface. The respective probes were kept at a point at which no change in fluid temperature was observed.

To begin an experiment, the equipment was adjusted to provide the chosen experimental conditions. Since the variation of heat transfer coefficient with heat flux at a fixed pressure was the parametric variation of interest, the vacuum of the system was varied systematically. Thus a particular value of the vacuum was selected and this vacuum in the test vessel was obtained by switching -on vacuum pump and manipulating the control valve (III). After obtaining the desired value of vacuum in the system the vacuum pump was switched-off and the control valve (III) was closed. The heat flux was then adjusted by modulating the autotransformer. After the experimental conditions were adjusted the experiment was run for one to two hours until the steady state conditions reached. The steady state conditions were assumed when no variation in surface temperatures and liquid temperatures was observed with time. At steady state conditions the following informations were noted: The e.m.f. of all the surface and fluid thermocouples, the readings of voltmeter and ammeter, the



readings of vacuum gauge and the barometric pressure with the help of a barometer.

The heat flux was now varied to another value and the experimental run was allowed to reach steady state conditions. All the informations, as mentioned above, were noted at steady state. Similar runs were conducted for six to seven values of heat flux for one vacuum level. Six to seven values of vacuum were employed for each fluid. Four fluids : distilled water, isopropanol, ethanol and methanol were employed for the experimentation. The range of experimental parameters is given in Table 4.1.

Table 4.1 Range of Experimental Parameters

Heating surface: 410 AISI Stainless Steel

Fluid	System Parameters	
	Heat Flux, $W/m^2$	Pressure, $kN/m^2$
1. Distilled water	6870 - 41,730	98.44 - 11.33
2. Isopropanol	6870 - 37,709	97.97 - 15.33
3. Ethanol	3307 - 33,893	98.18 - 19.33
4. Methanol	6870 - 33,893	98.64 - 27.99

#### 4.2.3 Reproducibility of the Surface Characteristics

Prior to the first experiment with each new experimental fluid an experiment was conducted with distilled water at atmospheric pressure to check the reproducibility

of the heating surface characteristics. This experiment was always performed with maximum heat flux available in this investigation as at this heat flux all possible active sites may get activated. At the end of the experiment these results were compared with the previously conducted experiment. Within the tolerance of experimental error (like change in barometric pressure etc.), they were always equivalent.

#### 4.2.4 Consistency of Experimental Data

The data produced with this experimental facility were consistent within the allowable experimental error. The data were not erratic in nature and yielded the expected trends. This trend was corroborated for those experiments also when certain experimental runs were repeated. However, experience with the facility revealed that no set of experimental conditions could be repeated lock, stock and barrel. Variations in voltage fluctuations and barometric pressure were responsible for this circumstance. Fortunately, the data were by and large consistent.

#### 4.3 OPERATIONAL CONSTRAINTS

Certain physical limitations restricted upon the range of operational parameters. The range of different parameters obtained during this investigation have been listed in Table 4.1.

The parameters involved in the present investigation were heat flux, system pressure and boiling fluids. This investigation was carried out at low values of heat flux. This parameter was constrained because of the limited space available for placing the electric heater into the heating surface and due to the maximum current carrying capacity of the heating element.

The condensing unit of the facility limited the maximum attainable value of the vacuum. At higher values of vacuum, ebullition of the boiling fluid occurred. This ebullition caused an increase in the quantity of vapours which were condensed in the condensers. Physical limitations of the condensers were responsible for the insufficient condensation for this out-burst. And this involved unfavourably in reaching a steady state. Although it was possible to attain quite lower value of the pressure as of the order of  $11 \text{ kN} / \text{m}^2$  in case of boiling distilled water but in case of other liquids it was restricted, relatively, to a higher value due to above mentioned difficulties.

## CHAPTER 5

### ANALYTICAL INVESTIGATIONS

#### 5.1 HEAT TRANSFER COEFFICIENT IN POOL BOILING

Literature survey of Chapter 2 shows that there are two major classifications of models of heat transfer in nucleate pool boiling. They are based either on experimental evidences or theoretical considerations or both.

The models based on experimental data consider that the boiling heat transfer is analogous to the phenomenon in single-phase convective heat transfer. Correlations of this class are written in the form of dimensionless groups incorporating wall heat flux, wall superheat, system pressure and pertinent physico-thermal properties of boiling fluids. However, these correlations did not make any precise reference to the heating surface characteristics except to introduce empirical constant which accounts for the effects of specific surface-liquid combination. Some correlations have been recommended in dimensional form as well.

An important break-through in the studies of heat transfer in nucleate pool boiling was made by Jakob and Linke [3], [4], [49]. They considered the effects of

heating surface characteristics on heat transfer coefficient assuming a linear relationship between the heat flux and number of active sites per unit area of the heating surface and product  $fD_b$  to be a constant. Based on these assumptions an equation for heat transfer coefficient was obtained. Subsequently, in 1952 Rohsenow [14] derived a semi-theoretical equation for predicting heat fluxes during nucleate pool boiling. His analysis was based on the tacit assumptions of Jakob [3], [49]. The objection to these analyses is that they have been derived under the assumptions that heat flux changes linearly with the number of active sites and the product of bubble emission frequency and bubble departure diameter is a constant. Recent studies have revealed that bubble departure diameter depends on pressure [44], [88], [89] [91], [93], [94], [95] and frequency on pressure and heat flux [19], [32], [98] as well. Therefore, analyses due to Jakob and Linke [3], [4], [49] and Rohsenow [14] are not of general applicability for the wide ranges of pressure and heat flux.

The Jakob linear relationship between heat flux and number of active sites has been followed by the Nishikawa relationships [26], [51]. Nishikawa et al [32] have shown that the relationship between heat flux and number of active-sites per unit area is governed by a power law and not by a linear relationship as proposed by

Jakob originally. Their results were based on a maximum population count of eight active sites per square inch. The subsequent studies by Kurihara and Myers [52] and Gaertner and Westwater [46] have verified the Nishikawa relationships for twenty-eight active sites and 1,130 active sites per square inch respectively but with different exponents.

More recently Wiebe and Judd [54] have attempted the measurement of superheated layer thickness in saturated and subcooled nucleate boiling. They established a power law relationship between heat flux and product  $nf$ .

In this Chapter a new method is developed for predicting heat transfer coefficients in nucleate pool boiling at atmospheric and subatmospheric pressures from theoretical considerations.

## 5.2 ANALYSIS

Nucleate boiling is characterised by the presence of unique active sites on heating surfaces. The vapour bubbles sustain on these sites and these active sites are effective in reducing the average wall superheat required for boiling and, hence, high boiling coefficients are realised. It is interesting to speculate that the average wall superheat will depend on the number of active sites, the frequency of bubble emission and the bubble departure size. The effects of these quantities are

reflected through vigorous agitation of the superheated layer adjacent to the heating surface. Recent studies by Cole and Shulman [95], Nishikawa [89] and other investigators, as mentioned previously, emphasize that bubble departure size depends on pressure of the boiling fluid. Therefore, it is apparent that the degree of agitation of superheated layer depends on number of active sites and bubble emission frequency only for a given system pressure.

From the above it can be concluded that boiling heat transfer coefficient can be considered a function of number of active sites  $n$  and bubble emission frequency  $f$ .

In the following sections relationships of  $n$  and  $f$  with wall heat flux, wall superheat, system pressure and pertinent physico-thermal properties of boiling fluids are established. Following these relationships expressions are derived which provide predictions of boiling heat transfer coefficients in terms of known quantities and constants.

### 5.2.1 Number of Active Sites

Brown [53] investigated that number of active sites per unit area  $n$  with radii larger than  $r_c$  could be correlated by the following power law :

$$n = c_0 \left( \frac{r}{r_c} \right)^m \quad (5.1)$$

where  $r_r$  is a radius for which  $n$  would be one per unit area, and  $c_0$  is a dimensional constant having dimension of (unit area)<sup>-1</sup>.

According to the Laplace equation, the minimum radius of bubble is given by :

$$r_c = \frac{2 \sigma}{\Delta P} \quad (a)$$

The difference  $\Delta P$  can be expressed in terms of wall superheat as follows:

$$\begin{aligned} \Delta P &= \frac{dP}{dT} \Delta T_w + \frac{d^2P}{dT^2} \cdot \frac{\Delta T_w^2}{2} + \dots \\ &\approx \frac{dP}{dT} \Delta T_w \quad (b) \end{aligned}$$

Using the Clausius - Clapeyron relation and ideal gas law the following equation can be shown:

$$\frac{dP}{dT} = \frac{\lambda \rho_v}{T_s} \quad (c)$$

From Eqs. (a), (b) and (c) the value of  $r_c$  is obtained in the following form:

$$r_c = \frac{2 \sigma T_s}{\lambda \rho_v \Delta T_w} \quad (5.2)$$

When the value of  $r_c$  from Eq.(5.2) is substituted in Eq.(5.1), the number of active sites as a function of wall superheat and fluid properties is obtained:



$$n = c_0 r_r^m \left[ \frac{\lambda \rho_v}{2T_s \sigma} \right]^m \Delta T_w^m \quad (5.3)$$

Mikic and Rohsenow [43] have shown that the value of  $m$  can be taken to be 2.5 for water implying that  $q \propto \Delta T^{3.5}$  and 3.0 for organic fluids.

### 5.2.2 Wall Superheat

Alad'ev [55] developed the following expression which relates the wall superheat to wall heat flux and pertinent fluid properties during pool boiling of water for pressure range of 0.09 to 200 atmospheres.

$$\frac{\Delta T_w}{T_s} = 4.7 \times 10^{-3} \left[ \frac{10^{-6} q \lambda}{k_{\ell} T_s g} \right]^{0.3} \left[ \frac{\lambda}{C_{\ell} T_s} \right]^{1.2} \quad (5.4)$$

For the boiling of fluids other than water the constant of Eq.(5.4) should be replaced by some other constant  $c_2$ . The value of constant  $c_2$  of Eq.(5.4a) is determined in Chapter 6 by least squares estimates using the experimental data in Eq. (5.4a) and is given in Table 6.1.

In order to show the extent of validity of Eq.(5.4) for the present investigation, a comparison between experimental and predicted values of  $\Delta T_w$  is made in Chapter 6.

$$\frac{\Delta T_w}{T_s} = c_2 \left[ \frac{10^{-6} q \lambda}{k_{\ell} T_s g} \right]^{0.3} \left[ \frac{\lambda}{C_{\ell} T_s} \right]^{1.2} \quad (5.4a)$$

From Eqs.(5.3) and (5.4a) the following equation for number of active sites results:

$$n = c_0 r_r^m c_2^m \left( \frac{\lambda \rho_v}{2 T_s \sigma} \right)^m \left[ \left( \frac{10^{-6} q \lambda}{k_{\ell} T_s g} \right)^{0.3} \left( \frac{\lambda}{C_{\ell} T_s} \right)^{1.2} T_s \right]^m \quad (5.5)$$

or

$$n = \frac{10^{-(1.8)m}}{2^m} c_0 c_2^m r_r^m \left[ \left( \frac{\lambda^{2.5} \rho_v}{T_s^{1.5} \sigma} \right) \left( \frac{q}{k_{\ell} g} \right)^{0.3} \left( \frac{1}{C_{\ell}} \right)^{1.2} T_s \right]^m \quad (5.6)$$

### 5.2.3 Bubble Emission Frequency

In this section a method has been attempted which gives frequency of bubble emission as a function of Jakob number, heat flux and physical properties of boiling fluid for atmospheric and subatmospheric pressures.

The frequency of bubble emission at a single site may be written as:

$$f = \frac{1}{\theta_d + \theta_w} \quad (5.7)$$

Cole and Shulman [ 66], following the analysis for bubble growth in a uniformly superheated liquid of infinite

extent have derived the following expression for bubble growth rate at moderate Jakob numbers ( $J_a \leq 100$ )

$$D(\theta) = J_a \sqrt{\pi \alpha \ell} \theta^{1/2} \quad (5.8)$$

The expression for bubble departure diameter for boiling under atmospheric and subatmospheric pressures has been suggested by Cole and Shulman [95] as follows:

$$D_b = \left[ \frac{133.3}{P} \right] \left[ \frac{\sigma}{(\rho_l - \rho_v)g} \right]^{1/2} \quad (5.9)$$

Where  $P$  is in  $\text{kN/m}^2$

From Eqs. (5.8) and (5.9),  $\theta_d$  is calculated as follows:

$$\theta_d = \left\{ \frac{\left[ \frac{133.3}{P} \right]^2 \left[ \frac{\sigma}{(\rho_l - \rho_v)g} \right]}{\pi \alpha \ell J_a^2} \right\} \quad (5.10)$$

Han and Griffith [106] have related the waiting period  $\theta_w$  with transient thermal layer thickness,  $\delta$  in the following form:

$$\delta(\theta) = \sqrt{\pi \alpha \ell} \theta^{1/2} \quad (5.11)$$

where  $\delta$  is given by the expression [124] :

$$\delta = 1.65 \frac{k \ell \Delta T_w}{q} \quad (5.12)$$

From Eqs. (5.11) and (5.12) the value of  $\theta_w$  is obtained in the following form:

$$\theta_w = (1.65)^2 \left( \frac{k_{\ell} \Delta T_w}{q} \right)^2 / \pi \alpha_{\ell}$$

$$\text{or } \theta_w = \frac{0.867}{\alpha_{\ell}} \left[ \frac{k_{\ell} \Delta T_w}{q} \right]^2 \quad (5.13)$$

Using the values of  $\theta_d$  and  $\theta_w$  from Eq (5.10) and Eq (5.13), respectively into Eq (5.7), an expression for frequency  $f$  is obtained as follows:

$$f = \left[ \frac{1}{\frac{(133.3/P)^2 [(\sigma/(\rho_{\ell} - \rho_v)g)]}{\pi \alpha_{\ell} J_a^2} + \frac{0.867}{\alpha_{\ell}} \left[ \frac{k_{\ell} \Delta T_w}{q} \right]^2} \right] \quad (5.14)$$

Substituting the value of  $\Delta T_w$  from Eq. (5.4a) in Eq.(5.14) the following is obtained:

$$f = \left[ \frac{1}{\frac{[133.3/P]^2 [\sigma/(\rho_{\ell} - \rho_v)g]}{\pi \alpha_{\ell} J_a^2} + \frac{0.867}{\alpha_{\ell}} \left[ \frac{k_{\ell}}{q} \left\{ c_2 T_s \left( \frac{10^{-6} q \lambda}{k_{\ell} T_s g} \right)^{0.3} \left( \frac{\lambda}{c_{\ell} T_s} \right)^{1.2} \right\} \right]^2} \right] \quad (5.15)$$

For high values of Jakob number ( $J_a > 100$ ) Cole and Shulman [66] have recommended the following empirical expression for bubble growth rate:

$$D(\theta) = 5 J_a^{3/4} \sqrt{\alpha \ell} \theta^{1/2} \quad (5.16)$$

From Eqs. (5.9) and (5.16) the value of  $\theta_d$  is obtained as follows:

$$\theta_d = \frac{[133.3/P]^2 [\sigma / (\rho \ell^{-\rho_v}) g]}{25 \alpha \ell J_a^{3/2}} \quad (5.17)$$

Insertion of  $\theta_w$  and  $\theta_d$  from Eq. (5.13) and Eq. (5.17) in Eq. (5.7) gives an expression for  $f$  as follows:

$$f = \left[ \frac{1}{\frac{[133.3/P]^2 [\sigma / (\rho \ell^{-\rho_v}) g]}{25 \alpha \ell J_a^{3/2}} + \frac{0.867}{\alpha \ell} \left[ \frac{k \ell \Delta T_w}{q} \right]^2} \right] \quad (5.18)$$

Now inserting the value of  $\Delta T_w$  from Eq. (5.4a) into Eq. (5.18) the following equation for bubble emission frequency results:

$$f = \left[ \frac{1}{\frac{[133.3/P]^2 [\sigma / (\rho \ell^{-\rho_v}) g]}{25 \alpha \ell J_a^{3/2}} + \frac{0.867}{\alpha \ell} \left[ \frac{k \ell}{q} \left\{ c_2 T_s \left( \frac{10^{-6} q \lambda^{0.3}}{k \ell T_s g} \right) \left( \frac{\lambda^{1.2}}{c \ell T_s} \right) \right\} \right]^2} \right] \quad (5.19)$$

Eq. (5.15) and Eq. (5.19) represent the expressions for  $f$  for Jakob number less and greater than 100,

respectively. The value of  $c_2$  is taken from Table 6.1. These expressions appear to depend upon wall heat flux also. It is interesting to mention that investigations [19], [32], [98] have also concluded that heat flux influences the values of bubble emission frequency.

Comparison of theoretical predictions from Eqs. (5.15) and (5.19) with experimental data is shown in Chapter 6 to determine the extent of validity of the proposed equations.

#### 5.2.4 Heat Transfer Coefficient

It has been shown by Wiebe and Judd [54] that it is possible to evaluate heat transfer coefficient in boiling liquids from the knowledge of number of active sites per unit area  $n$  and bubble emission frequency  $f$ . In the preceding sections procedures have been described to determine these quantities as function of known parameters except unknown quantities  $c_0$  and  $r_r$ . Equation of Wiebe and Judd is as follows:

$$h = c_3 (nf)^a \quad (5.20)$$

Where  $c_3$  is a constant and,  $a$ , is  $1/2$  and  $1/3$  for values of  $nf$  less and greater than  $55 \times 10^3$  Bubbles/in<sup>2</sup>.sec. respectively. When  $nf$  is not known, the value of,  $a$ , can be determined by regression analysis using the experimental data. Insertion of values of  $n$  from Eq. (5.6) in Eq(5.20) yields the following equation for heat transfer coefficient:

$$h = c_3 \left[ \left( \frac{10^{-(1.8)m}}{2^m} c_0 c_2^m r_r^m \right) \left\{ \left( \frac{\lambda^{2.5} \rho_v}{T_s^{1.5} \sigma} \right) \left( \frac{q}{k_l g} \right) \left( \frac{1}{\epsilon_l} \right)^{0.3} \right\}^{1.2} \right]^m \quad (5.21)$$

$$h = M \left[ \left\{ \left( \frac{\lambda^{2.5} \rho_v}{T_s^{1.5} \sigma} \right) \left( \frac{q}{k_l g} \right) \left( \frac{1}{\epsilon_l} \right)^{0.3} \right\}^{1.2} \right]^m \{f\} \quad (5.22)$$

where  $f$  is given by the respective equations, Eq. (5.15) or Eq. (5.19) for Jakob number less and greater than 100

and constant  $M \left[ = \left( c_3 \frac{10^{-(1.8)m}}{2^m} c_0 c_2^m r_r^m \right)^a \right]$

contains quantities whose measurement is extremely difficult. In order to utilise the resultant equation, Eq. (5.22) it is necessary to determine the nature of this constant  $M$ . When  $M$  is adequately defined it becomes possible to predict heat transfer coefficients from analytical relationship (that is, from considerations of heating surface characteristics and bubble dynamics).

To obtain the value for constant  $M$ , we proceed as follows:

Eq. (5.22) provides quantitative measure of the inter-relationship of the heat transfer coefficient and of the terms: wall heat flux and pertinent physico-thermal

properties of the boiling fluids. The analytical model, Eq.(5.22) does not account for the effects of pressure and surface-liquid combination explicitly. Therefore, it can be argued to treat the unknown constant  $M$  representing the combined effects of pressure and surface-liquid combination. The form of  $M$  can be intuitively expressed as follows:

$$M = \phi(P), \psi(C_{sf}) \quad (5.23)$$

where  $\phi$  is a function of pressure only and  $\psi$  is a function of surface - liquid combination factor. The present and existing experimental data will be used to show the multiplicative nature of  $M$  in Chapter 6. When one considers the bubble formation on a solid surface through which heat is transported into the fluid, the conditions for the dynamic equilibrium of a bubble attached to the heating surface are governed by the wettability of the solid by the boiling fluid among other factors. Thus the value of  $\psi(C_{sf})$ , as it is, depends on the nature of heating surface and the fluid in touch with it. As a matter of fact, it is highly improbable to describe the nature of heating surface. An implication of this would be that general agreement on the absolute values of heat transfer coefficient is possible only if the same heating surface is used in various investigations. But in industrial equipment the heating surfaces used are of widely differing nature. Therefore, a rigorous generalised correlation for absolute values of heat transfer coefficient from different heating



surfaces is extremely difficult. Keeping in view this inevitable difficulty and the proposed functional form of constant  $M$  it seems best to re-arrange Eq.(5.22) so as to yield the values of ratio,  $h^*/h_1^*$ , where  $h_1^*$  is the value at the normal boiling point. Thus the function,  $\Psi(C_{sf})$  is easily eliminated and the data of different investigators obtained on different heating surfaces should be correlated fairly well by the resultant equation. Therefore, the general equation for the prediction of  $h^*/h_1^*$  assumes the following form where  $f$  is given by the respective equations, Eq.(5.15) or Eq.(5.19) for Jakob number less and greater than 100.

$$\frac{h^*}{h_1^*} = \frac{M}{M_1} \left[ \left( \frac{\lambda}{\lambda_1} \right)^{2.5} \left( \frac{\rho_v}{\rho_{v1}} \right) \left( \frac{T_{sl}}{T_s} \right)^{1.5} \left( \frac{\sigma_1}{\sigma} \right) \left( \frac{k_{\ell 1}}{k_{\ell}} \right)^{0.3} \left( \frac{q}{q_1} \right)^{0.3} \left( \frac{C_{\ell 1}}{C_{\ell}} \right)^{1.2} \right]^m \left\{ \frac{f}{f_1} \right\}^a \quad (5.24)$$

subscript '1' denotes the values corresponding to normal boiling point.

where  $M/M_1 = \phi(P)/\phi(P_1)$  which can be represented as function of  $(P/P_1)$  as follows:

$$\frac{M}{M_1} = \eta(P/P_1) \quad (5.25)$$

The analytical model, Eq. (5.24) serves to illustrate the general nature of heat transfer to boiling fluids from

the heating surfaces. It is important to note that the resultant equation is independent of surface-liquid combination factor,  $C_{sf}$ ; and therefore this equation should serve to compare the data on differing heating surfaces. Further, this equation, Eq. (5.24) is capable to predict heat transfer coefficients at subatmospheric pressures if the value of  $h_1^*$  is adequately known.

The predicted values of wall superheat and heat transfer coefficient from the present analysis as discussed above, have been compared with the experimentally measured values of present study and existing investigations in Chapter 6.

## C H A P T E R 6

### RESULTS AND DISCUSSION

A total of 149 runs were conducted. Of these 30 were for distilled water, 45 for isopropanol, 39 for ethanol and 35 for methanol.

The data with ranges of experimental parameters are listed in Tables B-1, B-2, B-3 and B-4 of Appendix B. Columns 6 and 7 list corrected temperature difference & point values of heat transfer coefficient respectively.

In the present Chapter the experimental and the analytical results of nucleate pool boiling of fluids at atmospheric and subatmospheric pressures are discussed. Computer programs were written on an IBM 360 digital computer for calculations for all the runs reported in Appendix B. The inputs to these programs are: heat flux, heating surface temperature, liquid saturation temperature, system pressure, and physico-thermal properties of boiling fluids at their saturation temperature.

#### 6.1 LIMITATIONS OF ANALYSIS

The practical limitations which have been used in the analysis of present experimental data are summarized as follows:

In the present investigation the measurement of wall temperature was done at three locations around the heating

surface by means of thermocouples as discussed in Section 3.2.2. Fluid temperatures were also measured at three positions corresponding to the wall thermocouple locations. Experimental data as recorded in Appendix B show that wall and the fluid temperatures vary circumferentially. Therefore, there was a need to evaluate average wall temperature,  $\bar{T}_w$  and average temperature difference,  $\overline{\Delta T}$  for further analysis and interpretation of the experimental results. The values of  $\overline{\Delta T}$  were required to calculate average experimental heat transfer coefficients. In order to calculate these quantities the following procedures have been employed:

Average values of  $\overline{\Delta T}$  over the circumference was calculated by the method of mechanical quadrature using  $\Delta T$  values at the top, at the middle and at the bottom of the heating surface.  $\Delta T$  values at these locations represented the respective difference between corrected wall temperature and fluid temperature. The corrected wall temperatures were determined by subtracting temperature drop across the wall from the thermocouple readings. In some of the calculations, average values of wall temperatures and wall superheat  $\overline{\Delta T}_w$  over the circumference were also required. These have also been obtained by mechanical quadrature method as detailed in Appendix A.

The fluid temperature around the heating surface was found to vary. However, the thermophysical properties

of the boiling fluid were approximated to the properties of the fluid at the saturation temperature corresponding to the system pressure. This has been accepted because the variation in liquid temperature around the heating surface was small enough to cause any significant change in the pertinent physico-thermal properties of the boiling fluids.

The longitudinal conduction of heat in the heating surface has been neglected since the heating surface was a long tube of thin wall.

## 6.2 COMPARISON OF EXPERIMENTAL VALUES OF HEAT TRANSFER COEFFICIENT WITH HEAT FLUX AT ATMOSPHERIC PRESSURE

To test the extent of the validity of the widely accepted relationship;  $h \propto q^{0.7}$ , the heat transfer coefficients of distilled water, isopropanol, ethanol and methanol are plotted in Figures 6.1 through 6.4 respectively as functions of heat flux. The experimental observations of the present study have been augmented with the data available in the literature [11], [28], [42], [98], [135]. These figures show that heat transfer coefficient — heat flux relationship ( $h \propto q^{0.7}$ ) is valid for all the liquids investigated. A trend similar to that illustrated on present data is evident in the data of other investigators. This ensures that the measurements and techniques used for data collection in the present investigation are reliable.

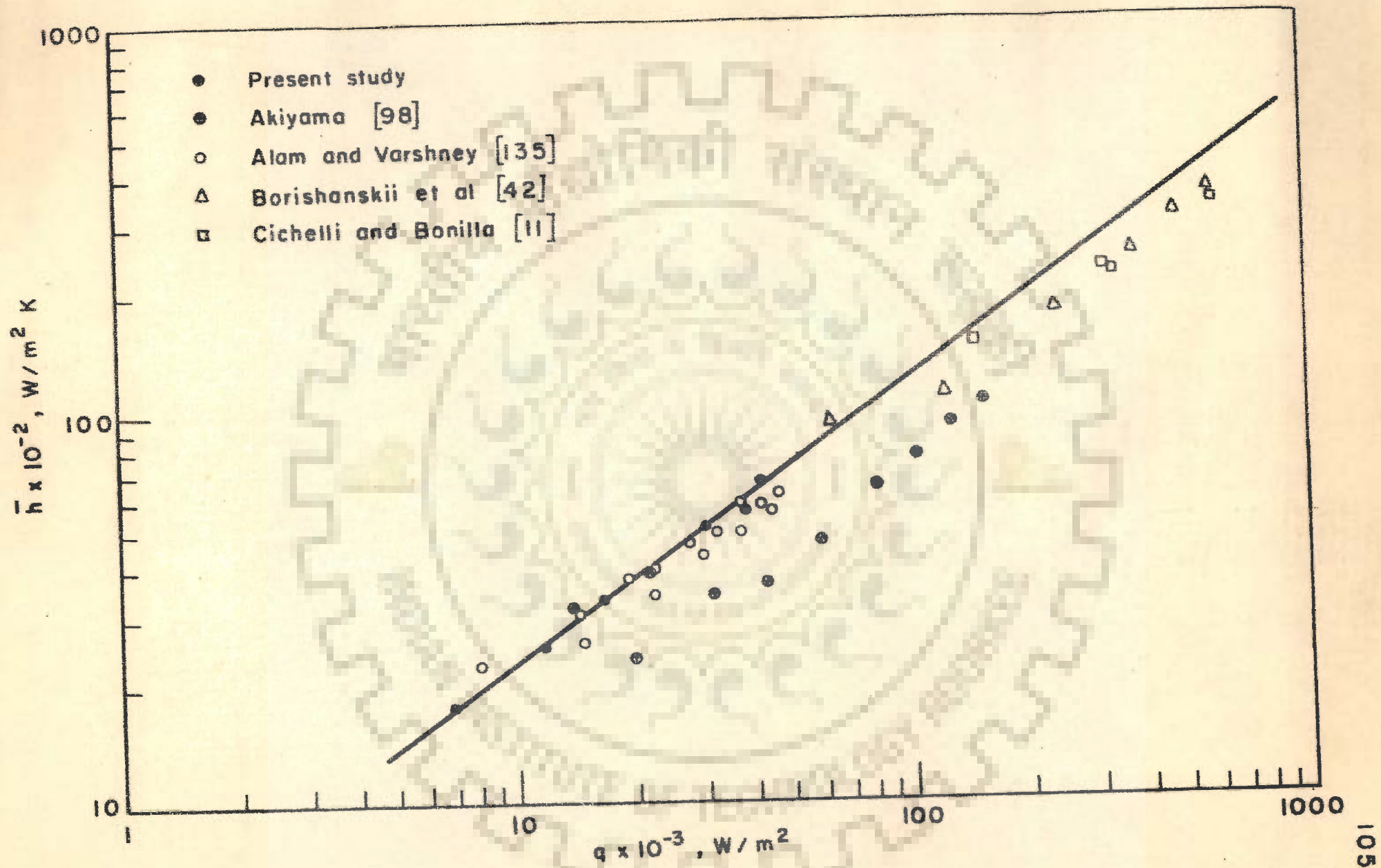


Fig. 6-1 Heat transfer coefficient - heat flux relationship for distilled water at atmospheric pressure

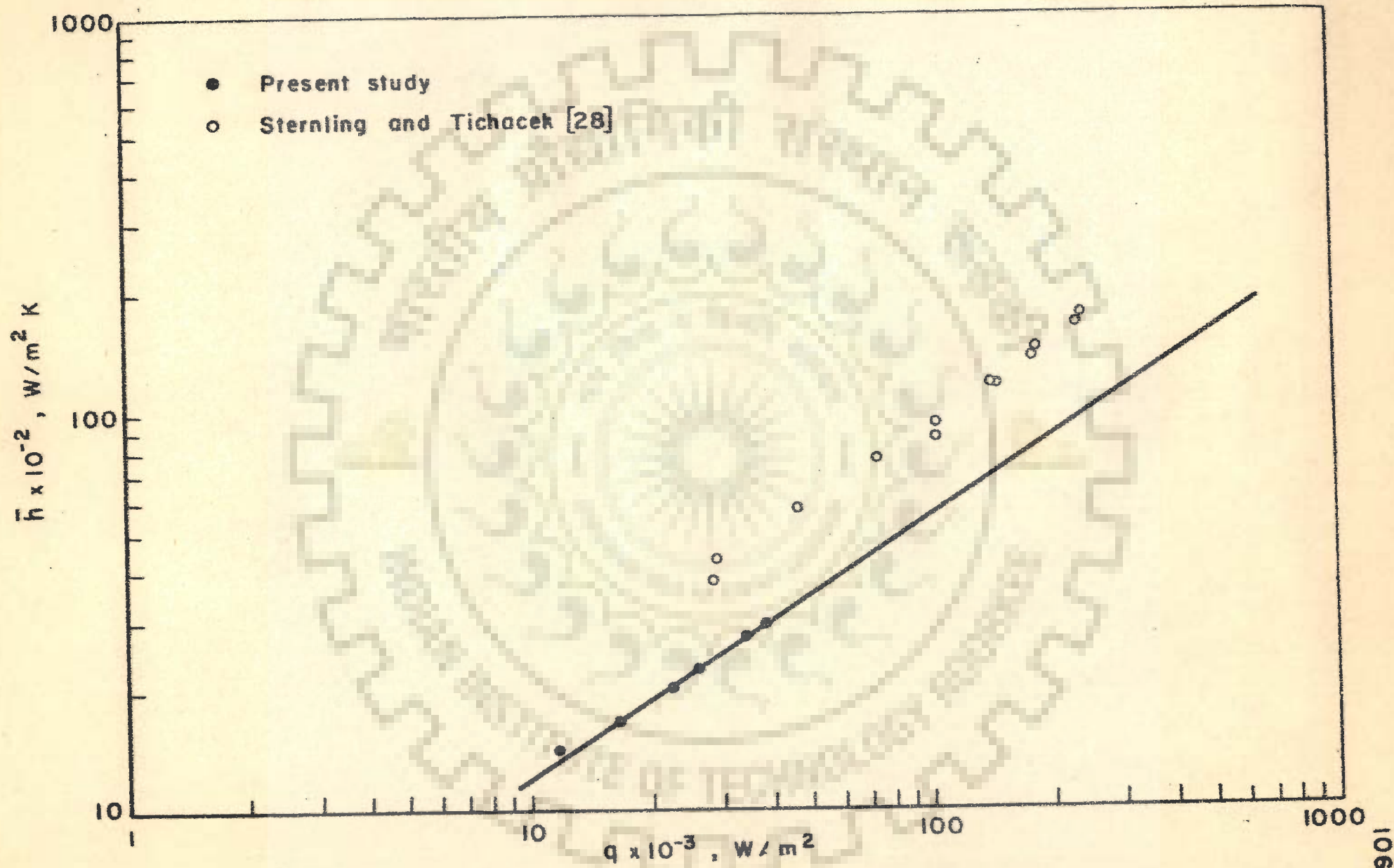


Fig. 6-2 Heat transfer coefficient-heat flux relationship for isopropanol at atmospheric pressure

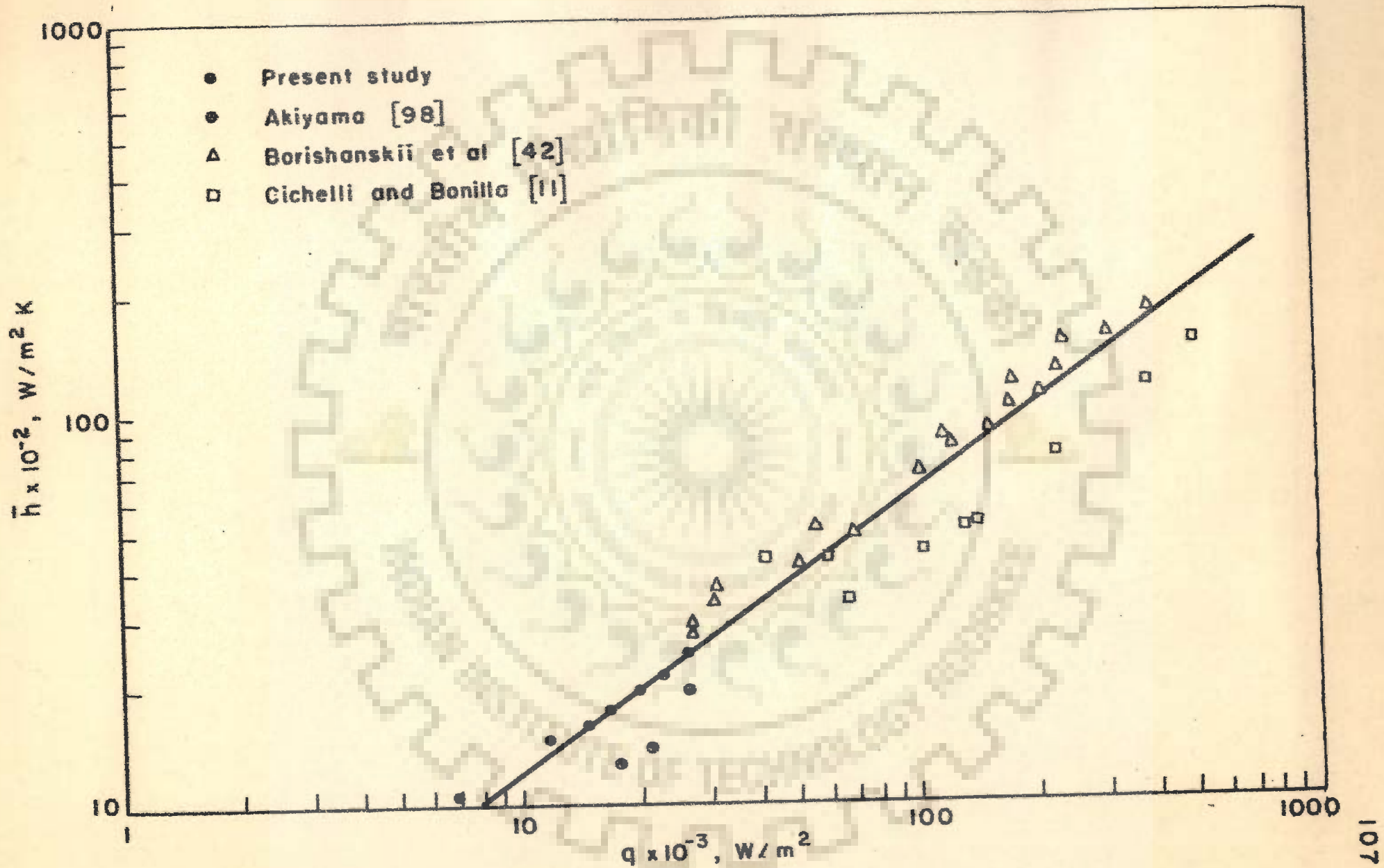


Fig. 6-3 Heat transfer coefficient-heat flux relationship for ethanol at atmospheric pressure



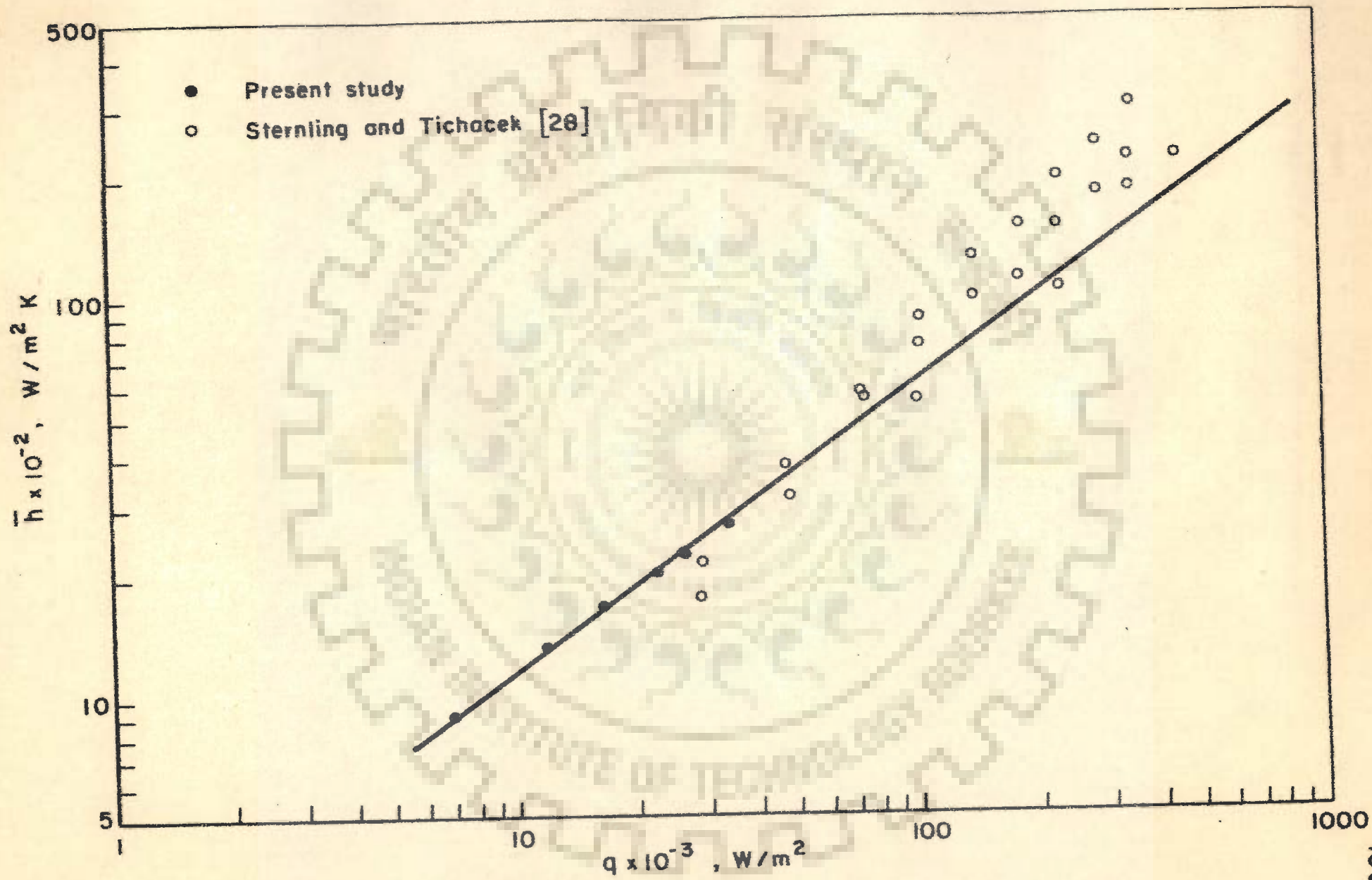


Fig. 6.4 Heat transfer coefficient - heat flux relationship for methanol at atmospheric pressure

Some of the experimental data [28], [42], [98] exhibit disagreement with the present values, but there is clearly a general correspondence between the two as a function of heat flux over a whole range of heat flux shown. It can be seen that these data form separate groupings about the lines with the slope of 0.7. This indicates that a single expression may not adequately relate heat transfer coefficient to heat flux for all heat transfer surfaces and liquids. This behaviour is not surprising but reassures the result that the characteristics of heating surface and the nature of boiling fluids in touch with it play a significant role on boiling heat transfer rates.

Whether the value of constant  $b$  is affected mainly or entirely by the surface characteristics and the nature of liquid remains to be proved.

### 6.3 HEAT TRANSFER COEFFICIENT—HEAT FLUX RELATIONSHIP OVER A RANGE OF SUBATMOSPHERIC PRESSURE

In this section the experimental data of the boiling fluids for subatmospheric pressure were examined by plotting them in Figures 6.5 to 6.8. The main purpose herein is to determine the relationship between heat transfer coefficient and heat flux in boiling fluids for pressures less than atmospheric pressure. It is seen from these figures that the experimental data for subatmospheric pressures can be correlated by the same relationship as for atmospheric pressure ( $h = bq^{0.7}$ ) with constant  $b$  depending upon the system pressure. The constant  $b$  decreases with

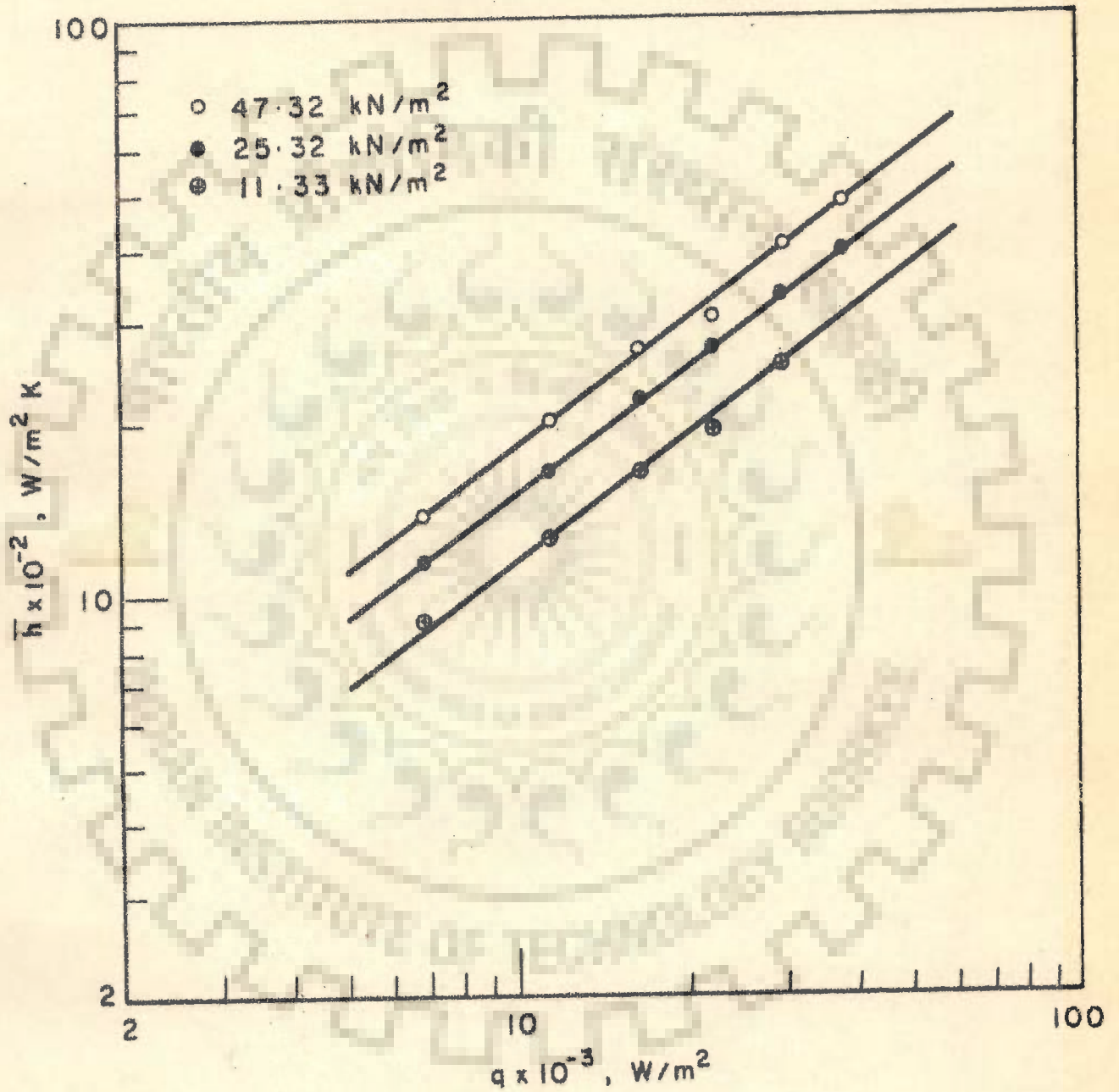


Fig. 6.5 Heat transfer coefficient—heat flux for distilled water at subatmospheric pressures

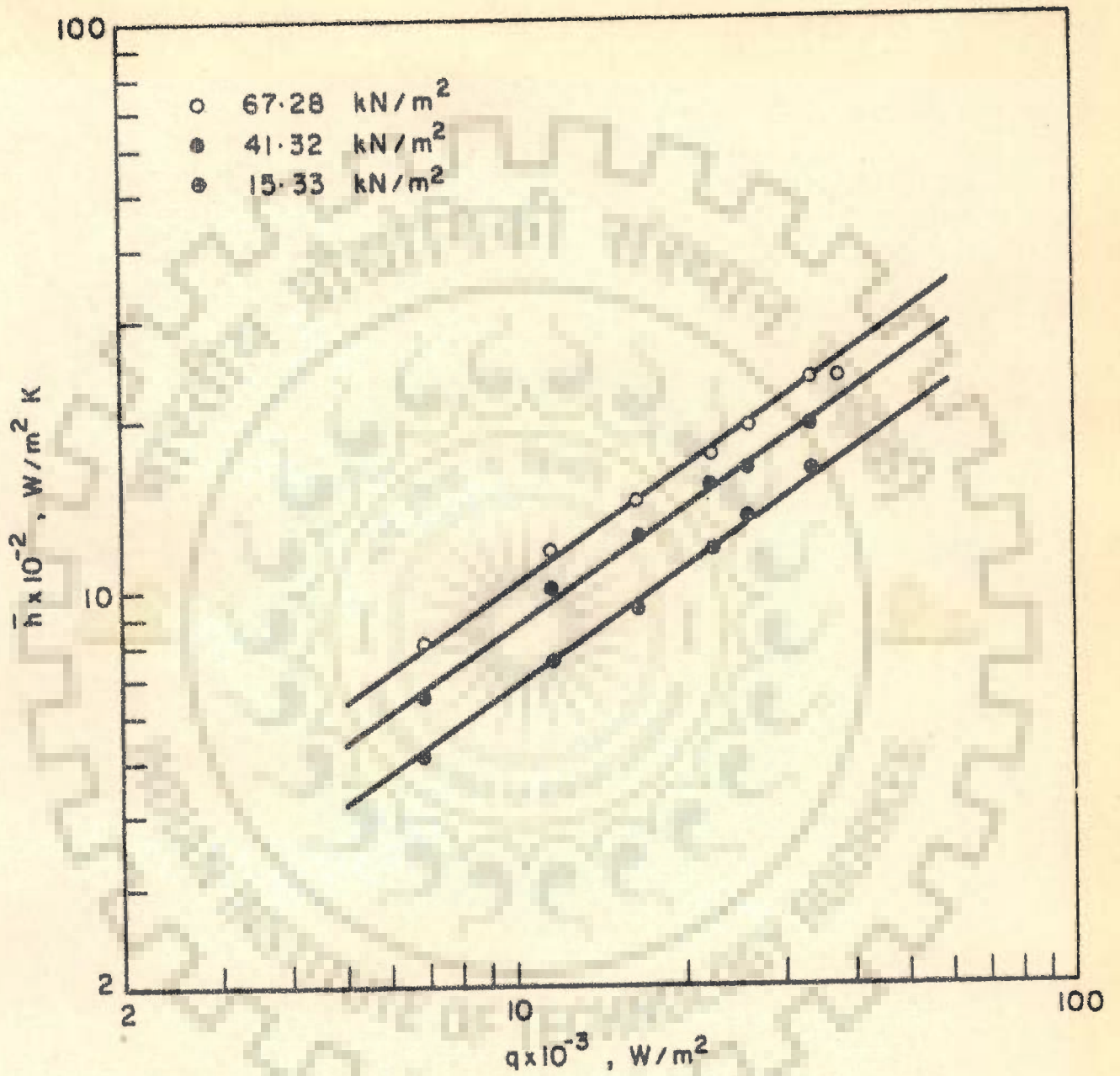


Fig. 6-6 Heat transfer coefficient-heat flux for isopropanol at subatmospheric pressures

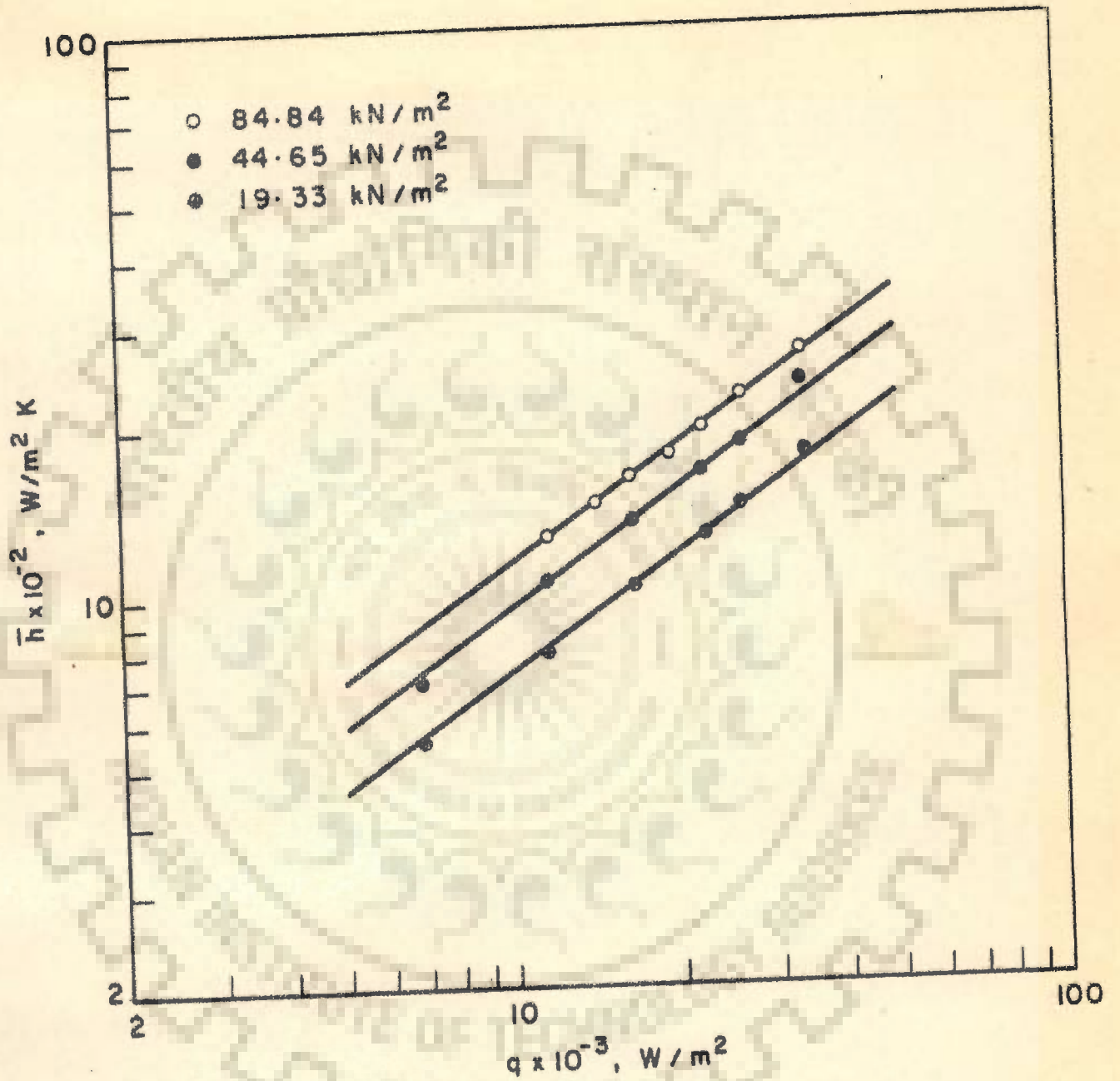


Fig. 6.7 Heat transfer coefficient–heat flux for ethanol at subatmospheric pressures

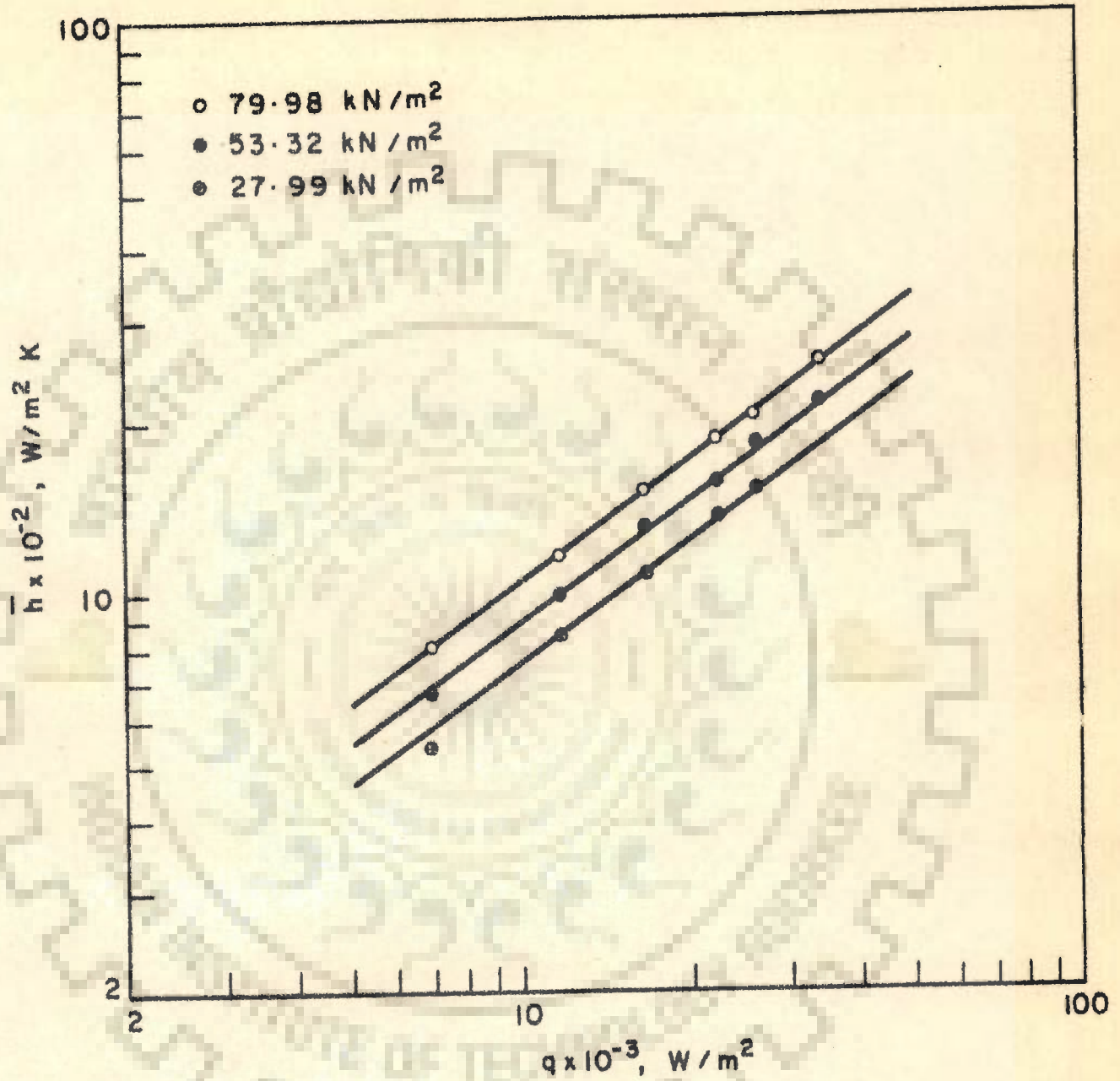


Fig. 6-8 Heat transfer coefficient-heat flux for methanol at subatmospheric pressures

the decrease in pressure . The superimpos of this section and of the previous section concludes that constant  $b$  is complex which among other parameters is affected by surface characteristics, nature of boiling fluids and pressure as well. An implication of this would be that constant  $b$  cannot be incorporated in accurate theoretical analysis of the boiling heat transfer in which the proportionality constant  $b$  relating heat transfer coefficient with heat flux is sought as an exact theoretical value.

#### 6.4 COMPARISON BETWEEN EXPERIMENTAL WALL SUPERHEAT AND PREDICTED VALUES FROM ALAD'EV EQUATION

Alad'ev equation [55] relates wall superheat to wall heat flux and pertinent physico-thermal properties of water in nucleate pool boiling for pressure range from 0.09 to 200 atmospheres.

Figure 6.9 shows comparison between experimentally measured and predicted values of wall superheat from the Alad'ev equation, Eq. (5.4) as follows: The predictions are in good agreement with the experimental data for distilled water. The equation underpredicted the values for isopropanol, ethanol and methanol. The possible reason for this discrepancy among other reasons seems to be due to that this equation was derived for the experimental data of water only. Therefore, it can be concluded that the Alad'ev equation does not possess general applicability for liquids differing in their physico-thermal properties.

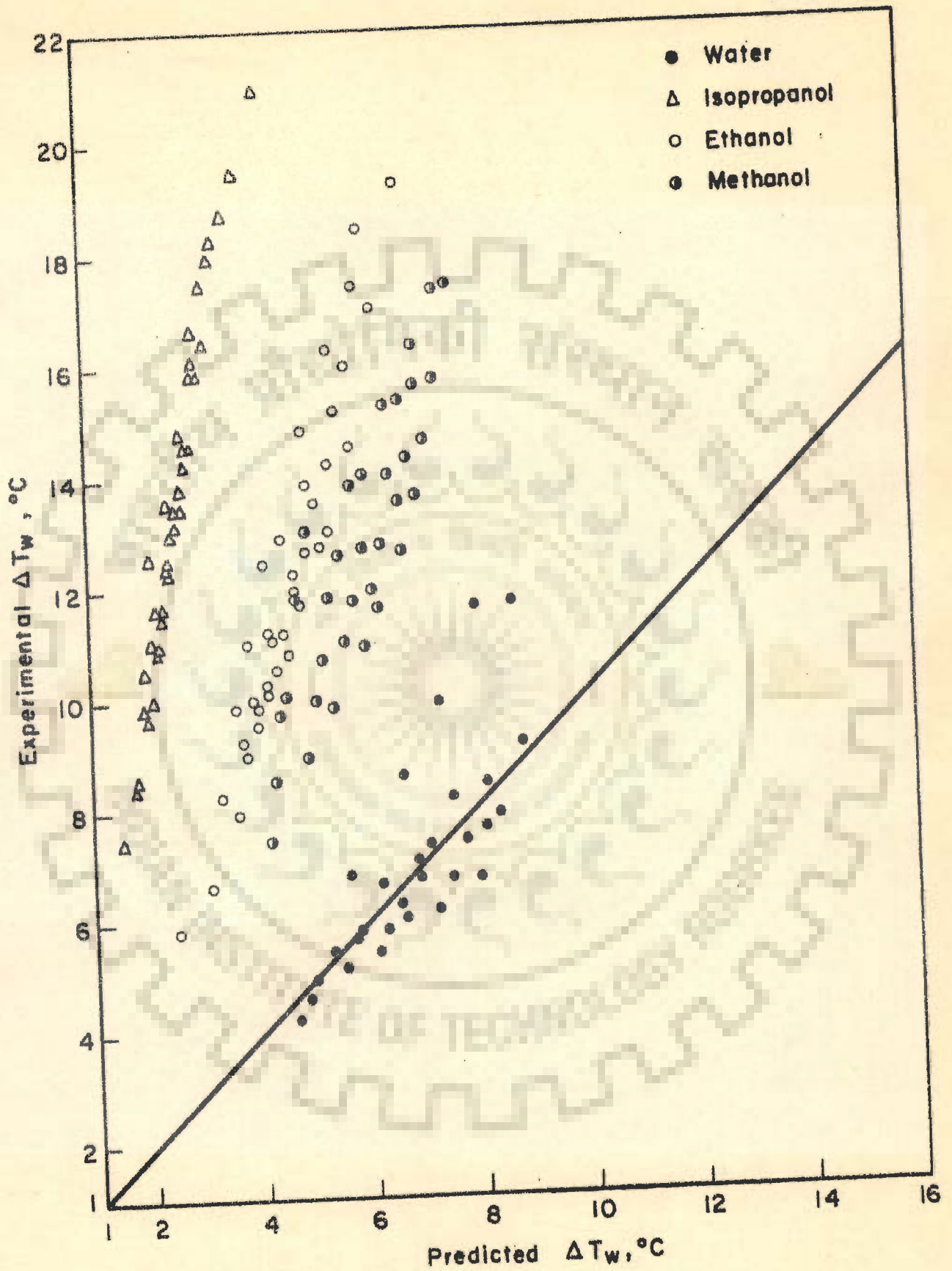


Fig. 6-9 Present experimental data compared with the Alad'ev equation, Eq(5-4)



It is intuitively obvious that the constant of the Alad'ev equation represents the surface-liquid combination effect. With this in view an attempt was made to modify the constant of the equation without altering the basic form of the equation. Computation revealed that the most optimum value of constant was found to depend upon the surface-liquid combination. For respective liquids the values of the constant are given in Table 6.1.

Table 6.1 The values of constant  $c_2$  of Eq. (5.4a)

Liquid	$c_2$
Distilled water	$4.70 \times 10^{-3}$
Isopropanol	$2.40 \times 10^{-2}$
Ethanol	$1.24 \times 10^{-2}$
Methanol	$9.99 \times 10^{-3}$

With the values of constant  $c_2$  from Table 6.1 calculations were made to obtain predicted values of wall superheat. The predicted values are compared with the average experimental values for isopropanol, ethanol and methanol in Figures 6.10 and 6.11. These figures show that the comparison is excellent within a maximum of  $\pm 15$  per cent. An implication of this would be that surface-liquid combination plays a significant role on wall superheat of heating surfaces in nucleate pool boiling. Therefore, the Alad'ev equation may then be written as follows:

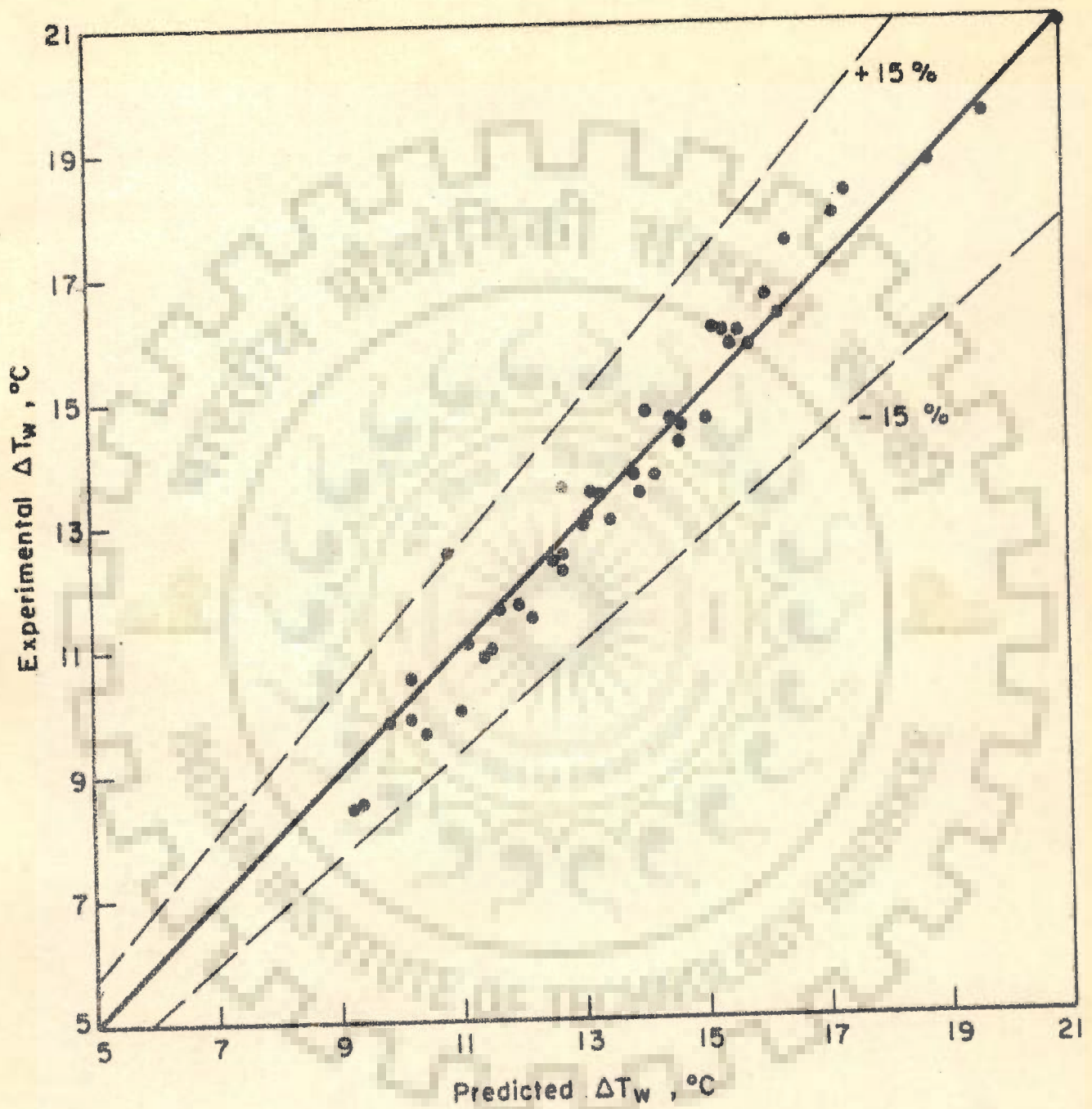


Fig. 6-10 Present experimental data of isopropanol compared with the modified Alad'ev equation, Eq(6-1)

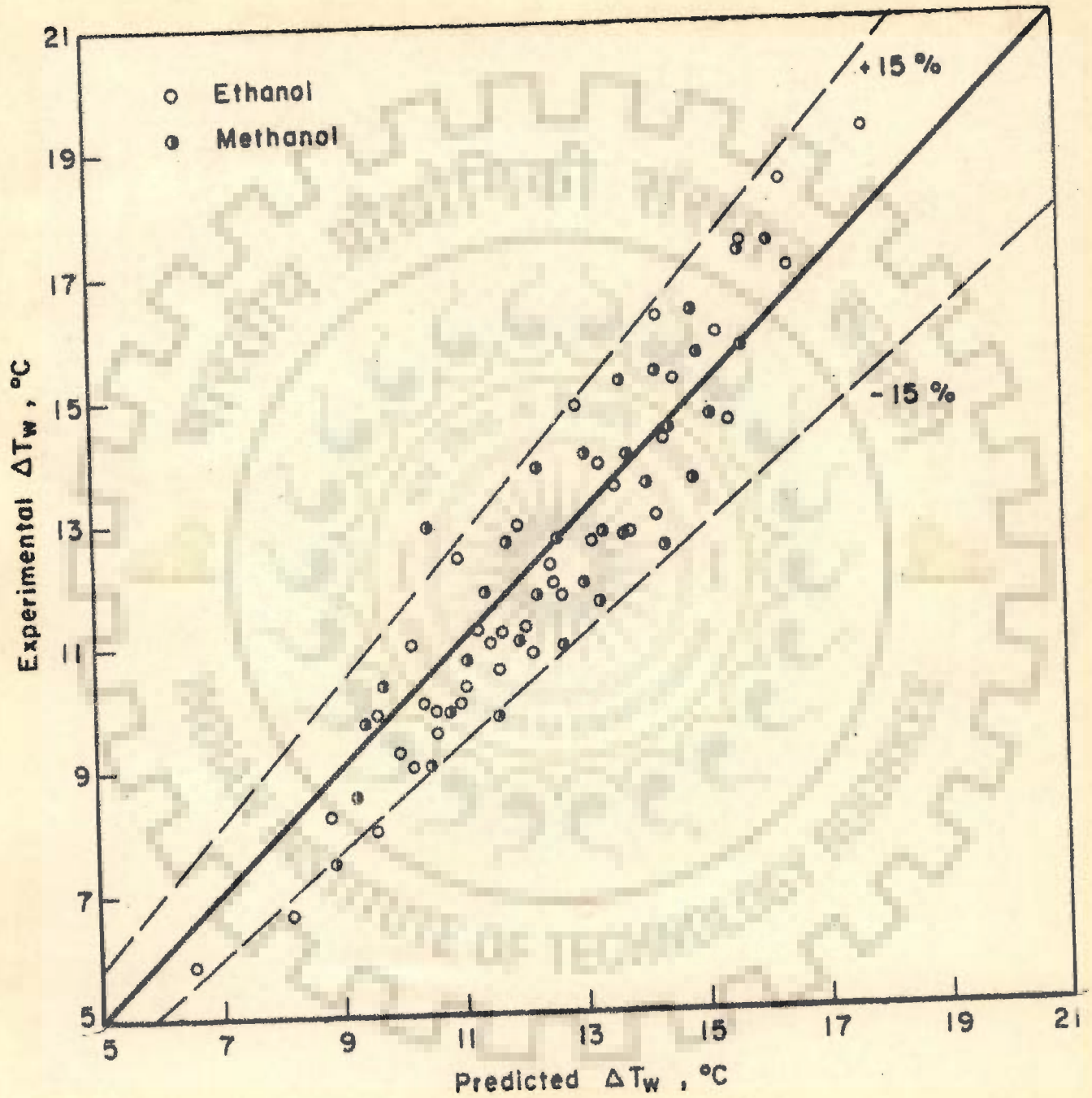


Fig. 6.11 Present experimental data compared with the modified Alad'ev equation, Eq (6.1)

$$\frac{\Delta T_w}{T_s} = c_2 \left[ \frac{10^{-6} q \lambda}{k_{\ell} T_s \delta} \right]^{0.3} \left[ \frac{\lambda}{C_{\ell} T_s} \right]^{1.2} \quad (6.1)$$

Where constant  $c_2$  is to be taken from Table 6.1 for the liquids investigated. It is important to recall that in the analytical analysis of Chapter 5 the Alad'ev equation was presumed to possess the same form [cf. (5.4a)] as above.

#### 6.5 COMPARISON BETWEEN THEORETICAL FREQUENCY FROM PROPOSED MODEL AND EXISTING EXPERIMENTAL DATA

Following the analysis of Cole and Shulman [66] for bubble growth rate and the analysis of Han and Griffith [106] for transient thermal layer thickness,  $\delta$  Eqs.(5.15 & 5.19) were developed in Section 5.2.3 of Chapter 5 for the determination of bubble emission frequency,  $f$ . Cole [45] has measured experimentally the values of frequency for the given values of  $\theta_w$ ,  $\theta_d$  and  $Ja$  as parameters at atmospheric and subatmospheric pressures. Therefore, a comparison was made between the experimental values of frequency measured by Cole [45] and the calculated values from the present analysis, Eqs.(5.15 & 5.19) for almost similar values of  $\theta_w$ ,  $\theta_d$  and  $Ja$ . These values are given in Table 6.2.

Table 6.2 Comparison between predicted frequency from Eq.(5.15 or 5.19) and experimental values of Cole [45]

Liquid	Ja	$\theta_d, s$		$\theta_w, s$		$f, s^{-1}$	
		Exptl.	Predt.	Exptl.	Predt.	Exptl.	Predt.
Water	87.9	0.039	0.0477	0.694	0.3351	1.36	2.61
	191.0	0.034	0.0927	0.222	0.8060	3.91	1.11
Methanol	41.2	0.015	0.0300	0.087	0.0750	9.79	9.41
	59.6	0.019	0.0255	0.141	0.0915	6.22	8.54
	74.6	0.025	0.0358	0.298	0.3337	3.09	2.71

It is clear from the above table that the agreement between predicted and experimental values of frequency is fairly well and encouraging.

#### 6.6 BUBBLE EMISSION FREQUENCY — HEAT FLUX RELATIONSHIP FOR ATMOSPHERIC AND SUBATMOSPHERIC PRESSURES

In Chapter 5 Eqs. (5.15 and 5.19) for  $f$  were derived from theoretical considerations. As obvious from these equations that at a given system pressure frequency depends upon heat flux. Therefore, typical plots were drawn between  $f$  and  $q$  on log log scale with pressure as parameter in Figures 6.12 through 6.15. From these figures it is seen that the variation of  $f$  with  $q$  is represented by a power law of the following form:

$$f = C_L q^{n_L} \quad (6.2)$$

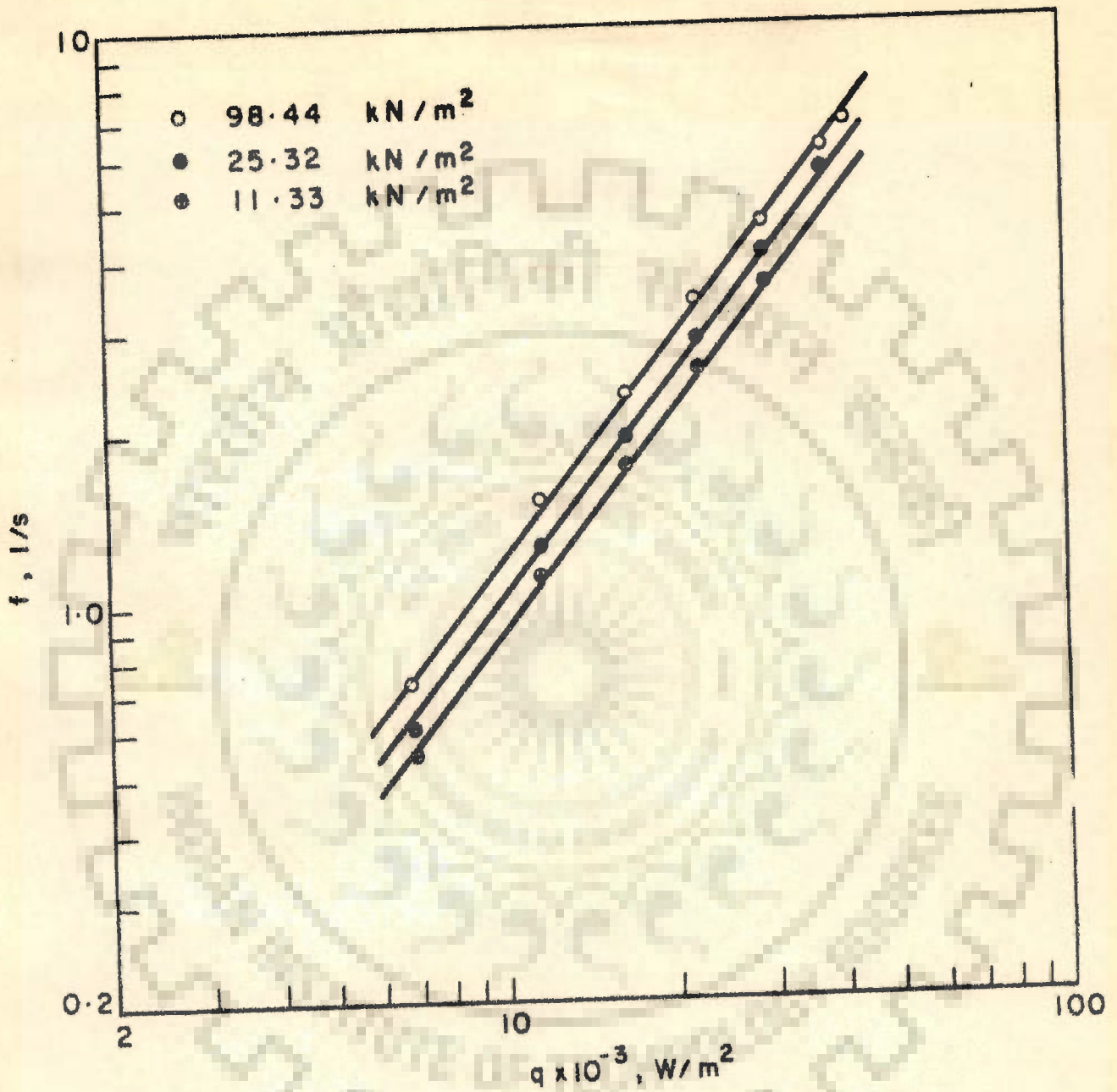


Fig. 6-12 Frequency - heat flux relationship for distilled water

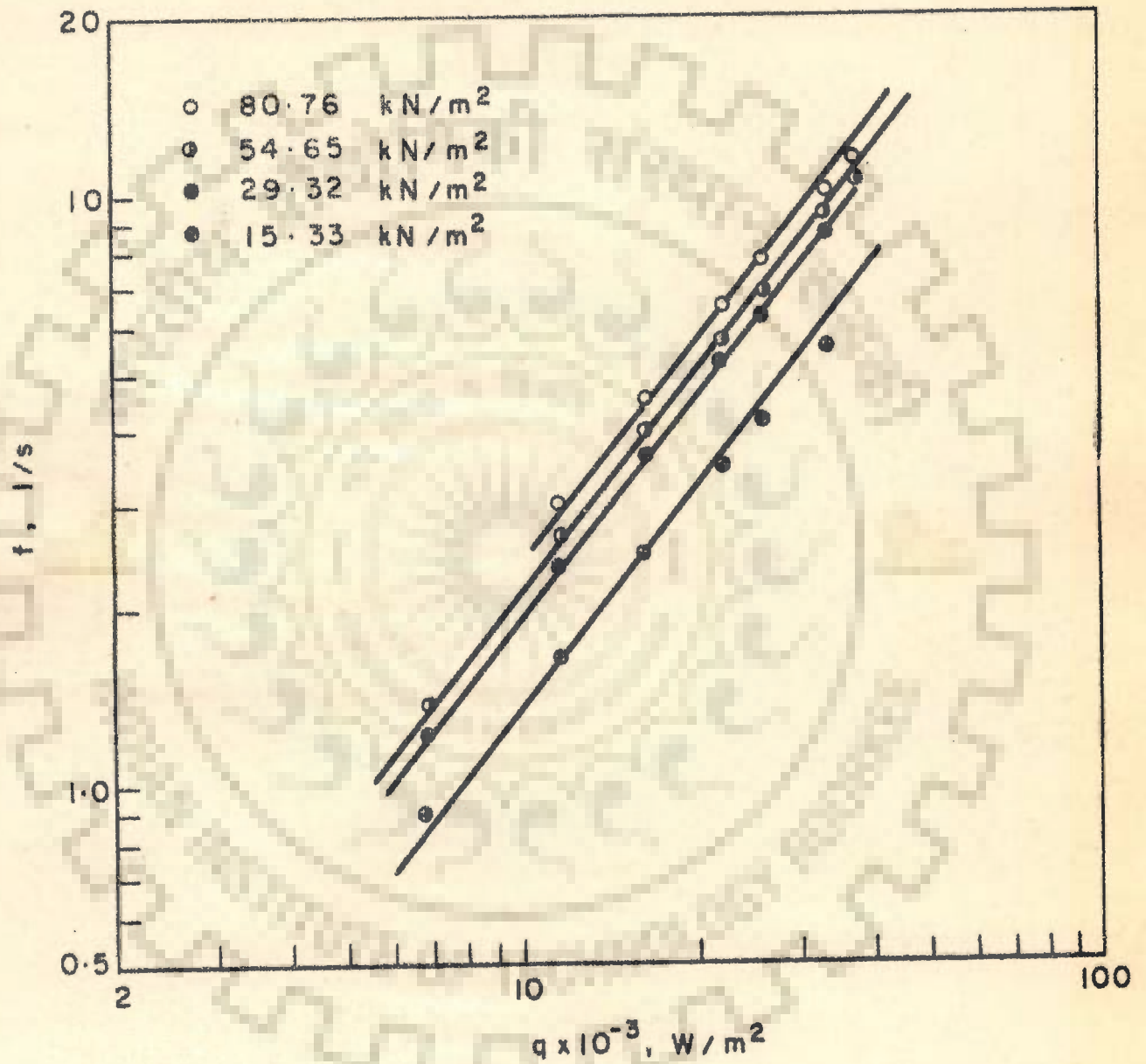


Fig. 6.13 Frequency - heat flux relationship for isopropanol

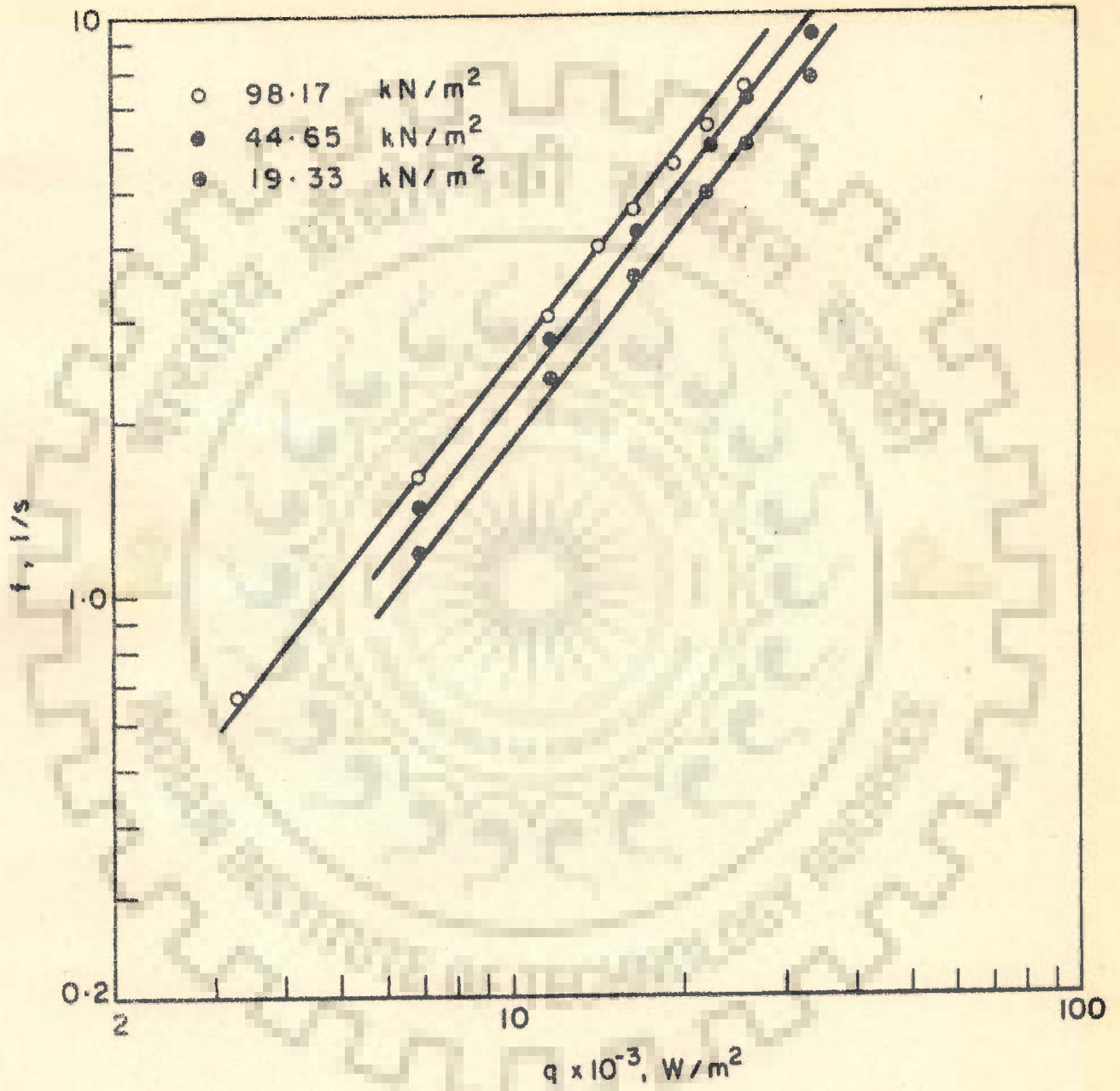


Fig. 6.14 Frequency - heat flux relationship for ethanol



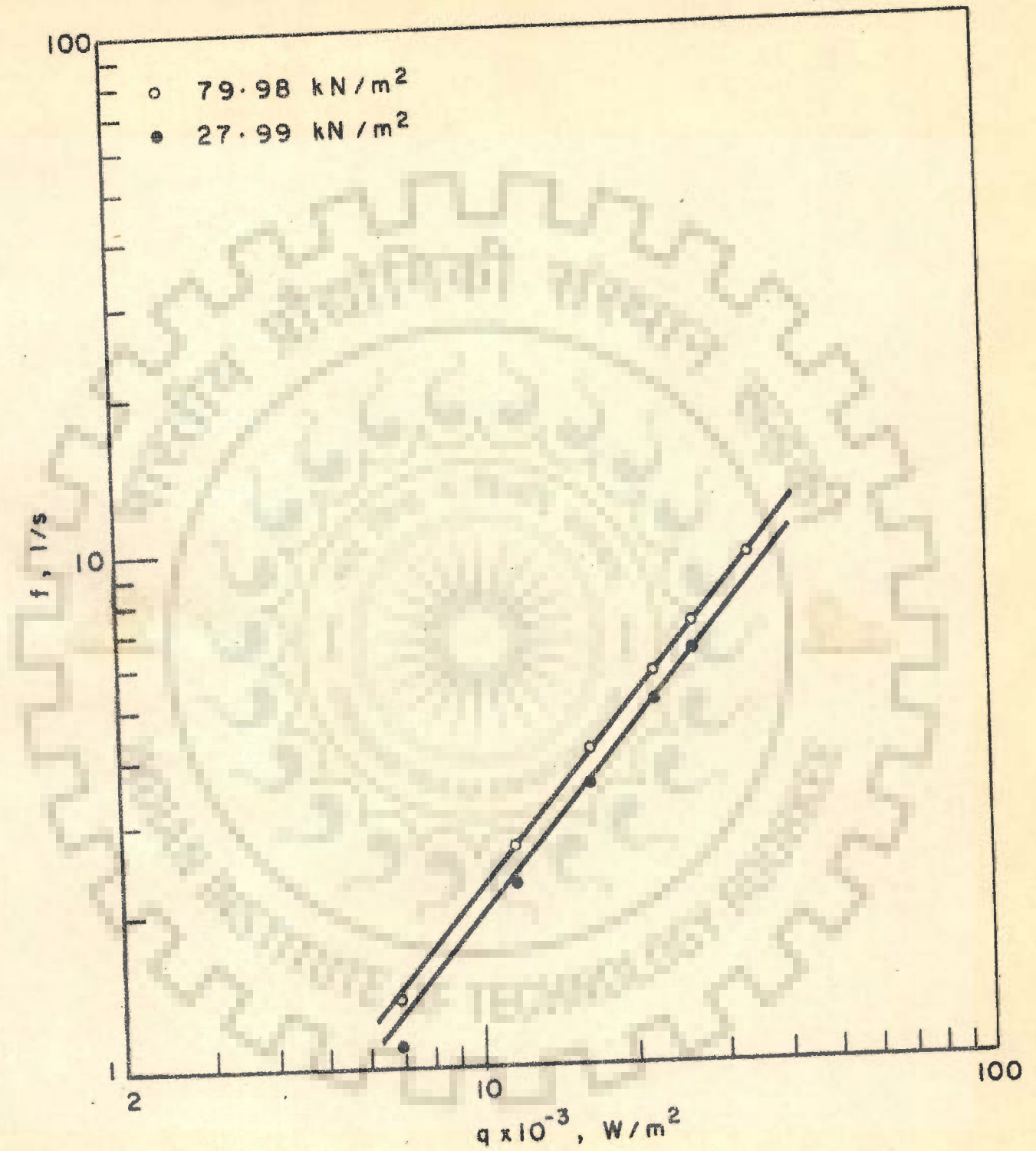


Fig. 6.15 Frequency - heat flux relationship for methanol

The values of constant  $C_{l_1}$  and exponent  $n_{l_1}$  were determined by the method of least squares curve fitting and are given in Table 6.3.

Table 6.3 Values of constant  $C_{l_1}$  and exponent  $n_{l_1}$  in Eq. (6.2)

Distilled water			Isopropanol		
Pressure kN/m <sup>2</sup>	$C_{l_1} \times 10^5$	$n_{l_1}$	Pressure kN/m <sup>2</sup>	$C_{l_1} \times 10^4$	$n_{l_1}$
98.44	1.506	1.226	97.97	0.940	1.120
66.65	0.991	1.265	80.76	0.685	1.142
47.32	0.864	1.275	67.28	0.358	1.199
25.33	0.633	1.299	54.65	0.360	1.194
11.33	0.578	1.297	41.32	0.240	1.233
-	-	-	29.32	0.255	1.220
-	-	-	15.33	0.237	1.186

Ethanol			Methanol		
Pressure kN/m <sup>2</sup>	$C_{l_1} \times 10^4$	$n_{l_1}$	Pressure kN/m <sup>2</sup>	$C_{l_1} \times 10^4$	$n_{l_1}$
98.17	0.450	1.186	98.64	0.308	1.213
84.84	0.918	1.117	79.98	0.261	1.229
71.31	0.545	1.166	66.65	0.240	1.236
44.65	0.432	1.180	53.32	0.203	1.249
31.32	0.264	1.226	41.32	0.154	1.275
19.33	0.354	1.182	27.99	0.115	1.299

It is seen from the above table that  $C_{l_1}$  is a strong function of pressure and boiling fluids while  $n_{l_1}$  does not change appreciably. Therefore, the value of  $n_{l_1}$  for all the liquids investigated can be averaged arithmetically and is equal to 1.221. Thus Eq. (6.2) assumes the

following form:

$$f = C_4 q^{1.221} \quad (6.2a)$$

### 6.7 VARIATION OF $h^*/h_1^*$ WITH $P/P_1$

Referring to Figures 6.5 through 6.8 it is seen that the heat transfer coefficient varies with the wall heat flux, system pressure and boiling fluids. It is also a fact that  $h$  depends on heating surface as well. These figures also reveal that for a given pressure, fluid and heating surface  $h^*(=h/q^{0.7})$  bears a constant value (implying  $h \propto q^{0.7}$ ). Thus  $h^*$  is a function of pressure only for a given fluid and heating surface. Therefore, a plot of values of the ratio,  $h^*/h_1^*$  against  $P/P_1$  would become independent of boiling fluids and heating surfaces. Such a plot would correlate the data points of different investigations taken on different heating surfaces. This procedure was applied to the pool boiling data of present study alongwith the data of Cryder and Finalborgo [5] for water and methanol on a brass tube, data of Akiyama et al [79] for water on stainless steel tube and of Minchenko and Firsova [136] for distilled water. In Figure 6.16, the values of  $h^*/h_1^*$  versus  $P/P_1$  are plotted. The figure reveals that the relation between  $h^*/h_1^*$  and  $P/P_1$  is independent of boiling fluids and the heating surfaces as envisioned above.

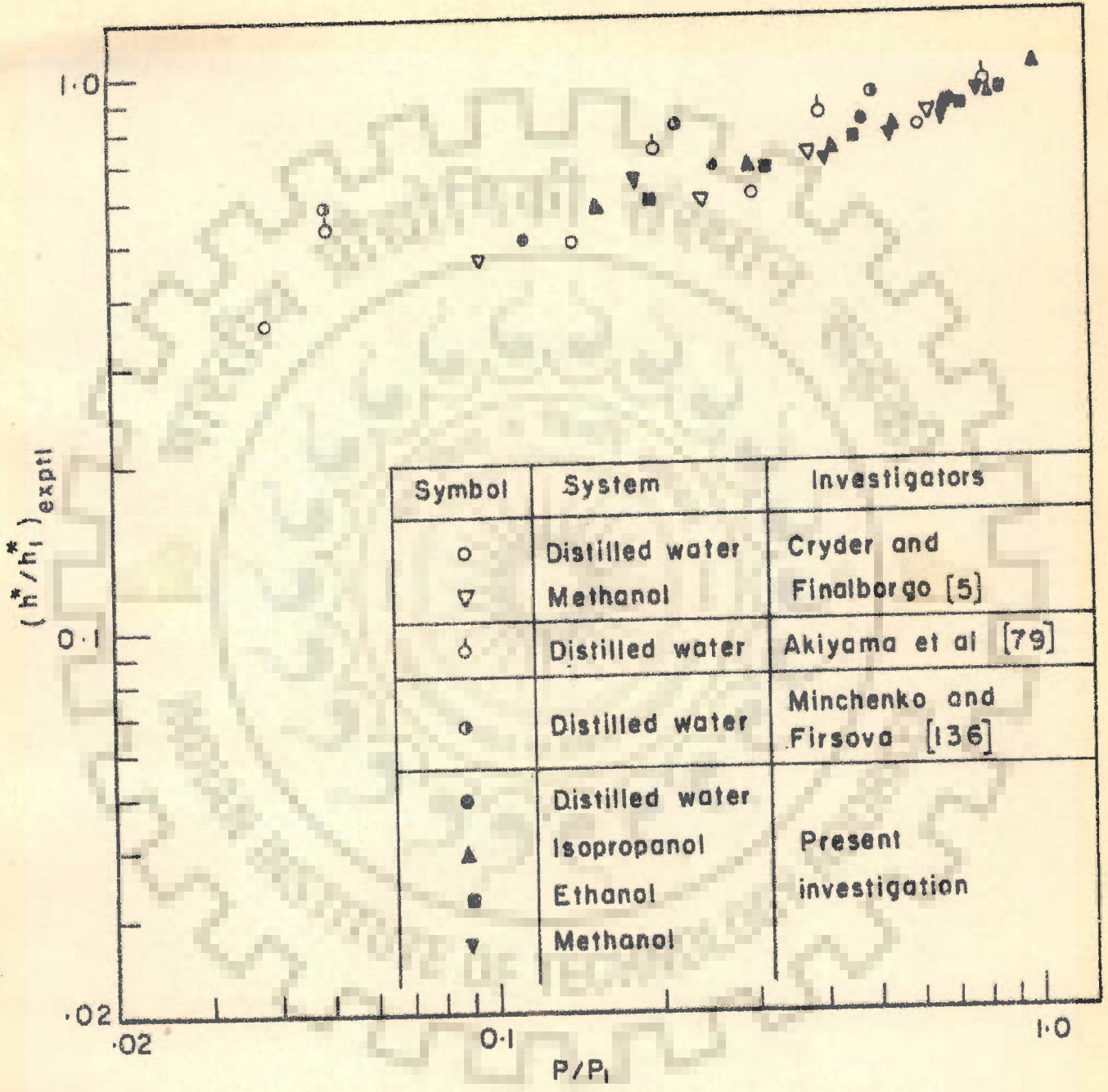


Fig. 6-16 A plot of  $\bar{h}^*/h_1^*$  vs  $P/P_1$

## 6.8 PREDICTIONS FROM KUTATELADZE et al ANALYSIS [19]

Kutateladze et al analysis is available for predicting  $h^*/h_1^*$  from the knowledge of physico-thermal properties of the boiling fluids, bubble departure diameter and bubble emission frequency. In this section the validity of the analysis is scrutinised by comparing the predicted values from it with the experimental data of present investigation and the data of Borishanskii et al [42].

Figure 6.17 shows a comparison between the experimental values of  $h^*/h_1^*$  of present study with the predicted values from the above analysis [19]. It is found that the analysis is inconsistent with these experimental data.

Figure 6.18 represents comparison between the predicted values and the experimental data of Borishanskii et al for distilled water. The experimental data of Borishanskii et al corresponds to pressures greater than atmospheric pressure. It is seen from this figure that the Kutateladze et al analysis is consistent with the experimental data at pressures greater than one atmosphere. However, the analysis does not correlate the experimental data for atmospheric and subatmospheric pressures satisfactorily.

## 6.9 DETERMINATION OF CONSTANT M IN Eq(5.22)

In order to determine the value of constant M in Eq.(5.22) it was required to know the value of exponents m and a. Mikic and Rohsenow [43] recommended the value of

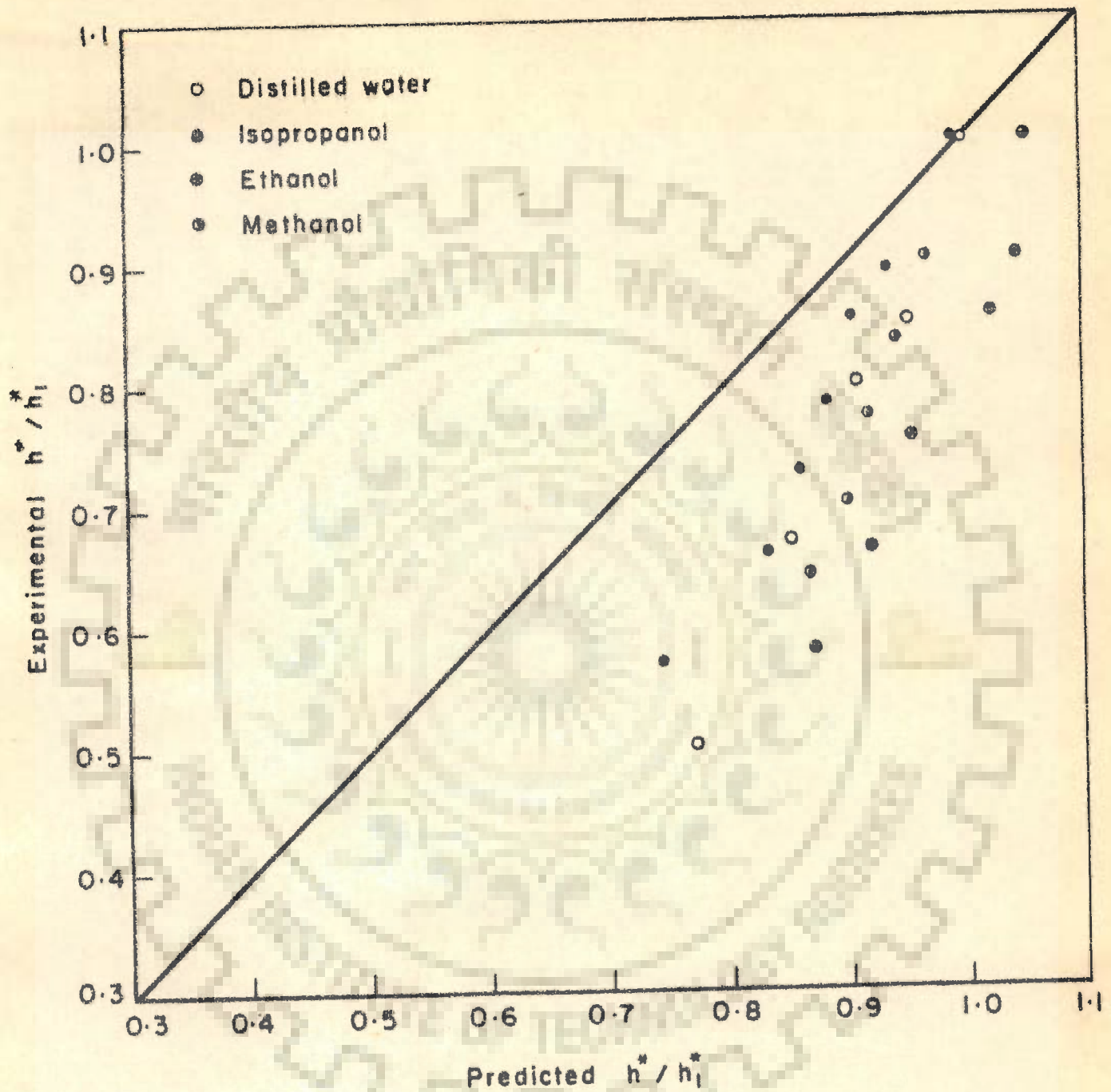


Fig. 6-17 Present experimental data compared with the Kutateladze et al analysis [19]

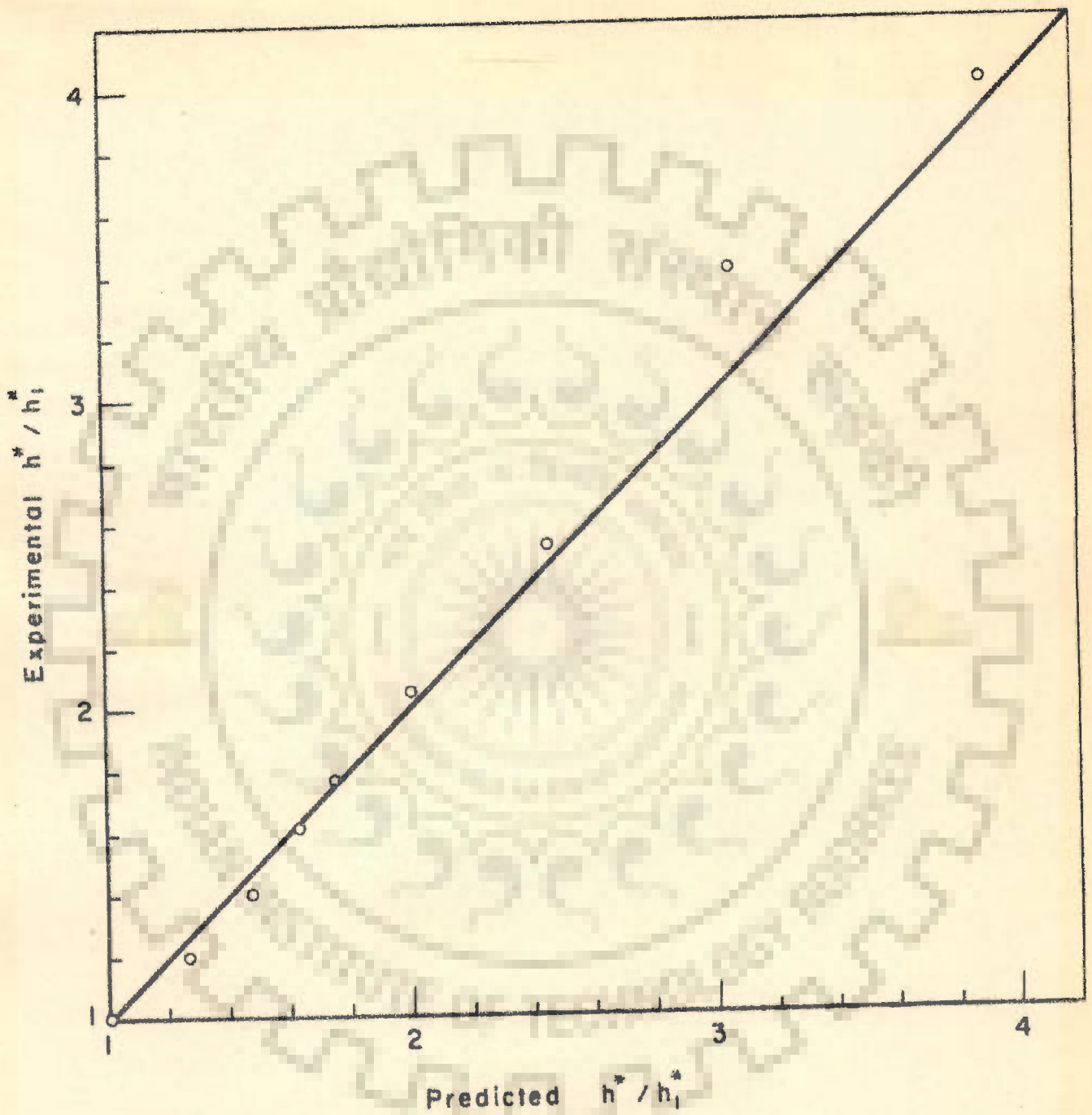


Fig. 6-18 Experimental data of Borishanskii et al [42] for distilled water compared with Kutateladze et al analysis [19]

m as 2.5 for water implying that  $q \propto \Delta T^{3.5}$  and 3.0 for organic liquids. However, the present data and data of many others conclude that  $q$  varies with  $\Delta T$  raised to the power of 3.33. Therefore, it is thought desirable to choose the value of  $m$  as 2.33 (implying  $q \propto \Delta T^{3.33}$ ). Exponent  $a$  was evaluated by the method of regression analysis using the entire experimental data. The values of exponent  $a$  ranged from 0.3046 to 0.3982 for all the pressures and fluids investigated. The analysis thus permitted to take an average value of 0.3683 for all the fluids employed in this investigation. It is interesting to mention here that this value is closer to 0.33 found by Wiebe and Judd [54] for the value of  $nf$  greater than  $55 \times 10^3$  Bubbles/ in<sup>2</sup>.sec. Hence these data seem to belong to the range of experimental parameters for which the value of  $nf$  are nearer to  $55 \times 10^3$  Bubbles/ in<sup>2</sup>.sec as recommended by the investigation of Wiebe and Judd which is based on careful photographic studies conducted by Judd[137].

In Chapter 5 , it is shown that  $M$  contains quantities whose measurement is extremely difficult . It is among many reasons due to the insufficient information about the surface characteristics. Therefore, one of the suitable methods for the determination of  $M$  may be by using the experimental data in Eq.(5.22) with exponent  $m$ (=2.33) and  $a$  equal to 0.3683 as determined above. These computations revealed that the value of  $M$  changes with pressure and with surface-liquid combination as well. Table 6.4 shows the



values of M for different pressures and surface-liquid combinations. Thus the argument made in Chapter 5, to treat the unknown constant M, representing the combined effects of pressure and surface-liquid combination seems to hold true.

Table 6.4 Experimental values of M for different pressures and surface-liquid combinations

Surface: Stainless steel

Distilled Water		Isopropanol		Ethanol		Methanol	
P kN/m <sup>2</sup>	Mx 10 <sup>5</sup>	P kN/m <sup>2</sup>	M/x10 <sup>5</sup>	P kN/m <sup>2</sup>	Mx10 <sup>5</sup>	P kN/m <sup>2</sup>	Mx10 <sup>5</sup>
98.442	1.14423	97.975	0.38961	98.175	0.22279	98.642	0.18169
66.650	1.29275	80.767	0.39247	84.845	0.22650	79.980	0.19005
47.321	1.55930	67.284	0.41480	71.315	0.24309	66.650	0.19864
25.327	2.07603	54.653	0.44132	44.655	0.29264	55.320	0.21521
11.330	2.92766	41.323	0.49432	31.325	0.33066	41.323	0.23885
-	-	29.326	0.57047	19.328	0.41347	27.993	0.29634
-	-	15.329	0.73346	-	-	-	-

Table 6.4 suggests that a mathematical relationship can be established relating constant M with system pressure P for a given surface-liquid combination. To accomplish this, regression analysis technique was employed. Three simple functions of hyperbolic, power and semilog were tried. In most of the cases these functions fitted quite well and gave coefficient of correlation varying from 0.8796 to 0.9927 for individual liquids. Tables 6.5, 6.6 and 6.7 show the properties

of these respective regression lines fitted on the experimental data.

Table 6.5 Properties of hyperbolic regression lines for M and P ( $M = P/[A + BP]$ ) for different fluids

Fluid	A	B	Coefficient of correlation
Distilled water	8.4759386E+04	-6.4150661E+05	0.9022
Isopropanol	2.7128524E+05	-2.2458743E+06	0.9485
Ethanol	4.8756164E+05	-5.1291132E+06	0.9583
Methanol	6.2898417E+05	-8.3686995E+05	0.9736

Table 6.6 Properties of power regression lines for M and P ( $M = AP^B$ ) for different fluids

Fluid	A	B	Coefficient of correlation
Distilled water	8.6193800E-05	-4.4409803E-01	0.9927
Isopropanol	1.8924030E-05	-3.5615637E-01	0.9801
Ethanol	1.2634947E-05	-3.8381813E-01	0.9878
Methanol	1.0130812E-05	-3.823097E-01	0.9744

Table 6.7 Properties of semilog regression lines for M and P ( $M = A + B \log_e P$ ) for different fluids

Fluid	A	B	Coefficient of correlation
Distilled water	4.8334136E-05	-8.2849672E-06	0.9843
Isopropanol	1.2210266E-05	-1.8919490E-06	0.9715
Ethanol	7.3989023E-06	-1.1518216E-06	0.9810
Methanol	5.7514742E-06	-8.8112245E-07	0.9601

An inspection of these Tables reveals that the power and semilog regression lines are fitting the data better than the hyperbolic expression. However, the power function is the best in all cases where the coefficient of correlation is of the order of 0.9927. Thus the following equations in the form of power function could represent the relation between M and P for respective fluids:

For Distilled water

$$M = 8.61938E-05(P)^{-4.4409803E-01} \quad (a)$$

For Isopropanol

$$M = 1.8924030E-05(P)^{-3.5615637E-01} \quad (b)$$

For Ethanol

$$M = 1.2634947E-05(P)^{-3.8381813E-01} \quad (c) \quad \left. \vphantom{\begin{matrix} (a) \\ (b) \\ (c) \end{matrix}} \right\} (6.3)$$

For Methanol

$$M = 1.0130812E-05(P)^{-3.823097E-01} \quad (d)$$

Figure 6.19 shows the experimentally - determined values of M against the pressure P for different fluids investigated. The straight lines passing through the data points of respective fluids represent the equations, Eqs. (6.3a, 6.3b, 6.3c & 6.3d). It is seen that these equations well-correlate the experimental values of M.

Using the values of m and a as determined above, in Eq. (5.22) the following equation for absolute heat transfer coefficient results:

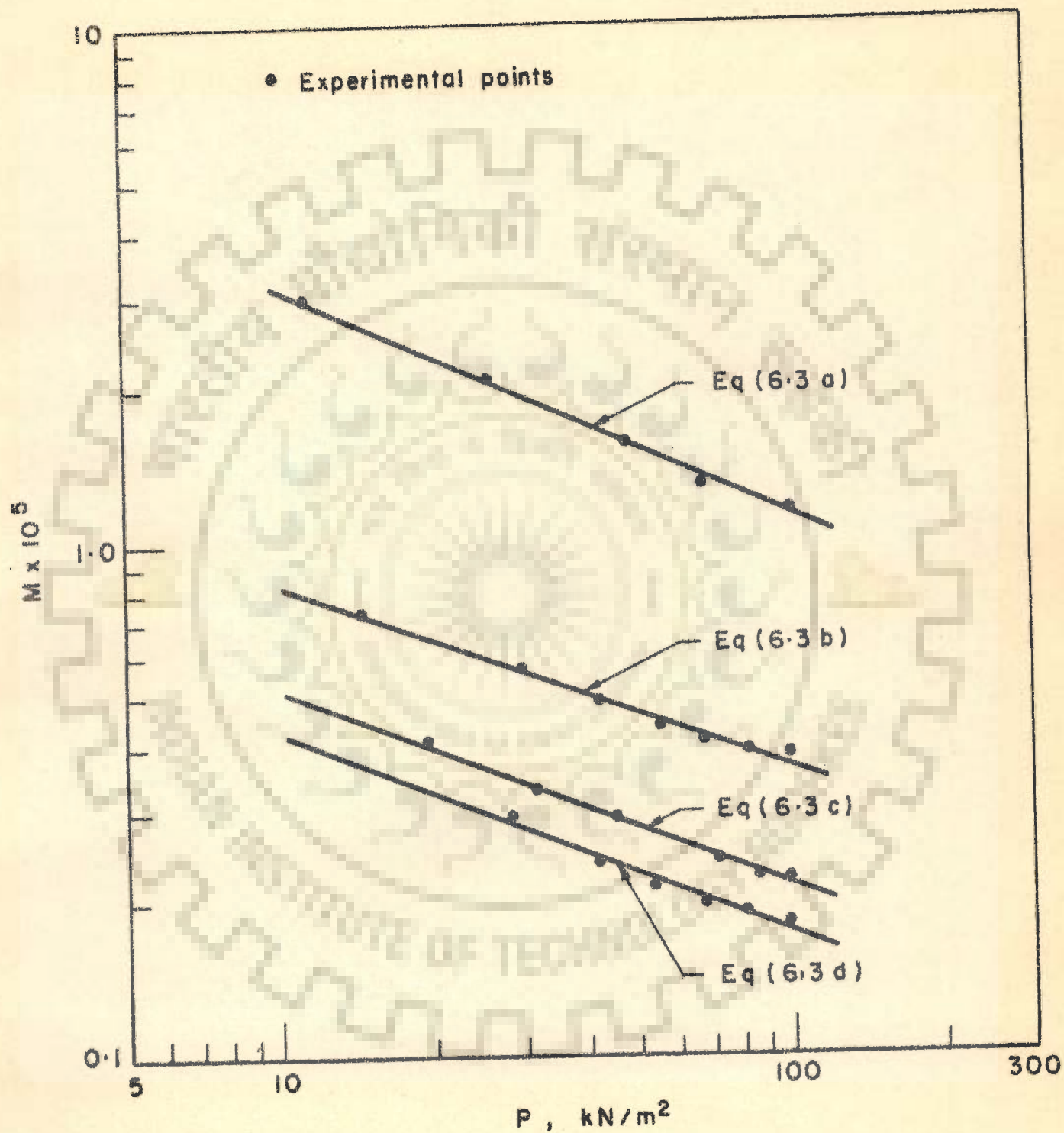


Fig. 6.19 Plots between  $M$  vs  $P$  for different fluids

$$h = M \left[ \left( \frac{\lambda^{2.5} \rho_v}{T_s^{1.5} \sigma} \right) \left( \frac{q}{k_l g} \right)^{0.3} \left( \frac{1}{C_l} \right)^{1.2} \right]^{2.33} \{f\}^{0.3683} \quad (6.4)$$

where  $M$  is calculated from Eq.(6.3)

It is of interest to examine the present analysis, Eq.(6.4) in conjunction with Eq.(6.2a). Using the value of  $f$  from Eq. (6.2a) into Eq.(6.4) the following equation results:

$$h = M C_l^{0.3683} \left[ \left( \frac{\lambda^{2.5} \rho_v}{T_s^{1.5} \sigma} \right) \left( \frac{1}{k_l g} \right)^{0.3} \left( \frac{1}{C_l} \right)^{1.2} \right]^{2.33} \left[ \frac{0.7065}{q} \right]$$

or  $h = \text{constant } q^{0.7065}$  for a given pressure.

Thus the widely accepted relationship that  $h$  varies with  $q$  raised to the power of 0.7 is deduced successfully.

The predicted values of absolute values of  $h$  from Eq.(6.4) are compared with the experimental ones in Figures 6.20 through 6.23 respectively for distilled water, isopropanol, ethanol and methanol. The agreement is excellent within a maximum deviation of  $\pm 10$  per cent.

#### 6.10 DETERMINATION OF $M/M_1$ IN Eq(5.25)

In order to determine the relationship between  $M/M_1$  and  $P/P_1$  the regression analysis, as detailed in Section 6.9, was employed considering all the data points. Fortunately, it is found that the data points for all the fluids are represented

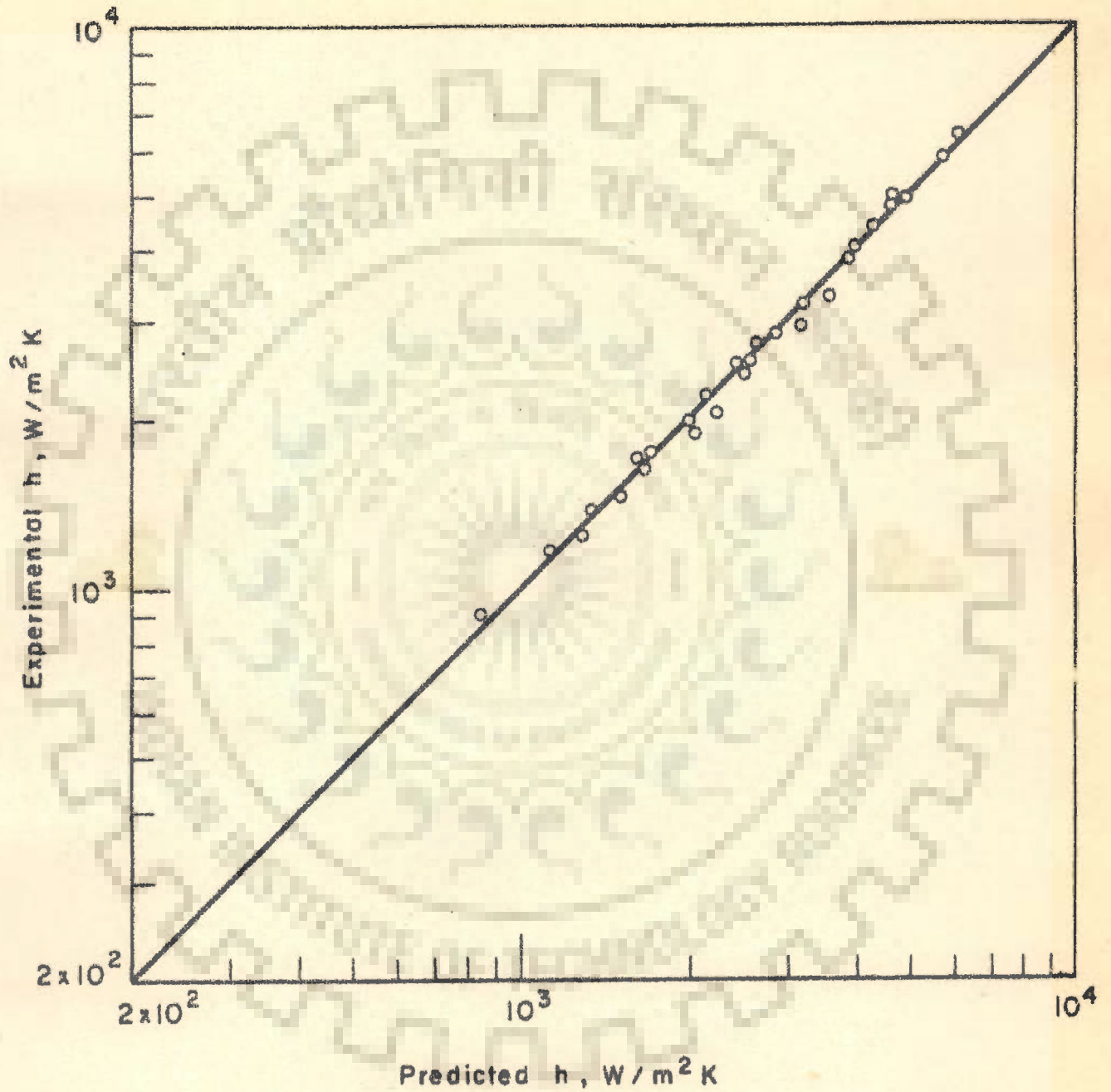


Fig. 6.20 Present experimental data for distilled water compared with the present analysis, Eqs (6.3a & 6.4)

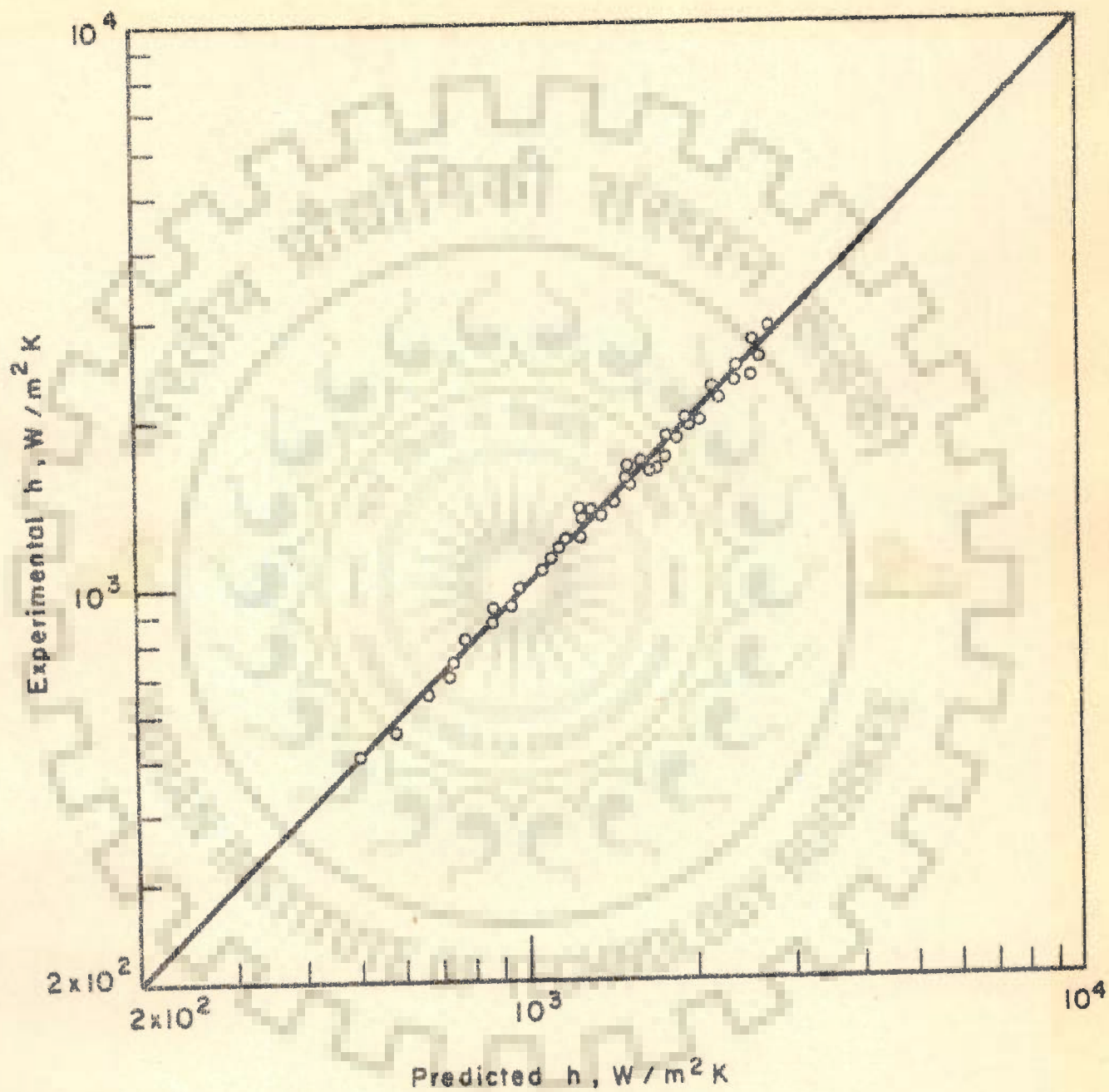


Fig. 6.21 Present experimental data for isopropanol compared with the present analysis, Eqs(6.3b & 6.4)

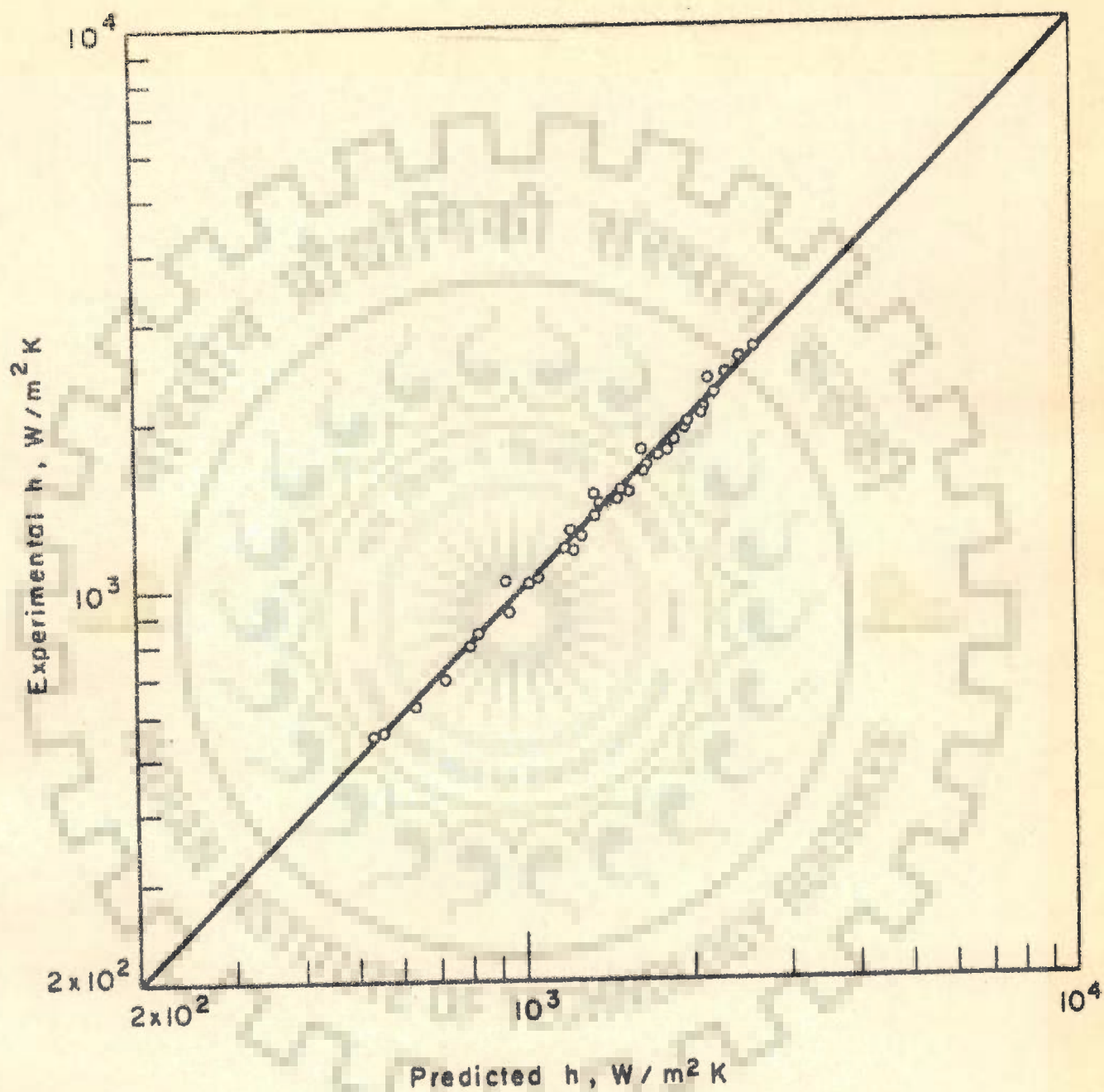


Fig. 6-22 Present experimental data for ethanol compared with the present analysis, Eqs (6-3c & 6-4)



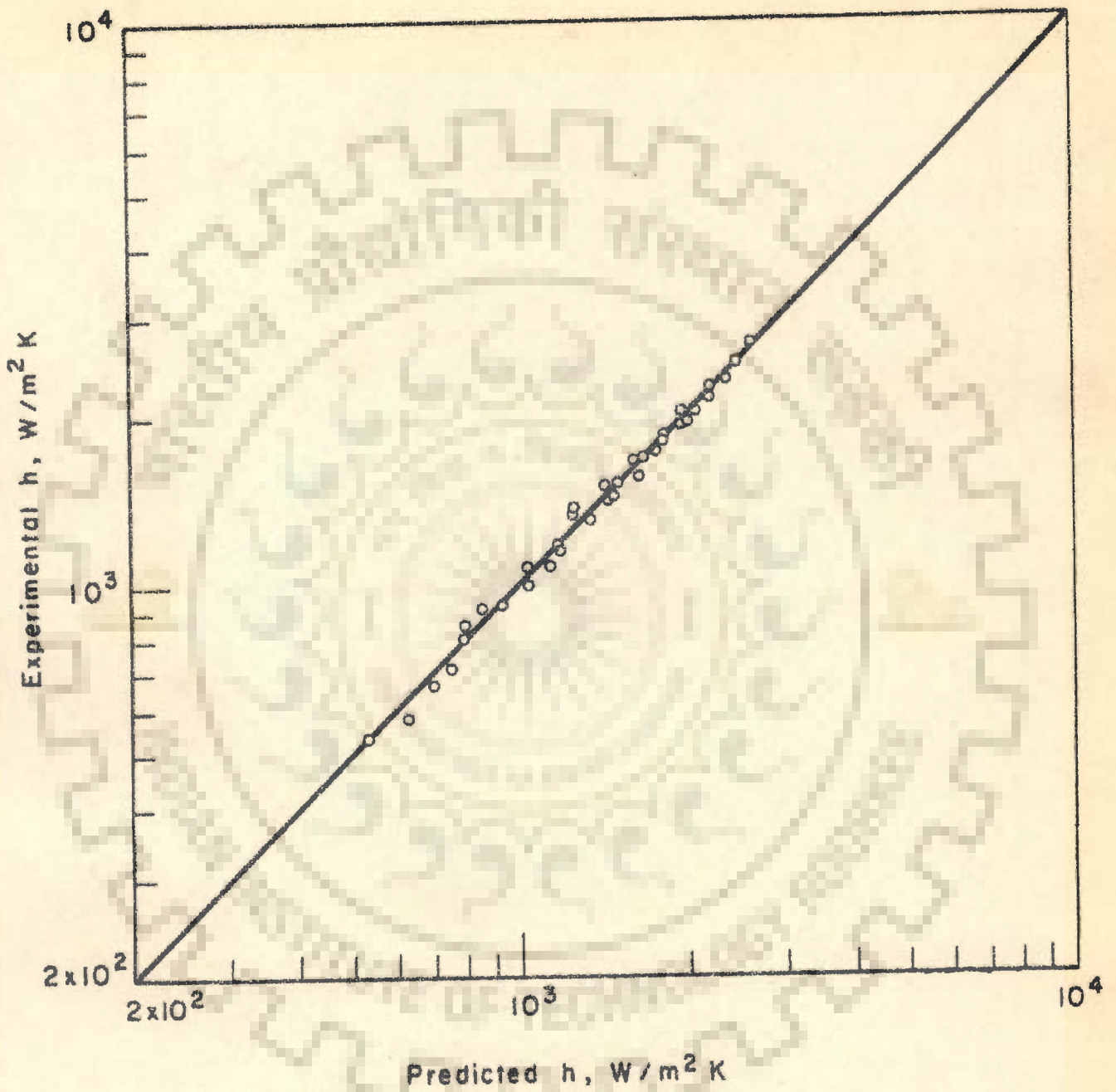


Fig. 6-23 Present experimental data for methanol compared with the present analysis, Eqs (6.3d & 6.4)

by a single line. The properties of these regression lines are given in Table 6.8 . Inspection of this Table reveals that the coefficient of correlation is the best in case of power function fit. Thus the following form of power function relates all the data points:

$$\frac{M}{M_1} = 0.95831645 (P/P_1)^{-0.3997825} \quad (6.5)$$

Table 6.8 Properties of regression lines for  $M/M_1$  and  $P/P_1$  for all the fluids

Regression line	A	B	Coefficient of correlation
Hyperbolic	1.0360125E+00	-8.9943040E-02	0.9185
Power function	9.5831645E-01	-3.997825E-01	0.9689
Semi log	9.0278652E-01	-5.8567074E-01	0.94235

Figure 6.24 shows a plot between the average experimental values of  $M/M_1$  of all the fluids investigated and  $P/P_1$ . The solid line is the recommended equation, Eq.(6.5). From this figure it is seen that the agreement is excellent suggesting that Eq.(6.5) represents a generalised correlation for determining  $M/M_1$  unlike Eq.(6.3).

It is thus seen that  $M/M_1$  depends upon  $P/P_1$  only as envisioned in Eq(5.25). This seems to be possible only if  $M$  is a multiplicative function of pressure and surface-liquid combination. This is in conformity to the speculations made in Chapter 5 [cf. Eq.(5.23) ]. The fact that  $M/M_1$  does depend on

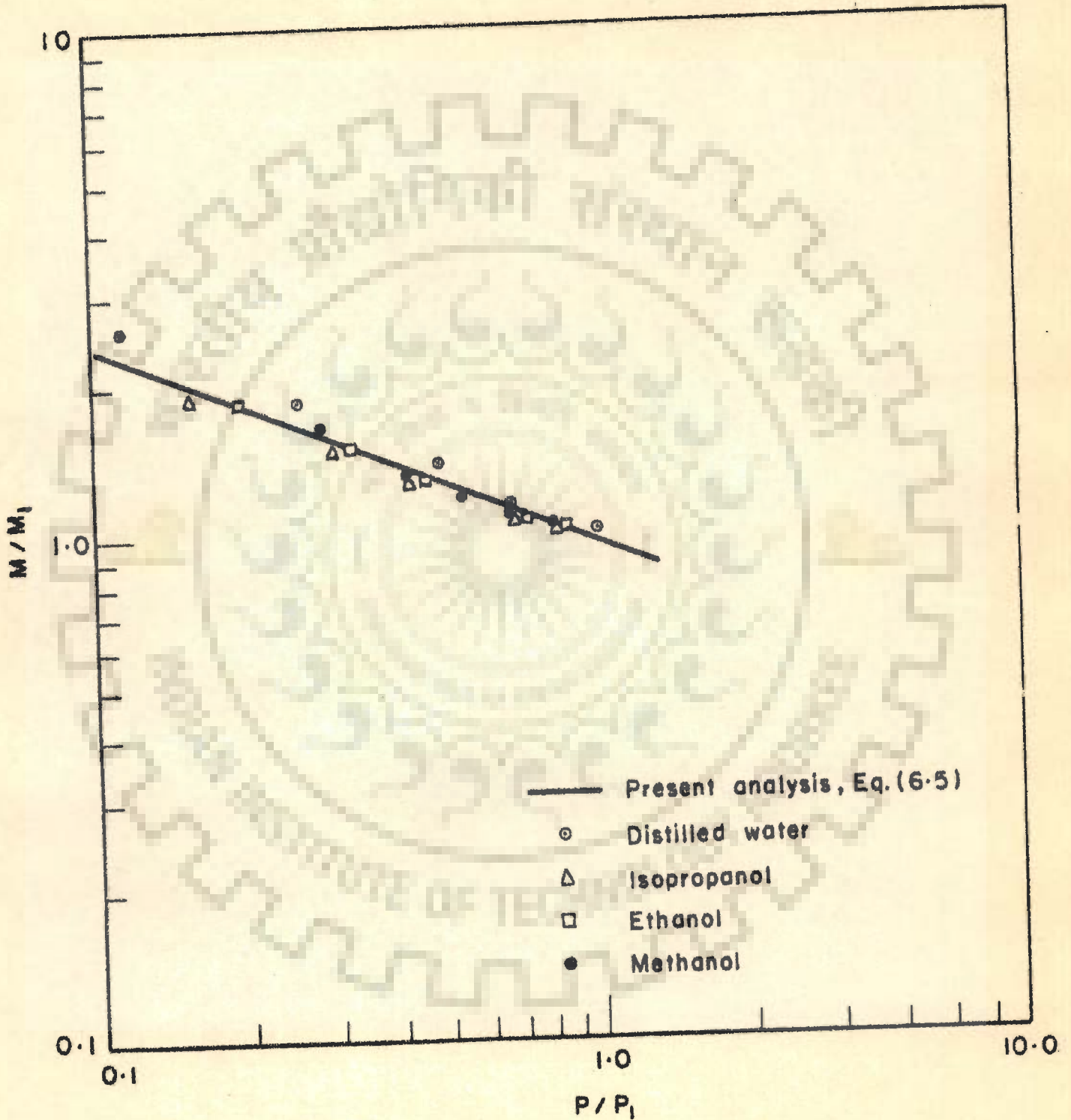


Fig. 6.24 Plot between  $M/M_1$  vs  $P/P_1$

pressure only and not on surface-liquid combination is scrutinized by comparing the experimental data of other investigators on different heating surfaces with the predicted values from this analysis in Section 6.11.

From the values of  $a (=0.3683)$ ,  $m (=2.33)$ , Eq.(6.5) and Eq.(5.24) the following equation results for  $h^*/h_1^*$  :

$$\frac{h^*}{h_1^*} = 0.95831645(P/P_1)^{-0.3997825} \left[ \left( \frac{\lambda}{\lambda_1} \right)^{2.5} \left( \frac{\rho}{\rho_{v1}} \right) \left( \frac{T_{sl}}{T_s} \right)^{1.5} \right. \\ \left. \left( \frac{\sigma_1}{\sigma} \right) \left( \frac{k/l}{k/l} \right)^{0.3} \left( \frac{q}{q_1} \right)^{0.3} \left( \frac{C_{\ell 1}}{C_{\ell}} \right)^{1.2} \right]^{2.33} \times \left[ \frac{f}{f_1} \right]^{0.3683} \quad (6.6)$$

Subscript '1' denotes the values corresponding to normal boiling point.

Figure 6.25 shows a comparison between the predicted values of  $h^*/h_1^*$  from the proposed correlation, Eq.(6.6) and the experimental values of the present investigation. The data points show an excellent agreement with a maximum deviation of  $\pm 10$  per cent.

Further, Eq.(6.6) can be used to calculate the absolute values of heat transfer coefficient for a surface-liquid combination at subatmospheric pressures, without resort to experiment, if the value of heat transfer coefficient

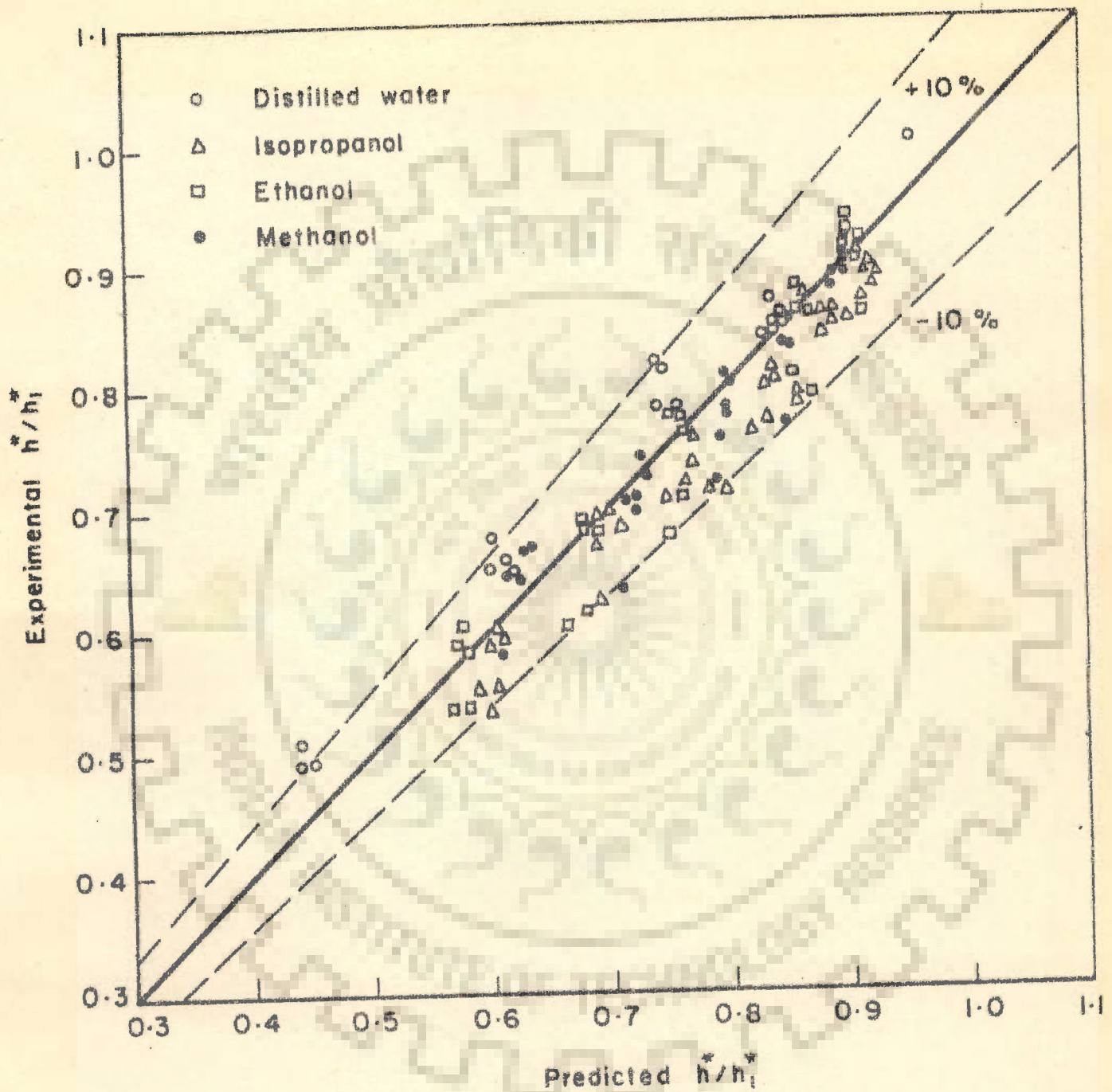


Fig. 6.25 Present experimental data compared with the present analysis, Eq (6.6)

at normal boiling point is known for that surface-liquid combination.

#### 6.11 COMPARISON OF PREDICTED HEAT TRANSFER COEFFICIENTS FROM PRESENT ANALYSIS WITH EXISTING DATA

To bolster the validity of the present analytical analysis, Eq.(6.6) the experimental data of Cryder and Finalborgo [5] for water, methanol and carbon tetrachloride on brass tube, and Raben et al [9] for water on the top end of a vertical cylindrical copper rod of high purity, at subatmospheric pressures were employed.

The comparison between the experimental values of  $(h^*/h_1^*)$  and the predicted ones from the present analysis is made in Figure 6.26. It is seen that the analysis is consistent with the experimental data obtained on different surface-liquid combinations. It also concludes that  $h^*/h_1^*$  does not depend on surface-liquid combination implying that  $M/M_1$  is independent of the surface-liquid combination.

The above conclusion is in conformity with the results of Cryder and Finalborgo [5] that the ratio  $h^*/h_1^*$  is relatively independent of the arrangement and composition of the heating element. Further, Bonilla and Perry [10] have also observed that the boiling surface does not change the ratios of the coefficients obtained at different pressures.

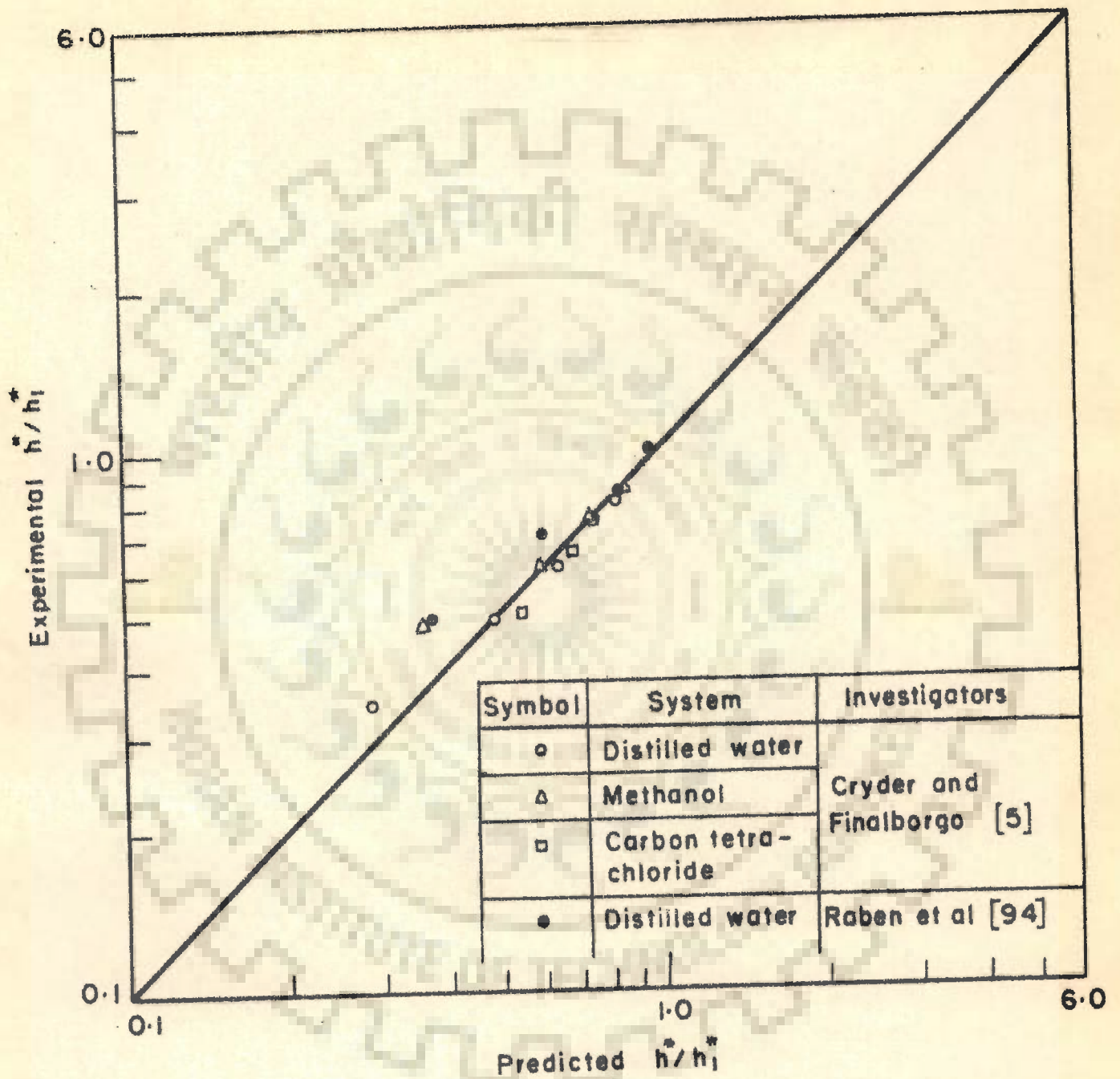


Fig. 6-26 Existing experimental data compared with the present analysis, Eq (6-6)

## 6.12 COMPARISON BETWEEN PREDICTED HEAT TRANSFER COEFFICIENTS FROM VARIOUS CORRELATIONS AND EXPERIMENTAL VALUES OF PRESENT STUDY

A comprehensive literature review in Chapter 2 shows that a large number of correlations have been proposed for heat transfer in nucleate pool boiling. Table 2.6 lists the selected heat transfer correlations for comparing the experimental data of this study with the predictions from them. The criteria of their selection have already been described. For ready reference some of the pertinent points of these correlations [4], [33], [36], [39], [43] are as follows:

Jakob and Linke [4] correlation is a semitheoretical correlation based on the assumptions that there exists a linear relationship between the heat flux and number of active sites per unit area of the heating surface and product  $fD_b$  is a constant.

The correlations of Kutateladze [39] and Kichigin and Tobilevich [39] have been derived empirically by choosing pertinent groups which explain the phenomenon of nucleate pool boiling. One of the important groups included in these correlations is  $K_p$  which is a criterion for pressure term in boiling.

The correlation of Labuntsov [36] is also an empirical correlation. The essential features of the correlation is that it contains criterion for bubble break-off frequency along with Peclet number for boiling.



The Forster- Greif correlation [33] is a theoretical approach for wall heat flux determination based on vapour-liquid exchange mechanism.

Mikic and Rohsenow correlation [43] assumes that the main mechanism of heat transfer in nucleate boiling is transient heat conduction to, and subsequent replacement of, the superheated layer around boiling sites associated with bubble departure.

Figures 6.27 and 6.28 represent the comparison between the present experimental data and the predicted values from the Jakob and Linke correlation [4]. Observations from these plots reveal that the Jakob -Linke correlation underpredicts the value. This observation is not surprising because this correlation was recommended for the experimental data for pressures greater than one atmosphere, while the present experimental data pertain to subatmospheric pressures. Another important reason for this disagreement is attributable, probably, to the fact that their correlation assumed the product  $fD_b$  to be a constant. But the recent studies [45],[118] have shown that  $fD_b$  is not a constant value and depends both upon heat flux and pressure.

Figures 6.29 and 6.30 are the plots which compare the experimental data of this study with the predictions from the Kutateladze correlation [39]. From these figures it is inferred that predicted values from the Kutateladze correlation are always lower than the experimental values. For methanol

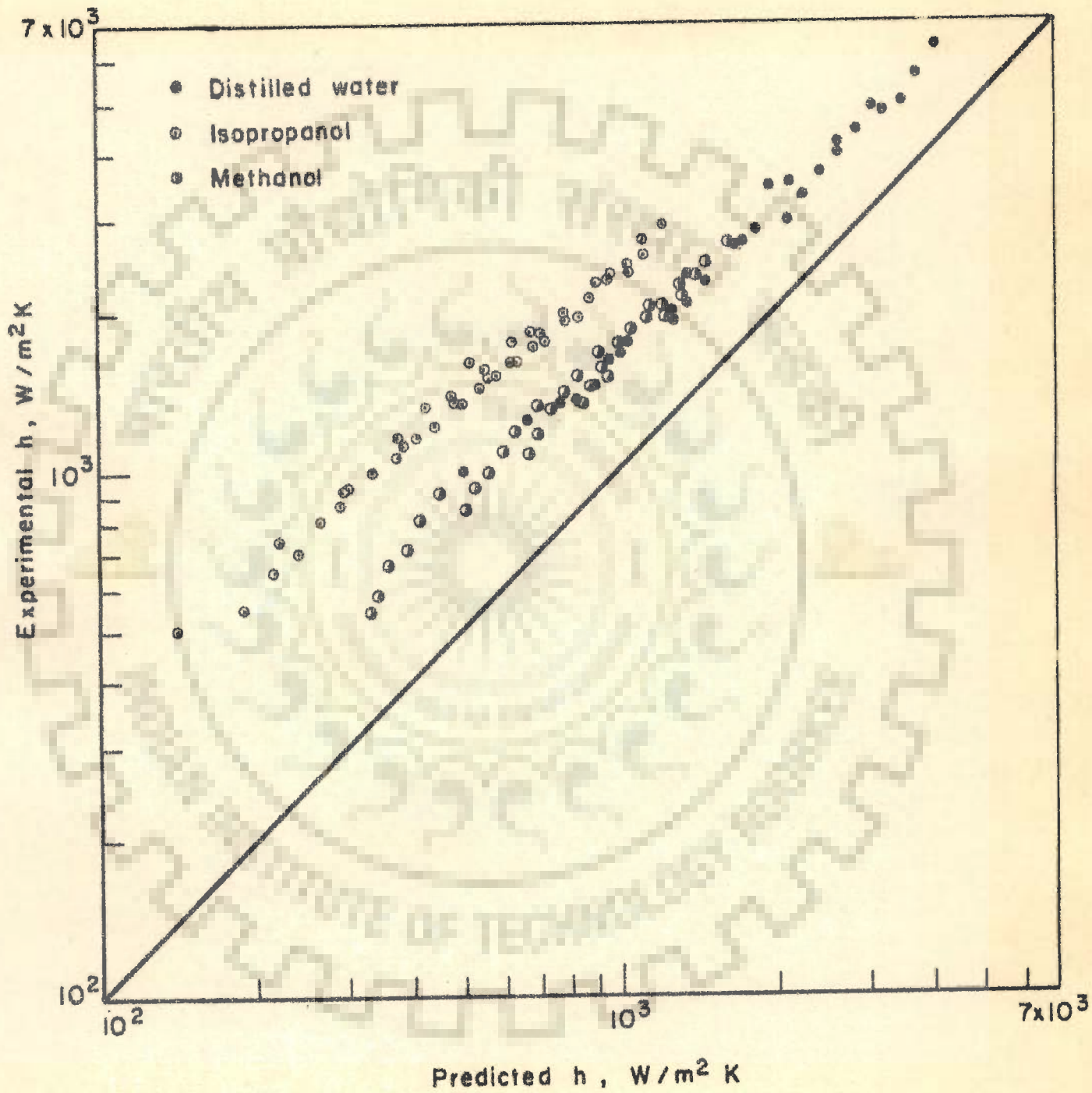


Fig. 6-27 Present experimental data compared with predictions from the Jakob & Linke correlation [4]

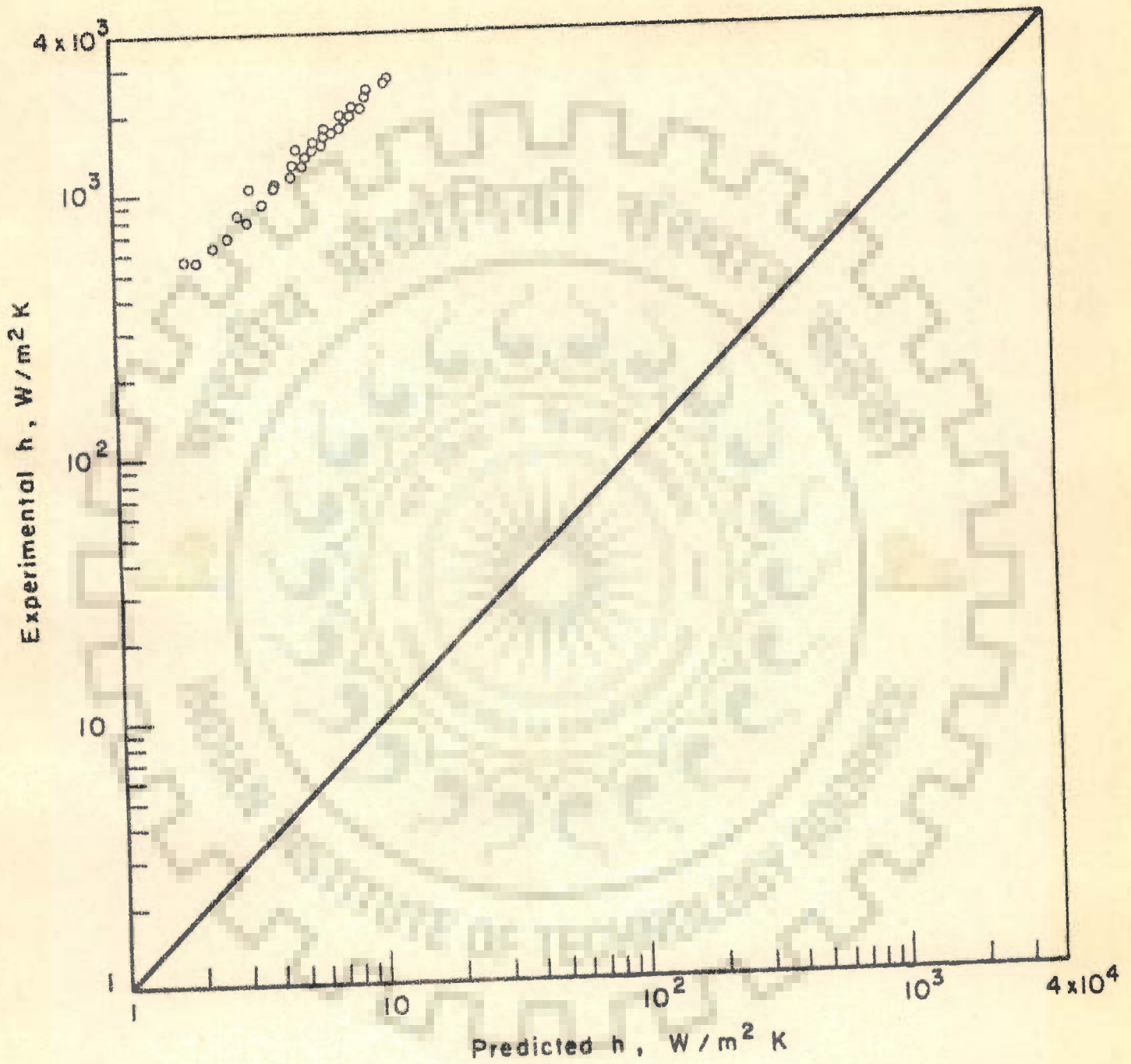


Fig. 6.28 Present experimental data for ethanol compared with predictions from the Jakob & Linke correlation [4]

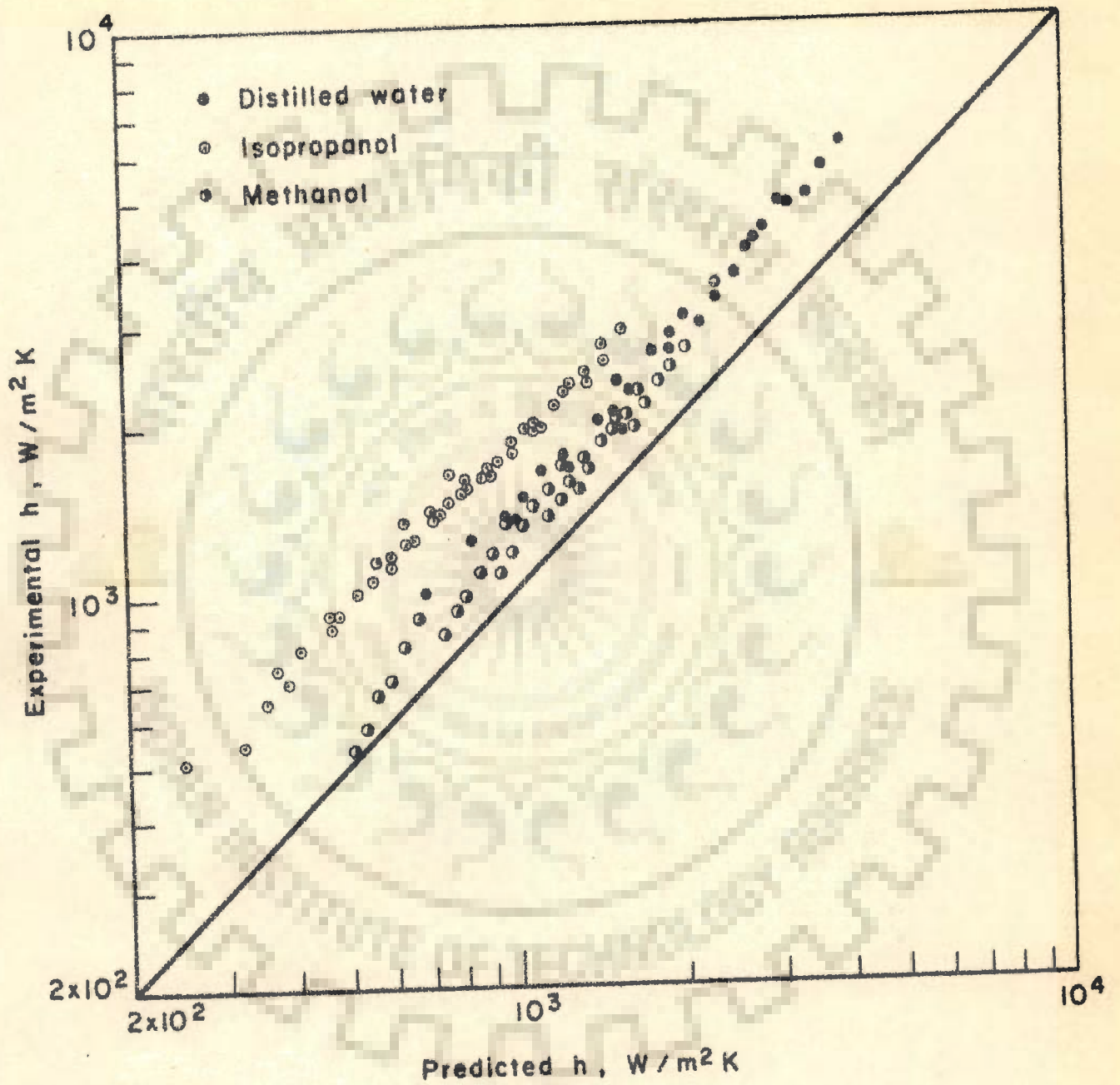


Fig. 6.29 Present experimental data compared with predictions from the Kutateladze correlation [39]

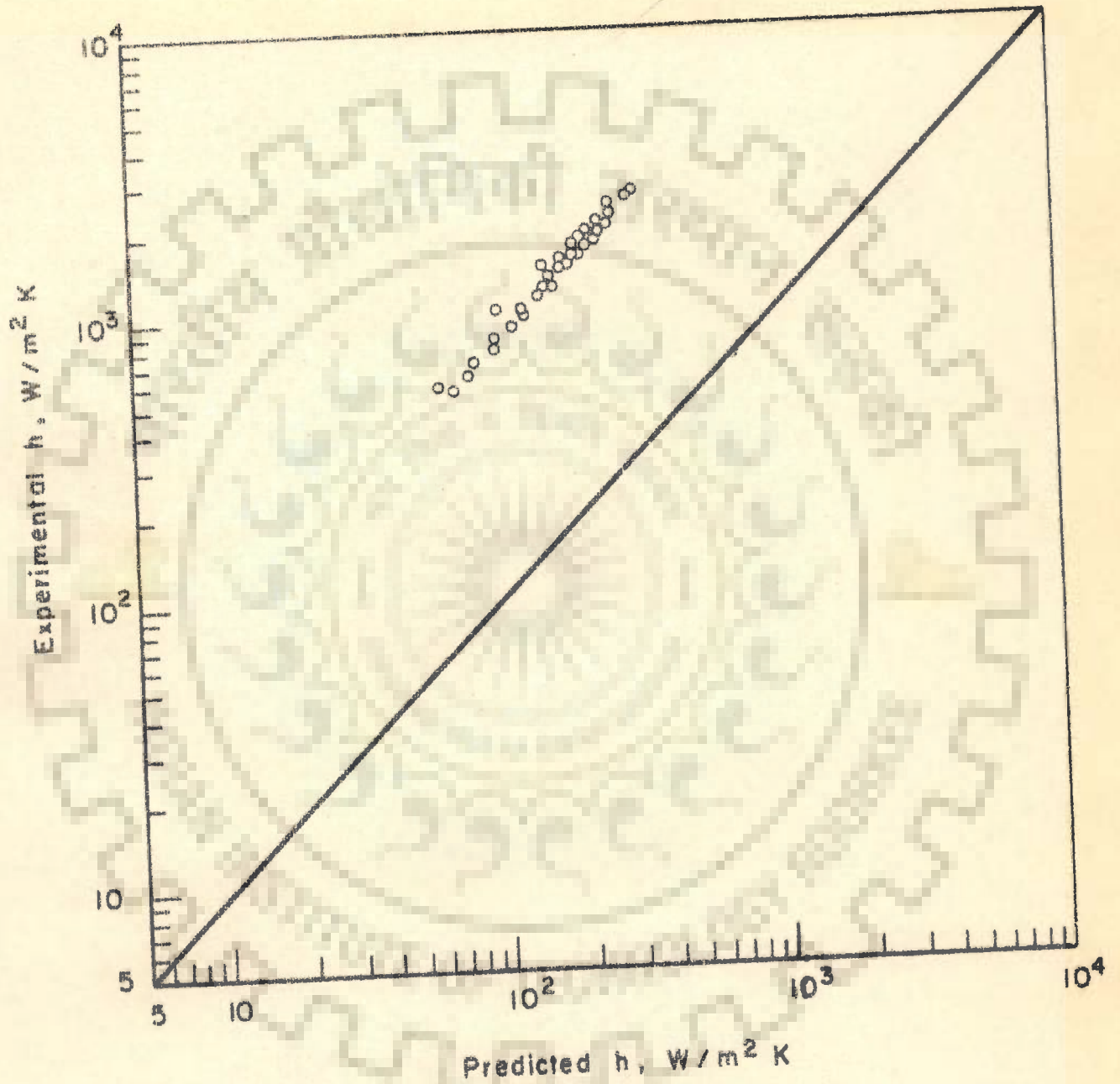


Fig. 6-30 Present experimental data for ethanol compared with predictions from the Kutateladze correlation [39]

the behaviour is same as for other liquids, however, the deviation is not much. Deviation is quite appreciable for the data of ethanol.

Figures 6.31 and 6.32 compare the present experimental data with the predictions from the Kichigen and Tobilevich correlation [39]. The agreement is good for the data of methanol, fairly well for the data of distilled water and isopropanol and poor for ethanol.

Figures 6.33 and 6.34 exhibit the comparison between experimental values of heat transfer coefficient and those calculated from the Labuntsov correlation [36]. The agreement is quite good for the experimental data for isopropanol and fairly well for distilled water. The correlation overpredicts the data of methanol and underpredicts the data of ethanol.

Based on the observations as above the following points can be concluded:

1. The correlations due to Kutateladze, and Kichigen and Tobilevich appear to correlate the experimental data for methanol well.
2. The Labuntsov correlation is found to well-correlate the data for isopropanol and it correlates the data for distilled water fairly well.
3. All the correlations are poor predictors for the data of ethanol. Also, they underpredict the values of heat transfer coefficient.

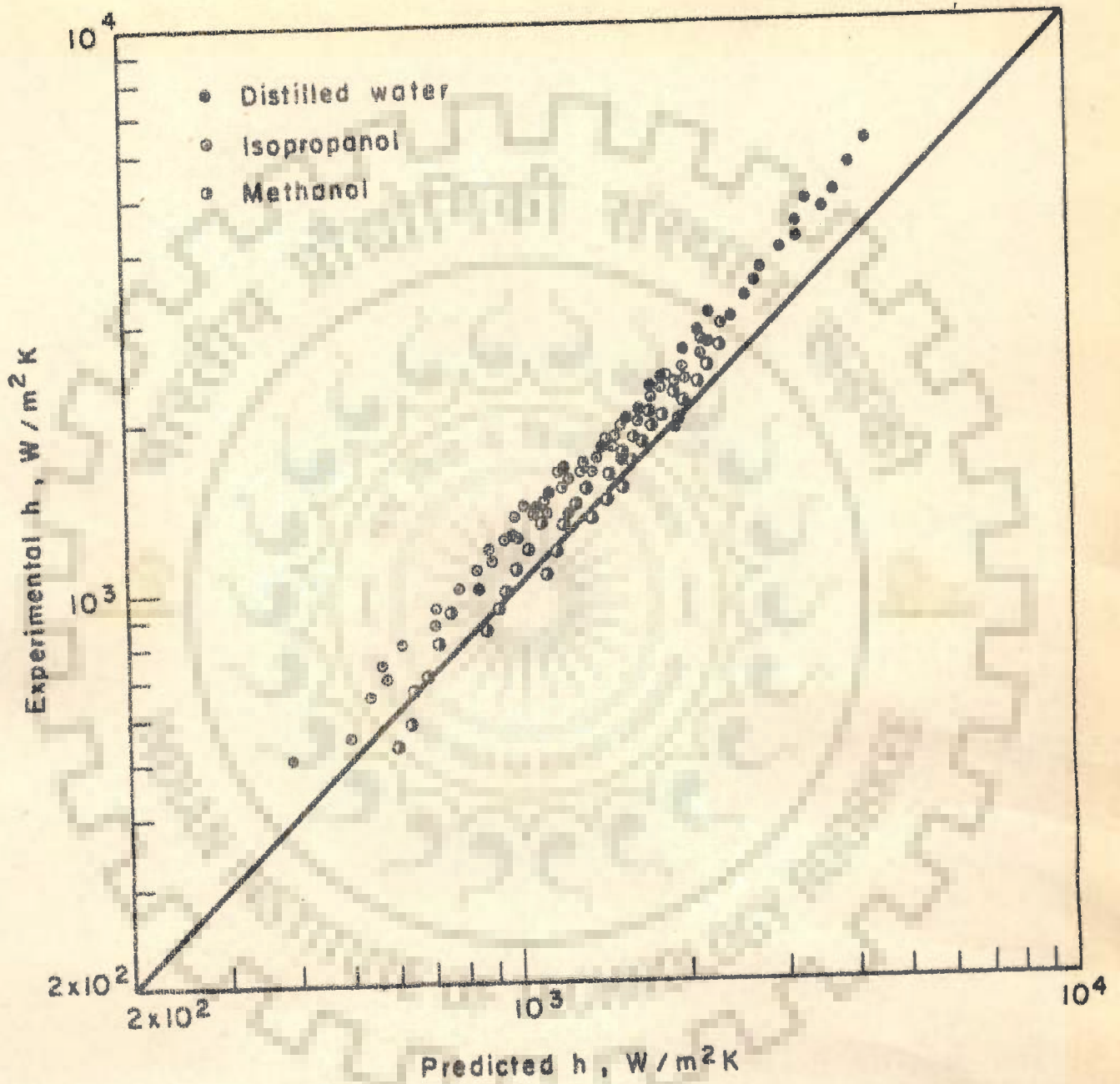


Fig. 6-31 Present experimental data compared with predictions from the Kichigen & Tobilevich correlation [39]

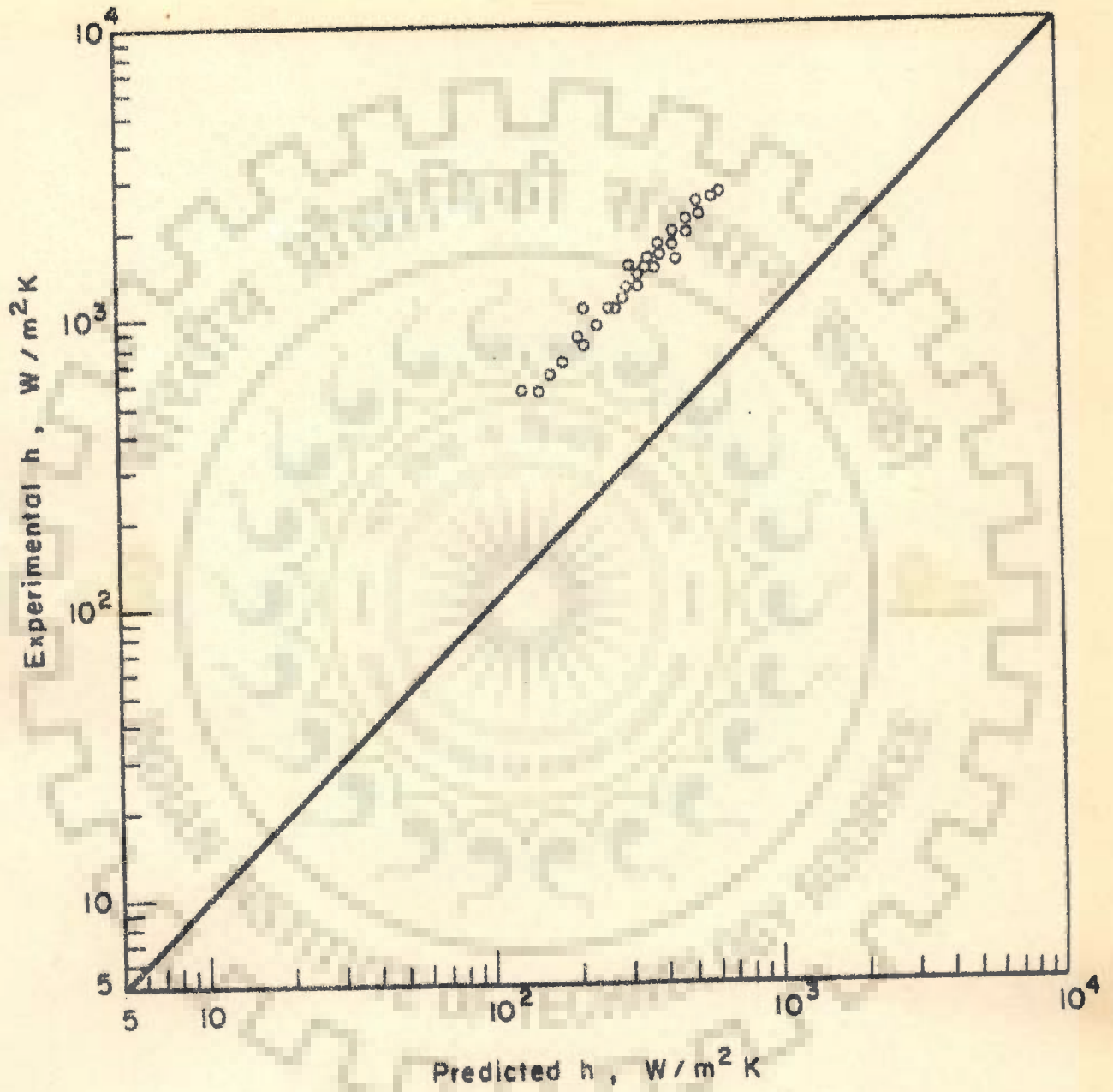


Fig. 6-32 Present experimental data for ethanol compared with predictions from the Kichigen & Tobilevich correlation [39]



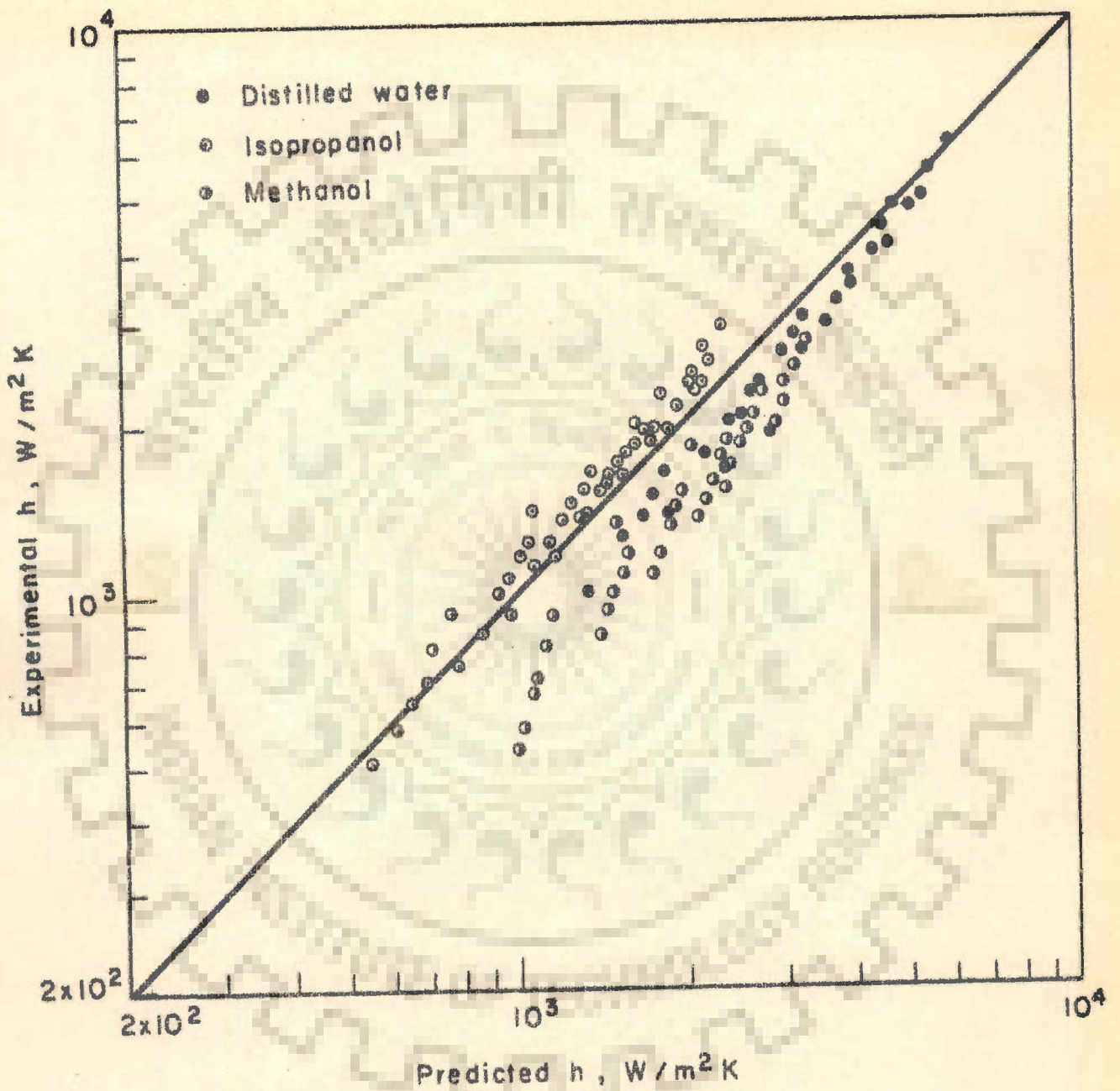


Fig. 6-33 Present experimental data compared with predictions from the Labuntsov correlation [36]

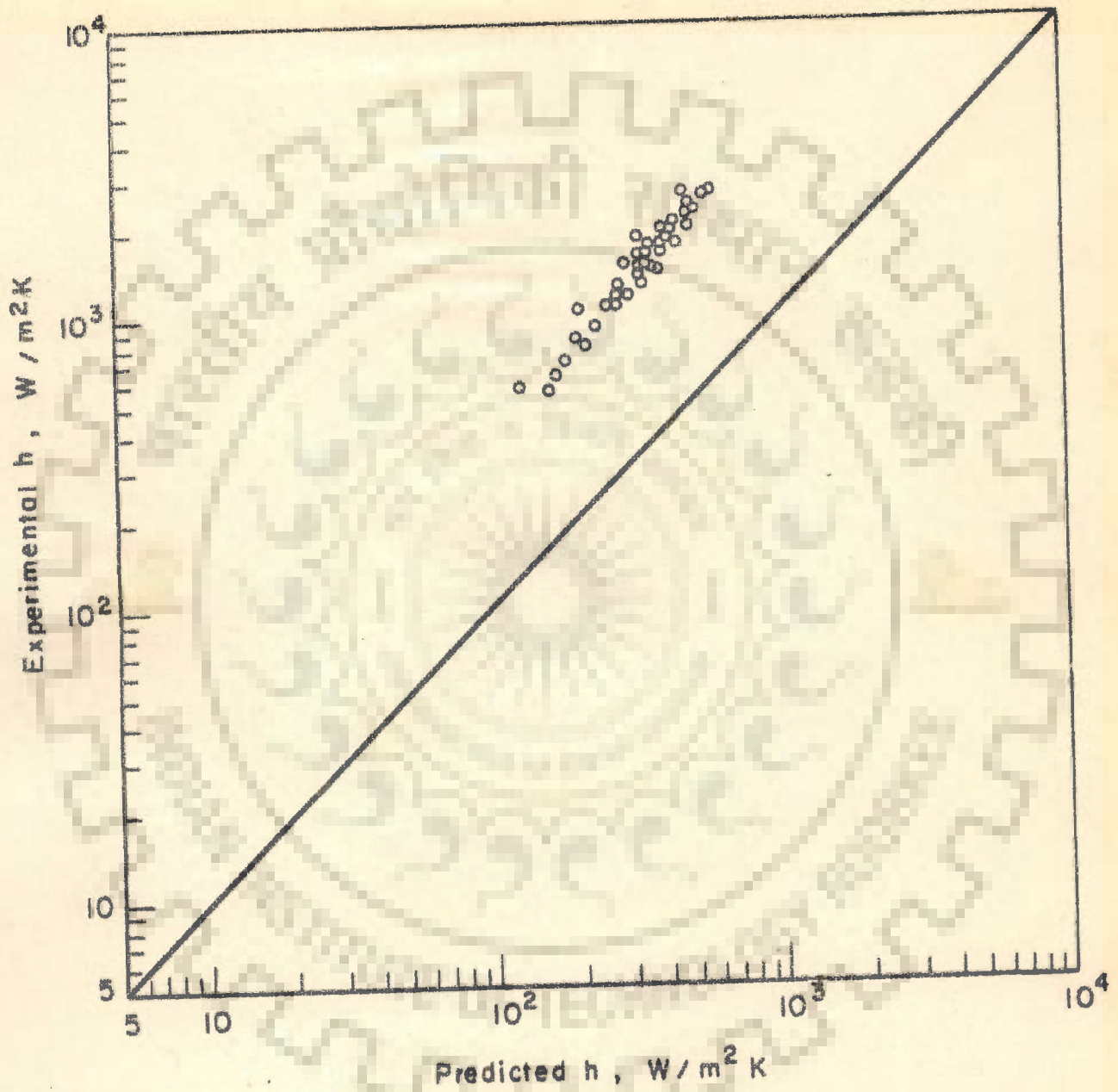


Fig. 6-34 Present experimental data for ethanol compared with predictions from the Labuntsov correlation [36]

Finally it would be concluded that none of these correlations is a good predictor for all the present experimental data at subatmospheric pressures and therefore, they do not possess general applicability for liquids differing in their physico-thermal properties.

Figures 6.35 and 6.36 represent the comparison between the present experimental values of heat flux and the predicted from the Forster and Greif correlation [33]. An inspection of these figures shows that the correlation overpredicts the value of heat flux for distilled water, isopropanol and methanol while it underpredicts the heat flux value for ethanol. These figures also reveal that their correlation seems to predict heat flux in its dependence on pressure and boiling fluid. The pressure effect is more pronounced for ethanol as shown by Figure 6.36. Thus their correlation does not possess the general applicability for the conditions employed in the present investigation.

Figures 6.37 and 6.38 represent the comparison between the present experimental data and the calculated values from the Mikic and Rohsenow correlation [43]. Abscissa  $\Delta T$  has been defined in Eq(2.44). It appears from these figures that this correlation satisfactorily correlates present experimental data for all the four fluids.

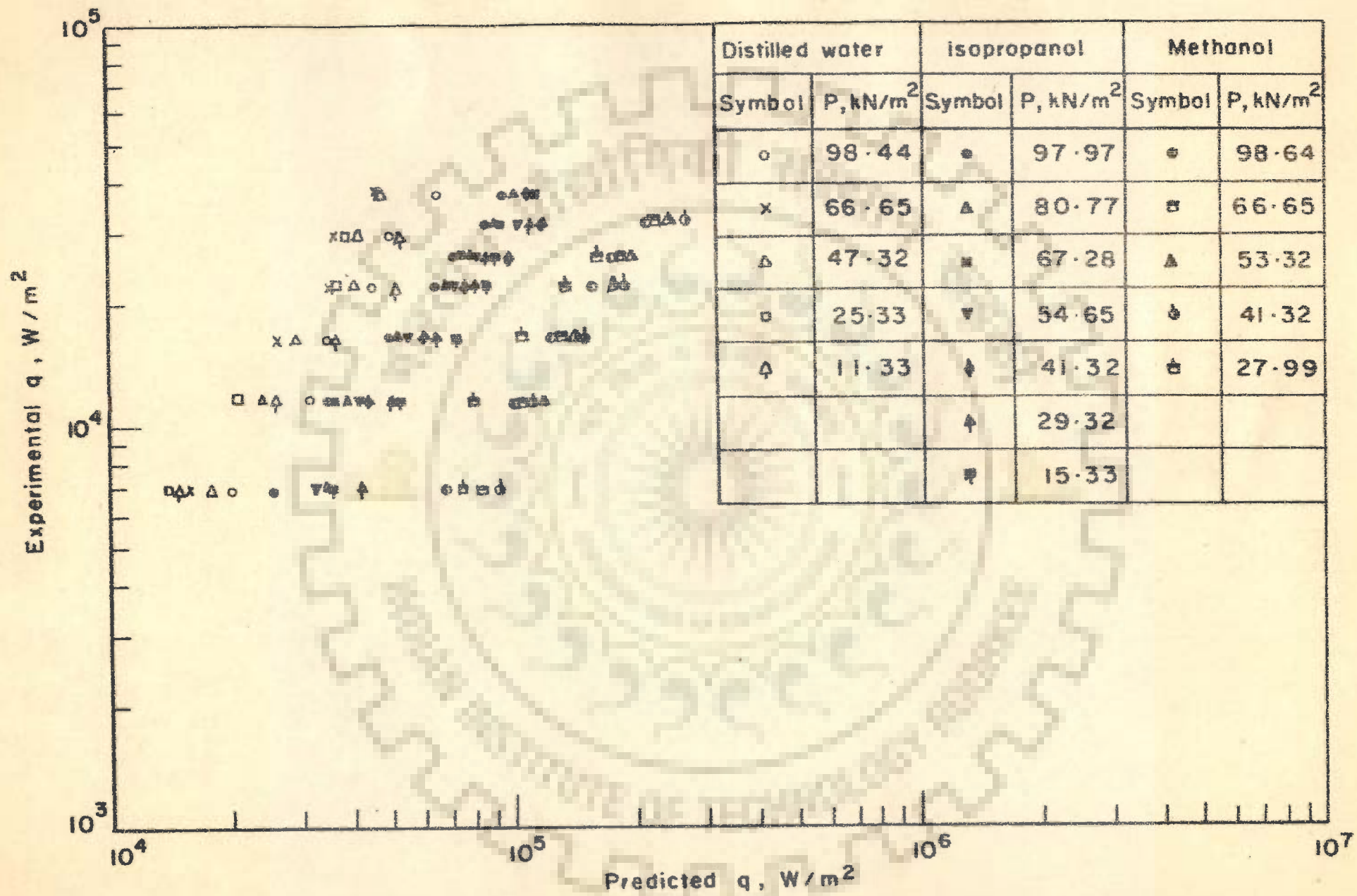


Fig. 6-35 Present experimental data compared with predictions from the Forster and Greif correlation [33]

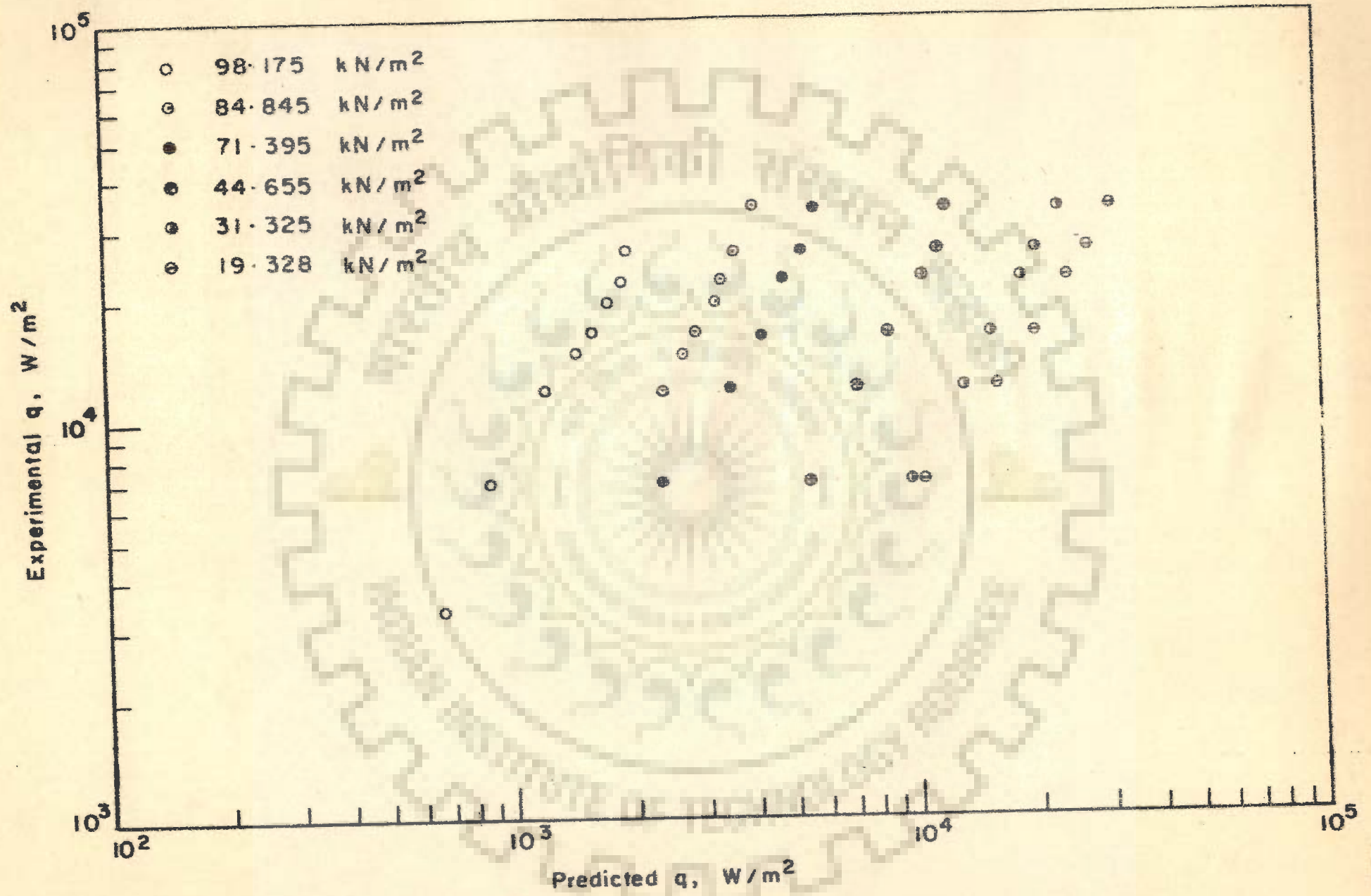


Fig. 6-36 Present experimental data for ethanol compared with predictions from the Forster and Greif correlation [33]

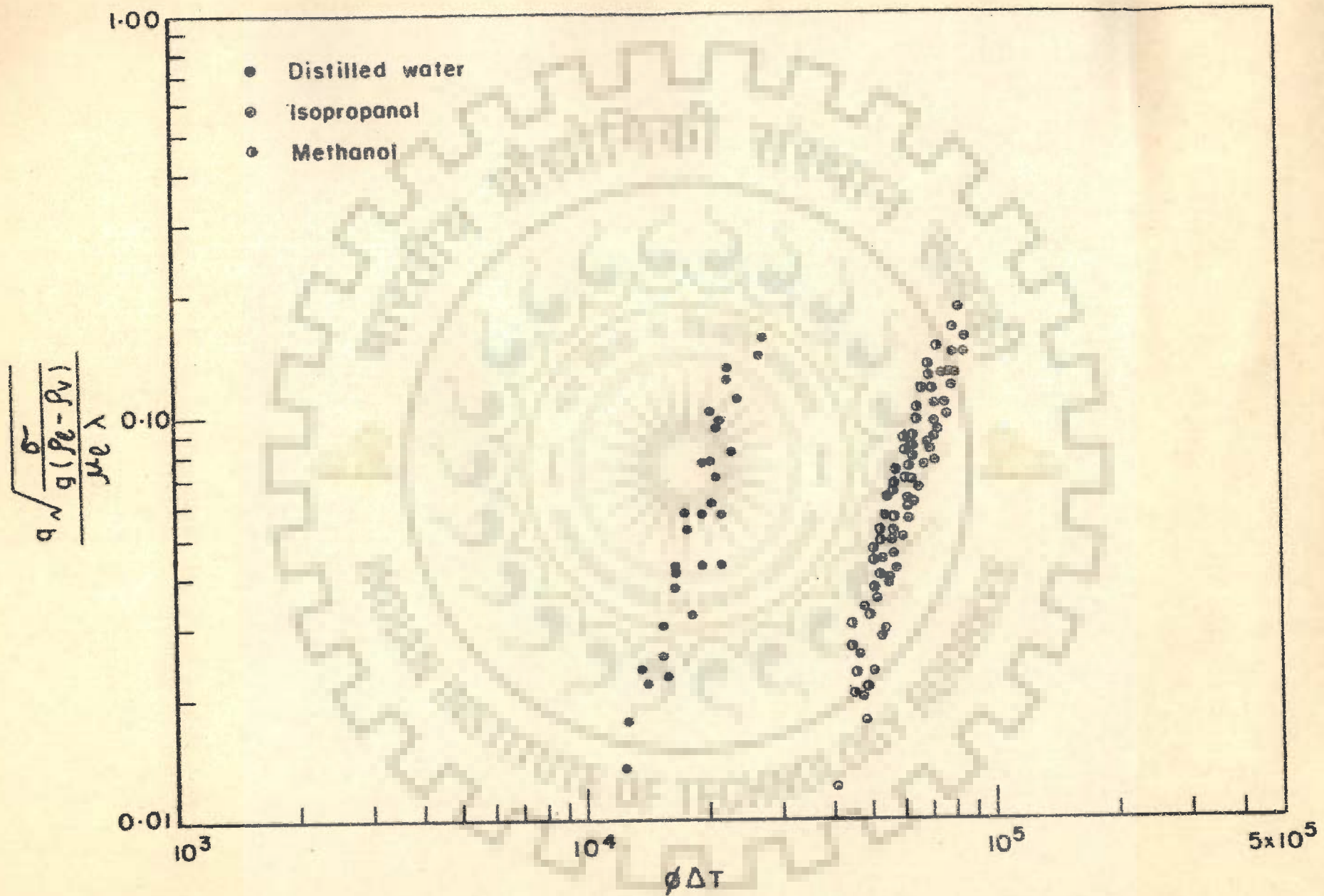


Fig. 6-37 Present experimental data compared with predictions from the Mikic and Rohsenow correlation [43]

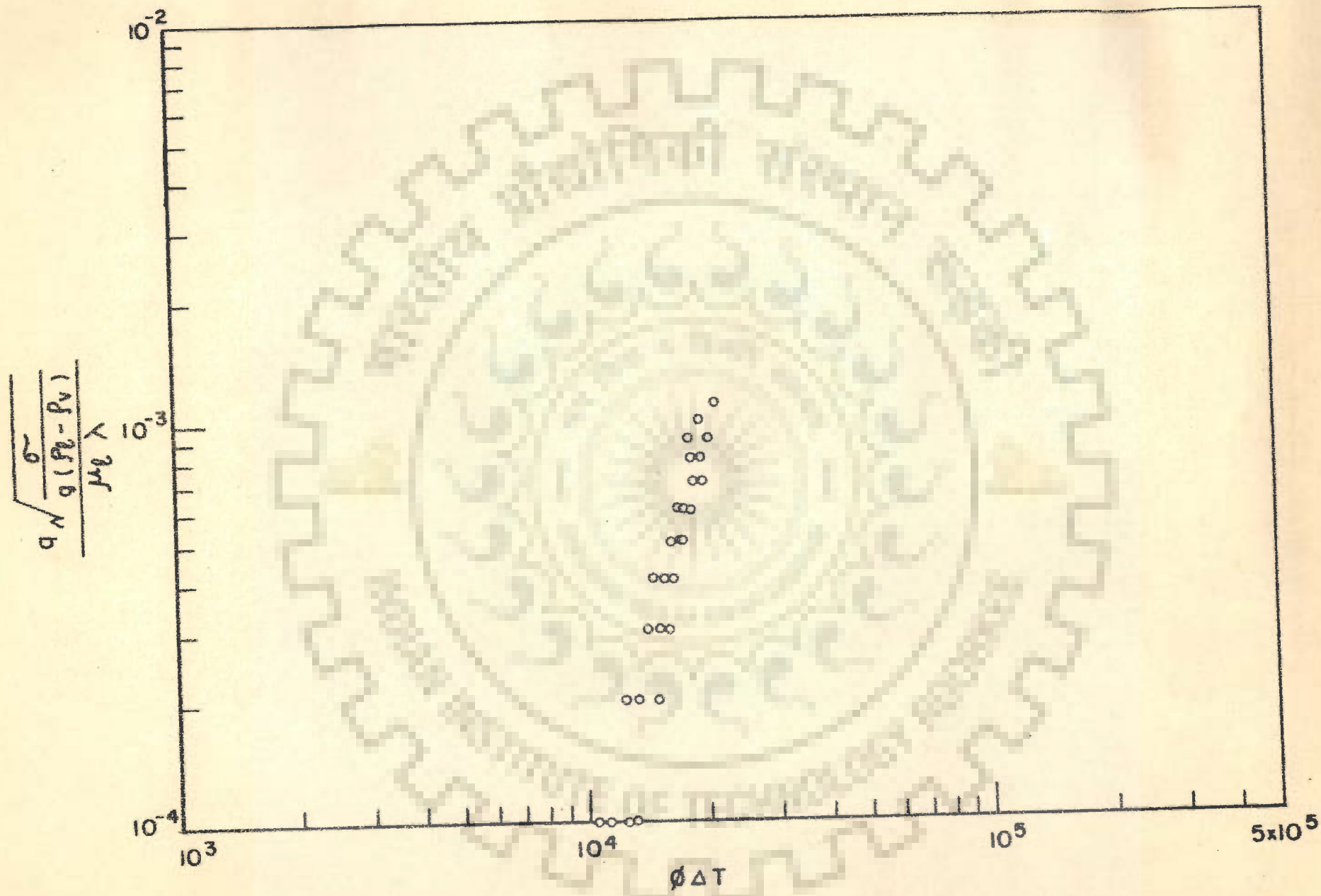


Fig. 6-38 Present experimental data of ethanol compared with predictions from the Mikic and Rohsenow correlation [43]

## CHAPTER 7

### CONCLUSIONS AND RECOMMENDATIONS

The main conclusions drawn from the present study are as follows:

1. The present investigation has developed a new analytical model for heat transfer in nucleate pool boiling by using adequate equations for nucleation sites [53], bubble growth [66], bubble size [95] and bubble emission frequency through heating surface characteristics. The model is represented by equation, Eq. ( 5.22). This equation provides an useful procedure for the computation of absolute values of boiling heat transfer coefficient from the knowledge of wall heat flux, system pressure, and pertinent physico-thermal properties of boiling fluids through the known surface characteristics and known value of exponent  $a$ . The value of  $a$  can be determined if  $nf$  is known as recommended by Wiebe and Judd [54]. But for industrial surfaces it is highly improbable to obtain satisfactory generalised analytical equations for the surface characteristics as represented by constant  $M$  and for the values of  $nf$ . However, it is possible to have the constant  $M$  and exponent  $a$  determined empirically. For the surface characteristics used in the present investigation a procedure has been devised to determine the values of constant  $M$  as function of pressure and



the boiling fluids, and are represented by the set of equations, Eq. (6.3). The value of  $a$  is found to be independent of system parameters and has been evaluated as 0.3683. Finally, the model is represented by Eq. (6.4).

In order to obviate the unpredictable quantities built in constant  $M$ , and to provide a procedure for checking the consistency of experimental data from different heating surfaces used by different investigators, Eq.(5.22), has been transformed to Eq.(5.24). This equation incorporates the effects of wall heat flux, pertinent physico-thermal properties of boiling fluids and  $M/M_1$  on  $h^*/h_1^*$ . Further the values of  $M/M_1$  are found to depend on system pressure only and they are independent of boiling fluids [cf. Eq.(6.5)]. The final form of Eq. (5.24) is represented by Eq. (6.6). The agreement between the experimental data of present investigation and the predicted values from the proposed analysis, Eq. (6.6) is excellent within  $\pm 10$  per cent. In addition, this equation is consistent with the experimental data of Cryder and Finalborgo [5], Raben, Beaubouef and Commerford [94] as well, which were obtained from the heating surfaces and fluids differing from each other and from that used in the present investigation. As the resultant equation, Eq. (6.6) of the present analysis is found to well-correlate the experimental data of different investigators for different conditions of heating surfaces and fluids, a considerable confidence is placed in this new analysis of heat transfer in nucleat pool boiling.

Another usefulness of this analysis is that it provides a design procedure for determining the absolute values of heat transfer coefficient at subatmospheric pressures, without resort to experimentation, from the knowledge of heat transfer coefficient at normal boiling point.

An excellent agreement between the predicted values of heat transfer coefficient and those of present investigation and of Cryder and Finalborgo [5], Raben, Beaubouef and Commerford [94] corroborates implicitly the validity of the governing equations: Eq. (5.3) for nucleation sites, Eqs (5.8 & 5.16) for bubble growth rate, and Eq. (5.9) for bubble size for atmospheric and subatmospheric pressures. Since these governing equations are for atmospheric and subatmospheric pressures, these correlation might not correlate the boiling data for higher pressure. Therefore, a care should be exercised that the resultant equation of the present analysis, Eq. (6.6) should not be used for the system pressures greater than one atmosphere.

2. As envisioned in the present investigation, a mathematical analysis consistent with the requirements of heat transfer dissipated from the heating surfaces to the boiling fluids would include the consideration of bubble dynamics on the heating surface through surface characteristics. Adequate governing equations for nucleate sites, bubble growth, bubble size and frequency should be selected in accordance with the system parameters like heat flux,

pressure and others.

3. The boiling heat transfer coefficient from the heating surface was found to vary circumferentially. It seems believable that such variation is inevitable for heating surfaces of large diameters.

4. The predictions of frequency from proposed equations, Eqs.(5.15 and 5.19) compare fairly well with the experimental values measured by Cole [45].

5. The Alad'ev equation for wall superheat was checked using experimental data. The equation was found to be consistent with the experimental data for boiling distilled water. However, the experimental data for isopropanol, ethanol and methanol could not be correlated by this equation. The constant of the Alad'ev equation was modified to fit the experimental data for the latter three liquids investigated. The modified constant was found to depend on the nature of boiling liquid to which heat was dissipated from the heating surface.

6. The average values of experimental heat transfer coefficient showed a good agreement with the existing experimental data.

7. New experimental data have been generated for subatmospheric pressures for the boiling of distilled water, isopropanol, ethanol and methanol.

As a result of the present investigation the following points emerge for future studies:

1. As indicated in the present study the proposed mathematical analysis is applicable for a limited range of parameters. In order to extend the range of applicability of the present analysis it is necessary to test it with the experimental data which are on the border lines of the tested parameters.

2. It seems that sufficient information does not exist for the prediction of wall superheat during nucleate pool boiling. Thus further research efforts are due for a generalised equation which can relate the wall superheat with the relevant parameters which are directly and easily measurable.

3. There is also a need to further the experimental programs to measure the wall temperature circumferentially at more number of points. These data would provide a more detailed thermal behaviour of the heating surfaces.

## A P P E N D I X    A

### DETERMINATION OF AVERAGE WALL TEMPERATURE    USING MECHANICAL QUADRATURE    METHOD

With non-symmetrical boiling conditions around the circumference of a large diameter tube, immersed in a pool of boiling fluid, the circumferential variation in tube wall temperature might exist. In the present investigation, with tube diameter equal to 70 mm, the circumferential variation in wall temperature was observed. Numerical integration (mechanical quadrature) has been used for determining average wall temperature of heating surface. The problem of numerical integration has been solved by representing the integrand by an interpolation formula and then integrating it between the desired limits.

Let  $T = f(\theta)$  denote a function which represents the values of temperature along the circumference. Let  $T_0, T_1, T_2, \dots, T_n$  be the values of the function  $T$  at equidistant values of  $\theta_0, \theta_1, \theta_2, \dots, \theta_n$  of the independent variable  $\theta$ .

From Newton's interpolation formula the following relationship is derived:

$$d\theta = h du$$

where,  $u = \frac{\theta - \theta_0}{h}$  and  $h$  is the small interval  $\Delta\theta$ .

Integration of Newton's formula over  $n$  equidistant intervals of width  $h(= \Delta\theta)$  leads to the following:

$$\int_{\theta_0}^{\theta_0 + nh} T d\theta = h \int_0^n \left[ T_0 + u \Delta T_0 + \frac{u(u-1)}{2!} \Delta^2 T_0 + \dots \right] du \quad (\text{A.1})$$

or

$$\int_{\theta_0}^{\theta_0 + nh} T d\theta = h \left[ nT_0 + \frac{n^2}{2} \Delta T_0 + \left( \frac{n^3}{3} - \frac{n^2}{2} \right) \frac{\Delta^2 T_0}{2} + \dots \right] \quad (\text{A.2})$$

Equation (A.2) is the general form of quadrature formula for equidistant ordinates.

In the present investigation, three thermocouples, evenly stationed, at a regular interval of  $\pi/2$ , were employed to record the circumferential variation in the heating surface temperature. Figure 3.7 shows locations of these thermocouples at the side, at the top and at the bottom of the heating surface. The temperature at  $a'$  was not measured since it is equal to temperature at  $a$ , due to the symmetry of boiling conditions about the horizontal mid-plane  $a-a'$ . Therefore, with available three values two step lengths have been considered. Putting  $n = 2$ , and neglecting all differences above the second (there can be no difference higher than the second, with the available three values), equation (A-2) assumes the form :

$$\int_{\theta_0}^{\theta_0 + 2h} T d\theta = h \left[ 2T_0 + 2 \Delta T_0 + \left( \frac{8}{3} - 2 \right) \frac{\Delta^2 T_0}{2} \right] \quad (\text{A.3})$$

$$\left. \begin{aligned}
 \text{Where } \Delta T_o &= T_{w1} - T_{wo} \\
 \Delta^2 T_o &= \Delta T_{w1} - \Delta T_{wo} \\
 &= T_{w2} - 2T_{w1} + T_{wo}
 \end{aligned} \right\} \quad (A.4)$$

Inserting the values of  $\Delta T_o$  and  $\Delta^2 T_o$  from (A.4) in Eq.(A.3) the following is obtained:

$$\int_{\theta_o}^{\theta_o + 2h} T d\theta = \frac{h}{3} \left[ T_{wo} + 4T_{w1} + T_{w2} \right] \quad (A.5)$$

The average of the circumferential temperature is defined by the following equation:

$$\begin{aligned}
 \bar{T}_w &= \frac{1}{2\pi} \int_0^{2\pi} T d\theta \\
 &= \frac{1}{2\pi} \left[ \int_0^{\pi} T d\theta + \int_{\pi}^{2\pi} T d\theta \right] \quad (A.6)
 \end{aligned}$$

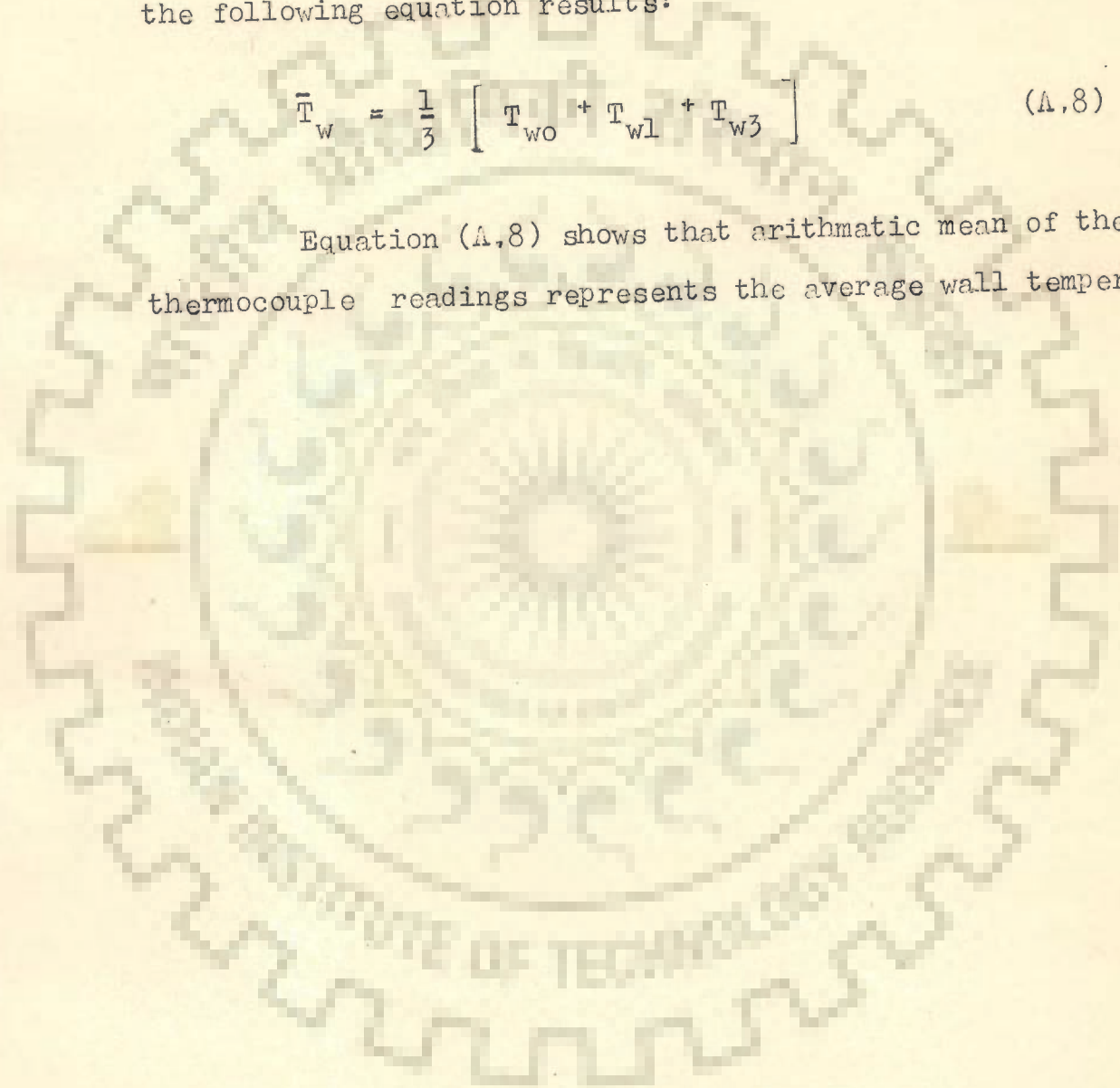
From Eqs. (A.5) and (A.6) and  $h (= \pi/2)$  the average value of  $T_w$  is obtained as follows:

$$\begin{aligned}
 \bar{T}_w &= \frac{1}{2\pi} \left[ \frac{\pi}{2} \cdot \frac{1}{3} (T_{wo} + 4T_{w1} + T_{w2}) + \frac{\pi}{2} \cdot \frac{1}{3} (T_{w2} + 4T_{w3} + T_{wo}) \right] \\
 &= \frac{1}{12} \left[ 2T_{wo} + 2T_{w2} + 4T_{w1} + 4T_{w3} \right] \quad (A.7)
 \end{aligned}$$

By symmetry  $T_{w2} = T_{w0}$  and using this in Eq. (A.7) the following equation results:

$$\bar{T}_w = \frac{1}{3} [T_{w0} + T_{w1} + T_{w3}] \quad (A.8)$$

Equation (A.8) shows that arithmetic mean of the thermocouple readings represents the average wall temperature.





## A P P E N D I X B

### TABULATION OF EXPERIMENTAL DATA

- Table B-1 Experimental Data of Heat Transfer to Boiling Distilled Water
- Table B-2 Experimental data of heat Transfer to Boiling Isopropanol
- Table B-3 Experimental Data of Heat Transfer to Boiling Ethanol
- Table B-4 Experimental Data of Heat Transfer to Boiling Methanol

#### Nomenclature

P	=	System Pressure
TS	=	Saturation Temperature
TW	=	Surface Temperature
TL	=	Liquid Temperature
CTW	=	Corrected Surface Temperature
DTW	=	Corrected Temperature Difference
AVGTW	=	Average corrected Surface Temperature
AVGDTW	=	Average Temperature Difference
H	=	Heat Transfer Coefficient
AVGH	=	Average Heat Transfer Coefficient

Scripts 0, 1 and 3 represent the side, top and bottom positions respectively, as shown in Figure 3.7.

TABLE B-1 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING DISTILLED WATER

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
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P=98.44 KN/SQ.N

TS=99.00 DEG.C

1	3870.22	TWO 103.900 TW1 102.725 TW3 105.575 AVGTW=103.512	TLO 99.200 TL1 99.625 TL3 100.050	CTWO 103.350 CTW1 102.175 CTW3 105.025 AVGDTW=3.892	DTWO 4.150 DTW1 2.550 DTW3 4.975	HO 1655.17 H1 2693.40 H3 1380.95 AVGH=1765.37
2	1175.72	TWO 105.600 TW1 103.875 TW3 107.375 AVGTW=104.677	TLO 99.350 TL1 99.750 TL3 100.400	CTWO 104.660 CTW1 102.935 CTW3 106.435 AVGDTW= 4.843	DTWO 5.310 DTW1 3.185 DTW3 6.035	HO 2213.80 H1 3690.74 H3 1947.92 AVGH=2427.19
3	16539.44	TWO 106.180 TW1 104.700 TW3 108.100 AVGTW=104.718	TLO 99.425 TL1 99.800 TL3 100.500	CTWO 104.000 CTW1 103.377 CTW3 106.777 AVGDTW= 5.095	DTWO 5.432 DTW1 3.577 DTW3 6.277	HO 3044.39 H1 4622.85 H3 2634.93 AVGH=3245.99
4	22137.40	TWO 107.050 TW1 105.975 TW3 109.600 AVGTW=105.772	TLO 99.625 TL1 99.800 TL3 100.650	CTWO 105.280 CTW1 104.205 CTW3 107.830 AVGDTW= 5.746	DTWO 5.655 DTW1 4.405 DTW3 7.180	HO 3914.50 H1 5025.25 H3 3083.20 AVGH=3852.21
5	29414.75	TWO 107.650 TW1 107.450 TW3 110.200 AVGTW=106.081	TLO 99.725 TL1 100.150 TL3 101.000	CTWO 105.298 CTW1 105.098 CTW3 107.848 AVGDTW= 5.789	DTWO 5.573 DTW1 4.948 DTW3 6.848	HO 5277.66 H1 5944.24 H3 4295.37 AVGH=5081.45
6	37709.92	TWO 109.000 TW1 109.225 TW3 111.950 AVGTW=107.043	TLO 100.050 TL1 100.500 TL3 101.250	CTWO 105.985 CTW1 106.210 CTW3 108.935 AVGDTW= 6.443	DTWO 5.935 DTW1 5.710 DTW3 7.685	HO 6353.52 H1 6603.86 H3 4906.95 AVGH=5852.55
7	41730.27	TWO 109.325 TW1 109.425 TW3 113.100 AVGTW=107.279	TLO 100.050 TL1 100.500 TL3 101.900	CTWO 105.988 CTW1 106.088 CTW3 109.763 AVGDTW= 6.463	DTWO 5.938 DTW1 5.588 DTW3 7.863	HO 7026.62 H1 7466.66 H3 5307.17 AVGH=6456.79

TABLE B-1 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING DISTILLED WATER

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	LIQUID TEMPERATURE DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
		p=66.65 KN/SQ.M			TS=88.50 DEG.C	
8	6870.23	TVO 93.350	TLO 88.250	CTWO 92.800	DTWO 4.550	HO 1509.69
		TV1 91.670	TL1 88.250	CTW1 91.120	DTW1 2.870	H1 2393.17
		TV3 96.250	TL3 89.250	CTW3 95.700	DTW3 6.450	H3 1065.03
		AVGTW= 93.207		AVGDTW= 4.624		AVGH=1485.75
9	11752.72	TVO 95.150	TLO 88.250	CTWO 94.210	DTWO 5.960	HO 1972.37
		TV1 92.700	TL1 88.250	CTW1 91.760	DTW1 3.510	H1 3349.03
		TW3 97.750	TL3 89.250	CTW3 96.810	DTW3 7.560	H3 1554.95
		AVGTW= 94.260		AVGDTW= 5.676		AVGH=2070.82
10	16539.44	TWO 95.750	TLO 88.250	CTWO 94.427	DTWO 6.177	HO 2677.26
		TW1 93.650	TL1 88.250	CTW1 92.327	DTW1 4.077	H1 4056.02
		TW3 98.000	TL3 89.550	CTW3 96.677	DTW3 7.127	H3 2320.43
		AVGTW= 94.477		AVGDTW= 5.794		AVGH=2854.37
11	22137.40	TWO 96.450	TLO 88.250	CTWO 94.680	DTWO 6.430	HO 3442.71
		TW1 94.950	TL1 88.250	CTW1 93.180	DTW1 4.930	H1 4490.14
		TW3 100.250	TL3 89.550	CTW3 98.480	DTW3 8.930	H3 2478.93
		AVGTW= 95.446		AVGDTW= 6.763		AVGH=3273.04
12	29414.75	TWO 96.450	TLO 88.250	CTWO 94.098	DTWO 5.848	HO 5029.51
		TW1 96.100	TL1 88.250	CTW1 93.748	DTW1 5.498	H1 5349.66
		TW3 100.750	TL3 89.550	CTW3 98.398	DTW3 8.848	H3 3324.29
		AVGTW= 95.415		AVGDTW= 6.731		AVGH=4369.54
13	37709.92	TWO 97.900	TLO 88.250	CTWO 94.885	DTWO 6.635	HO 5683.24
		TW1 97.650	TL1 88.250	CTW1 94.635	DTW1 6.385	H1 5905.76
		TW3 102.350	TL3 89.550	CTW3 99.335	DTW3 9.785	H3 3853.74
		AVGTW= 96.285		AVGDTW= 7.601		AVGH=4960.56

TABLE B-1 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING DISTILLED WATER

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
---------	------------------	---------------------------	--------------------------	--------------------	---------------------	-------------------------------

P=47.32 KN/SQ.M

TS=80.00 DEG.C

14	6870.22	TWO	85.400	TL0	79.900	CTWO	84.850	DTWO	4.950	HO	1387.71
		TW1	83.550	TL1	79.900	CTW1	83.000	DTW1	3.100	H1	2215.66
		TW3	88.400	TL3	81.050	CTW3	87.850	DTW3	6.800	H3	1010.21
		AVGTW=	85.234			AVGDTW=	4.950			AVGH=	1387.71
15	11755.72	TWO	87.250	TL0	79.900	CTWO	86.310	DTWO	6.410	HO	1833.91
		TW1	84.500	TL1	79.900	CTW1	83.560	DTW1	3.660	H1	3211.78
		TW3	89.550	TL3	81.050	CTW3	88.610	DTW3	7.560	H3	1554.95
		AVGTW=	86.160			AVGDTW=	5.876			AVGH=	2000.34
16	16539.44	TWO	87.900	TL0	79.900	CTWO	86.577	DTWO	6.677	HO	2476.80
		TW1	85.550	TL1	79.900	CTW1	84.227	DTW1	4.327	H1	3821.71
		TW3	90.500	TL3	81.450	CTW3	89.177	DTW3	7.727	H3	2140.26
		AVGTW=	86.661			AVGDTW=	6.244			AVGH=	2648.67
17	22127.40	TWO	88.700	TL0	79.900	CTWO	86.930	DTWO	7.030	HO	3148.89
		TW1	86.900	TL1	79.900	CTW1	85.130	DTW1	5.230	H1	4232.59
		TW3	93.150	TL3	81.450	CTW3	91.380	DTW3	9.930	H3	2229.29
		AVGTW=	87.813			AVGDTW=	7.396			AVGH=	2992.80
18	29414.76	TWO	89.200	TL0	79.900	CTWO	86.848	DTWO	6.948	HO	4233.29
		TW1	88.000	TL1	79.900	CTW1	85.648	DTW1	5.748	H1	5117.00
		TW3	93.250	TL3	81.450	CTW3	90.898	DTW3	9.448	H3	3113.19
		AVGTW=	87.798			AVGDTW=	7.381			AVGH=	3984.78
19	37709.92	TWO	90.000	TL0	79.900	CTWO	86.985	DTWO	7.085	HO	5322.29
		TW1	89.400	TL1	79.900	CTW1	86.385	DTW1	6.485	H1	5814.69
		TW3	94.575	TL3	81.450	CTW3	91.560	DTW3	10.110	H3	3729.86
		AVGTW=	88.310			AVGDTW=	7.893			AVGH=	4777.27

TABLE B-1 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING DISTILLED WATER

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	LIQUID TEMPERATURE DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K	
		p=25.33 KN/SQ.M			TS=65.30 DEG.C		
20	6870.23	TWO 71.200 TW1 69.025 TW3 75.550 AVGTW= 71.375	TL0 65.100 TL1 65.100 TL3 66.000	CTWO 70.650 CTW1 68.475 CTW3 75.000 AVGDTW= 5.975	DTWO 5.550 DTW1 3.375 DTW3 9.000	HO 1237.71 H1 2035.17 H3 763.36 AVGH=1143.83	
21	11755.72	TWO 72.850 TW1 70.350 TW3 77.030 AVGTW= 72.470	TL0 65.100 TL1 65.100 TL3 66.000	CTWO 71.910 CTW1 69.410 CTW3 76.090 AVGDTW= 7.070	DTWO 6.810 DTW1 4.310 DTW3 10.09	HO 1726.20 H1 2727.43 H3 1165.08 AVGH=1662.80	
22	16539.44	TWO 73.800 TW1 71.475 TW3 78.150 AVGTW= 73.152	TL0 65.100 TL1 65.100 TL3 66.700	CTWO 72.477 CTW1 70.152 CTW3 76.827 AVGDTW= 7.512	DTWO 7.377 DTW1 5.052 DTW3 10.127	HO 2241.80 H1 3273.35 H3 1633.20 AVGH=2199.78	
23	22137.40	TWO 74.700 TW1 73.000 TW3 79.125 AVGTW= 73.838	TL0 65.100 TL1 65.100 TL3 66.700	CTWO 72.930 CTW1 71.230 CTW3 77.355 AVGDTW= 8.205	DTWO 7.830 DTW1 6.130 DTW3 10.655	HO 2827.17 H1 3611.19 H3 2077.61 AVGH=2697.96	
24	29414.76	TWO 75.500 TW1 74.000 TW3 81.200 AVGTW= 74.548	TL0 65.100 TL1 65.100 TL3 66.700	CTWO 73.148 CTW1 71.648 CTW3 78.848 AVGDTW= 8.915	DTWO 8.048 DTW1 6.548 DTW3 12.148	HO 3654.72 H1 4491.87 H3 2421.36 AVGH=3299.59	
25	37709.92	TWO 76.500 TW1 75.750 TW3 82.675 AVGTW= 75.293	TL0 65.100 TL1 65.100 TL3 66.700	CTWO 73.485 CTW1 72.735 CTW3 79.660 AVGDTW= 9.660	DTWO 8.385 DTW1 7.635 DTW3 12.960	HO 4497.16 H1 4938.90 H3 2909.71 AVGH=3903.72	

TABLE B-1 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING DISTILLED WATER

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	LIQUID TEMPERATURE DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
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P=11.33 KN/SQ.M

TS=48.50 DEG.C

26	6870.23	TWO	54.153	TL0	48.300	CTWO	53.603	DTWO	5.303	HO	1295.54
		TW1	56.483	TL1	48.300	CTW1	55.933	DTW1	7.633	H1	900.07
		TW3	59.753	TL3	49.400	CTW3	59.503	DTW3	9.803	H3	700.83
		AVGTW=	56.346			AVGDTW=	7.580			AVGH=	906.26
27	11755.73	TWO	56.337	TL0	48.300	CTWO	55.397	DTWO	7.097	HO	1656.44
		TW1	58.588	TL1	48.300	CTW1	57.649	DTW1	9.349	H1	1257.43
		TW3	62.108	TL3	49.400	CTW3	61.168	DTW3	11.768	H3	998.96
		AVGTW=	58.071			AVGDTW=	9.405			AVGH=	1249.97
28	16539.44	TWO	56.947	TL0	48.300	CTWO	55.624	DTWO	7.324	HO	2258.02
		TW1	59.448	TL1	48.300	CTW1	58.125	DTW1	9.825	H1	1683.27
		TW3	63.446	TL3	49.600	CTW3	62.123	DTW3	12.523	H3	1320.65
		AVGTW=	58.624			AVGDTW=	9.891			AVGH=	1672.10
29	22137.40	TWO	59.400	TL0	48.300	CTWO	57.630	DTWO	9.330	HO	2372.65
		TW1	61.321	TL1	48.300	CTW1	59.551	DTW1	11.251	H1	1967.55
		TW3	65.670	TL3	49.600	CTW3	63.900	DTW3	14.300	H3	1548.05
		AVGTW=	60.360			AVGDTW=	11.627			AVGH=	1903.93
30	29414.76	TWO	61.150	TL0	48.300	CTWO	58.798	DTWO	10.498	HO	2801.82
		TW1	62.751	TL1	48.300	CTW1	60.399	DTW1	12.099	H1	2431.08
		TW3	64.472	TL3	49.602	CTW3	62.120	DTW3	12.518	H3	2349.71
		AVGTW=	60.439			AVGDTW=	11.705			AVGH=	2512.91

TAELE B-2 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING ISOPROPANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	LIQUID TEMP DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
		p=97.98 KN/SQ.M			TS=81.60 DEG.C	
31	6870.23	TWO 89.600	TLO 81.800	CTWO 89.050	DTWO 7.250	HO 947.52
		TW1 90.650	TL1 81.800	CTW1 90.100	DTW1 8.300	H1 827.66
		TW3 89.550	TL3 82.250	CTW3 89.000	DTW3 6.750	H3 1017.70
		AVGTW= 89.384		AVGDTW= 7.434		AVGH= 924.15
32	11755.73	TWO 91.075	TLO 81.800	CTWO 90.135	DTWO 8.335	HO 1410.37
		TW1 91.850	TL1 81.800	CTW1 90.910	DTW1 9.110	H1 1290.39
		TW3 91.400	TL3 82.700	CTW3 90.460	DTW3 7.760	H3 1514.88
		AVGTW= 90.501		AVGDTW= 8.401		AVGH=1399.18
33	16539.44	TWO 92.925	TLO 81.800	CTWO 91.602	DTWO 9.802	HO 1687.22
		TW1 93.675	TL1 81.800	CTW1 92.352	DTW1 10.552	H1 1567.31
		TW3 93.300	TL3 82.700	CTW3 91.977	DTW3 9.277	H3 1782.70
		AVGTW= 91.977		AVGDTW= 9.877		AVGH=1674.41
34	22137.40	TWO 94.225	TLO 81.800	CTWO 92.455	DTWO 10.655	HO 2077.61
		TW1 95.375	TL1 81.800	CTW1 93.605	DTW1 11.805	H1 1875.22
		TW3 95.250	TL3 82.700	CTW3 93.480	DTW3 10.780	H3 2053.52
		AVGTW= 93.180		AVGDTW= 11.080		AVGH=1997.92
35	26055.98	TWO 94.925	TLO 81.800	CTWO 92.841	DTWO 11.041	HO 2359.72
		TW1 95.975	TL1 81.800	CTW1 93.891	DTW1 12.091	H1 2154.82
		TW3 96.425	TL3 82.700	CTW3 94.341	DTW3 11.641	H3 2238.11
		AVGTW= 93.691		AVGDTW= 11.591		AVGH=2247.76
36	33893.13	TWO 96.100	TLO 81.800	CTWO 93.390	DTWO 11.590	HO 2924.24
		TW1 96.700	TL1 81.800	CTW1 93.990	DTW1 12.190	H1 2780.31
		TW3 99.050	TL3 82.700	CTW3 96.340	DTW3 13.640	H3 2484.76
		AVGTW= 94.573		AVGDTW= 12.473		AVGH=2717.16
37	37709.92	TWO 96.900	TLO 81.800	CTWO 93.885	DTWO 12.085	HO 3120.32
		TW1 97.250	TL1 81.800	CTW1 94.235	DTW1 12.435	H1 3032.49
		TW3 100.150	TL3 82.700	CTW3 97.135	DTW3 14.435	H3 2612.34
		AVGTW= 95.085		AVGDTW= 12.985		AVGH=2904.05

TABLE B-2 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING ISOPROPANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
		P=80.77 KN/SQ.M		TS=77.00 DEG.C		
38	11755.73	TWO 87.875	TL0 77.200	CTWO 86.935	DTWO 9.735	HO 1207.55
		TW1 88.575	TL1 77.200	CTW1 87.635	DTW1 10.435	H1 1126.55
		TW3 87.550	TL3 77.900	CTW3 86.610	DTW3 8.710	H3 1349.65
		AVGTW= 87.060		AVGDTW= 9.626		AVGH=1221.14
39	16539.44	TWO 89.700	TL0 77.200	CTWO 88.377	DTWO 11.177	HO 1479.67
		TW1 90.150	TL1 77.200	CTW1 88.827	DTW1 11.627	H1 1422.41
		TW3 89.000	TL3 77.900	CTW3 87.677	DTW3 9.777	H3 1691.54
		AVGTW= 88.294		AVGDTW= 10.861		AVGH=1522.82
40	22137.40	TWO 91.300	TL0 77.200	CTWO 89.530	DTWO 12.330	HO 1795.38
		TW1 91.850	TL1 77.200	CTW1 90.080	DTW1 12.880	H1 1718.71
		TW3 91.575	TL3 77.900	CTW3 89.805	DTW3 11.905	H3 1859.47
		AVGTW= 89.805		AVGDTW= 12.371		AVGH=1789.33
41	26055.98	TWO 92.275	TL0 77.200	CTWO 90.191	DTWO 12.991	HO 2005.55
		TW1 92.500	TL1 77.200	CTW1 90.416	DTW1 13.216	H1 1971.41
		TW3 93.200	TL3 77.900	CTW3 91.116	DTW3 13.216	H3 1971.41
		AVGTW= 90.575		AVGDTW= 13.141		AVGH=1982.66
42	33893.13	TWO 93.350	TL0 77.200	CTWO 90.640	DTWO 13.440	HO 2521.73
		TW1 92.500	TL1 77.200	CTW1 89.790	DTW1 12.590	H1 2691.98
		TW3 95.900	TL3 77.900	CTW3 93.190	DTW3 15.290	H3 2216.63
		AVGTW= 91.207		AVGDTW= 13.773		AVGH=2460.70
43	37709.92	TWO 94.350	TL0 77.200	CTWO 91.335	DTWO 14.135	HO 2667.79
		TW1 93.275	TL1 77.200	CTW1 90.260	DTW1 13.060	H1 2887.37
		TW3 97.425	TL3 77.900	CTW3 94.410	DTW3 16.510	H3 2284.03
		AVGTW= 92.001		AVGDTW= 14.568		AVGH=2588.44



TABLE B-2 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING ISOPROPANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	LIQUID TEMPERATURE DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K	
		p=67.28 KN/SQ.M			TS=72.90 DEG.C		
44	6870.23	TWO 82.025	TLO 73.050	CTWO 81.475	DTWO 8.425	HO 815.38	
		TW1 82.500	TL1 73.050	CTW1 81.950	DTW1 8.900	H1 771.87	
		TW3 82.500	TL3 73.775	CTW3 81.950	DTW3 8.175	H3 840.32	
		AVGTW= 81.792		AVGDTW= 8.500		AVGH= 808.19	
45	11755.73	TWO 84.100	TLO 73.050	CTWO 83.160	DTWO 10.110	HO 1162.76	
		TW1 84.700	TL1 73.050	CTW1 83.760	DTW1 10.710	H1 1097.62	
		TW3 83.800	TL3 73.775	CTW3 82.860	DTW3 9.085	H3 1293.94	
		AVGTW= 83.260		AVGDTW= 9.968		AVGH=1179.28	
46	16539.44	TWO 86.025	TLO 73.050	CTWO 84.702	DTWO 11.652	HO 1419.36	
		TW1 86.550	TL1 73.050	CTW1 85.227	DTW1 12.177	H1 1358.17	
		TW3 85.700	TL3 73.775	CTW3 84.377	DTW3 10.602	H3 1559.92	
		AVGTW= 84.769		AVGDTW= 11.477		AVGH=1441.00	
47	22137.40	TWO 88.000	TLO 73.050	CTWO 86.230	DTWO 13.180	HO 1679.59	
		TW1 88.250	TL1 73.050	CTW1 86.480	DTW1 13.430	H1 1648.33	
		TW3 87.900	TL3 73.775	CTW3 86.130	DTW3 12.355	H3 1791.74	
		AVGTW= 86.280		AVGDTW= 12.988		AVGH=1704.38	
48	26055.98	TWO 88.675	TLO 73.050	CTWO 86.591	DTWO 13.541	HO 1924.09	
		TW1 88.575	TL1 73.050	CTW1 86.491	DTW1 13.441	H1 1938.41	
		TW3 89.200	TL3 73.775	CTW3 87.116	DTW3 13.341	H3 1952.94	
		AVGTW= 86.733		AVGDTW= 13.441		AVGH=1938.41	
49	33893.13	TWO 90.100	TLO 73.050	CTWO 87.390	DTWO 14.340	HO 2363.47	
		TW1 89.000	TL1 73.050	CTW1 86.290	DTW1 13.240	H1 2559.82	
		TW3 92.850	TL3 73.950	CTW3 90.140	DTW3 16.190	H3 2093.41	
		AVGTW= 87.940		AVGDTW= 14.590		AVGH=2322.97	
50	37709.92	TWO 91.100	TLO 73.050	CTWO 88.085	DTWO 15.035	HO 2508.10	
		TW1 89.925	TL1 73.050	CTW1 86.910	DTW1 13.860	H1 2720.72	
		TW3 96.300	TL3 73.950	CTW3 93.285	DTW3 19.335	H3 1950.32	
		AVGTW= 89.426		AVGDTW= 16.076		AVGH=2345.59	

TABLE B-2 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING ISOPROPANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
p=54.65 KN/SQ.M				TS=68.25 DEG.C		
51	6870.22	TWO 79.500	TL0 68.500	CTWO 78.950	DTWO 10.450	HO 657.39
		TW1 78.800	TL1 68.500	CTW1 78.250	DTW1 9.750	H1 704.58
		TW3 79.400	TL3 69.650	CTW3 78.850	DTW3 9.200	H3 746.70
		AVGTW= 78.684		AVGDTW= 9.800		AVGH= 700.99
52	11755.73	TWO 80.775	TL0 68.500	CTWO 79.835	DTWO 11.335	HO 1037.10
		TW1 81.056	TL1 68.500	CTW1 80.116	DTW1 11.616	H1 1012.01
		TW3 80.450	TL3 69.650	CTW3 79.510	DTW3 9.860	H3 1192.24
		AVGTW= 79.820		AVGDTW= 10.937		AVGH=1074.84
53	16539.44	TWO 82.700	TL0 68.500	CTWO 81.377	DTWO 12.877	HO 1284.34
		TW1 82.600	TL1 68.500	CTW1 81.277	DTW1 12.777	H1 1294.39
		TW3 81.900	TL3 69.450	CTW3 80.577	DTW3 11.127	H3 1486.32
		AVGTW= 81.077		AVGDTW= 12.261		AVGH=1348.94
54	22137.40	TWO 84.900	TL0 68.500	CTWO 83.130	DTWO 14.630	HO 1513.13
		TW1 84.025	TL1 68.500	CTW1 82.255	DTW1 13.755	H1 1609.38
		TW3 84.100	TL3 69.450	CTW3 82.230	DTW3 12.880	H3 1718.71
		AVGTW= 82.571		AVGDTW= 13.755		AVGH=1609.38
55	26055.98	TWO 85.450	TL0 68.500	CTWO 83.366	DTWO 14.866	HO 1752.61
		TW1 84.350	TL1 68.500	CTW1 82.266	DTW1 13.766	H1 1892.65
		TW3 85.575	TL3 69.450	CTW3 83.491	DTW3 14.041	H3 1855.58
		AVGTW= 83.041		AVGDTW= 14.225		AVGH=1831.67
56	33893.13	TWO 87.400	TL0 68.500	CTWO 84.690	DTWO 16.190	HO 2093.41
		TW1 85.625	TL1 68.500	CTW1 82.915	DTW1 14.415	H1 2351.17
		TW3 89.350	TL3 69.550	CTW3 86.640	DTW3 16.990	H3 1994.84
		AVGTW= 84.748		AVGDTW= 15.865		AVGH=2136.29
57	37709.92	TWO 88.025	TL0 68.500	CTWO 85.010	DTWO 16.510	HO 2284.03
		TW1 85.575	TL1 68.500	CTW1 82.560	DTW1 14.060	H1 2682.02
		TW3 91.000	TL3 69.450	CTW3 87.985	DTW3 18.535	H3 2034.49
		AVGTW= 85.185		AVGDTW= 16.368		AVGH=2303.79

TABLE B-2 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING ISOPROPANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
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p=41.32 KN/SQ.M

TS=62.40 DEG.C

58	6870.23	TWO	74.200	TLO	62.850	CTWO	73.650	DTWO	10.800	HO	636.09
		TW1	73.725	TL1	62.850	CTW1	73.175	DTW1	10.325	H1	665.35
		TW3	74.860	TL3	63.850	CTW3	74.310	DTW3	10.460	H3	656.76
		AVGTW=	73.712			AVGDTW=	10.529			AVGH=	652.50
59	11755.73	TWO	75.575	TLO	62.850	CTWO	74.635	DTWO	11.785	HO	997.50
		TW1	75.500	TL1	62.850	CTW1	74.560	DTW1	11.710	H1	1003.89
		TW3	76.250	TL3	63.850	CTW3	75.310	DTW3	11.460	H3	1025.79
		AVGTW=	74.835			AVGDTW=	11.651			AVGH=	1008.91
60	16559.44	TWO	77.850	TLO	62.850	CTWO	76.526	DTWO	13.676	HO	1210.83
		TW1	77.850	TL1	62.850	CTW1	76.526	DTW1	13.676	H1	1210.83
		TW3	78.075	TL3	63.850	CTW3	76.751	DTW3	12.901	H3	1283.56
		AVGTW=	76.601			AVGDTW=	13.417			AVGH=	1234.14
61	22137.40	TWO	79.925	TLO	62.850	CTWO	78.155	DTWO	15.305	HO	1446.40
		TW1	79.350	TL1	62.850	CTW1	77.580	DTW1	14.730	H1	1502.86
		TW3	79.450	TL3	63.850	CTW3	77.680	DTW3	13.830	H3	1600.65
		AVGTW=	77.805			AVGDTW=	14.621			AVGH=	1513.99
62	26055.98	TWO	81.850	TLO	62.850	CTWO	79.766	DTWO	16.916	HO	1540.23
		TW1	80.325	TL1	62.850	CTW1	78.241	DTW1	15.391	H1	1692.83
		TW3	82.150	TL3	63.850	CTW3	80.066	DTW3	16.216	H3	1606.71
		AVGTW=	79.358			AVGDTW=	16.175			AVGH=	1610.85
63	33893.13	TWO	83.350	TLO	62.850	CTWO	80.640	DTWO	17.790	HO	1905.13
		TW1	80.950	TL1	62.850	CTW1	78.240	DTW1	15.390	H1	2202.22
		TW3	85.850	TL3	63.850	CTW3	83.140	DTW3	19.290	H3	1756.99
		AVGTW=	80.673			AVGDTW=	17.490			AVGH=	1937.81

TABLE B-2 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING ISOPROPANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K	
		p=29.33 KN/SQ.M			TS=55.20 DEG.C		
64	6870.23	TWO 69.450	TLO 55.750	CTWO 68.900	DTWO 13.150	HO 522.42	
		TW1 67.000	TL1 55.750	CTW1 66.450	DTW1 10.700	H1 642.03	
		TW3 70.800	TL3 56.500	CTW3 70.250	DTW3 13.750	H3 499.63	
		AVGTW= 68.534		AVGDTW= 12.534		AVGH= 548.12	
65	11755.73	TWO 71.000	TLO 55.750	CTWO 70.060	DTWO 14.310	HO 821.49	
		TW1 68.750	TL1 55.750	CTW1 67.810	DTW1 12.060	H1 974.75	
		TW3 71.700	TL3 56.500	CTW3 70.760	DTW3 14.260	H3 824.37	
		AVGTW= 69.543		AVGDTW= 13.543		AVGH= 868.00	
66	16559.44	TWO 72.375	TLO 55.750	CTWO 71.051	DTWO 15.301	HO 1082.23	
		TW1 71.150	TL1 55.750	CTW1 69.826	DTW1 14.076	H1 1176.42	
		TW3 72.825	TL3 56.500	CTW3 71.501	DTW3 15.001	H3 1103.88	
		AVGTW= 70.792		AVGDTW= 14.792		AVGH=1119.42	
67	22137.40	TWO 74.100	TLO 55.750	CTWO 72.330	DTWO 16.580	HO 1335.17	
		TW1 72.400	TL1 55.750	CTW1 70.630	DTW1 14.880	H1 1487.71	
		TW3 75.000	TL3 56.500	CTW3 73.230	DTW3 16.730	H3 1323.20	
		AVGTW= 72.063		AVGDTW= 16.063		AVGH=1378.11	
68	26055.98	TWO 74.750	TLO 55.750	CTWO 72.666	DTWO 16.916	HO 1540.23	
		TW1 73.400	TL1 55.750	CTW1 71.316	DTW1 15.566	H1 1673.80	
		TW3 75.900	TL3 56.500	CTW3 73.816	DTW3 17.316	H3 1504.65	
		AVGTW= 72.600		AVGDTW= 16.600		AVGH=1569.61	
69	33893.13	TWO 77.200	TLO 55.750	CTWO 74.490	DTWO 18.740	HO 1808.56	
		TW1 74.200	TL1 55.750	CTW1 71.490	DTW1 15.740	H1 2153.25	
		TW3 79.500	TL3 56.500	CTW3 76.790	DTW3 20.290	H3 1670.40	
		AVGTW= 74.257		AVGDTW= 18.257		AVGH=1856.44	

TABLE B-2 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING ISOPROPANOL

FUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K	
		P=15.33 KN/SQ.M			TS=43.20 DEG.C		
70	6870.23	TWO 58.675	TL0 43.850	CTWO 58.125	DTWO 14.275	HO 481.25	
		TW1 55.250	TL1 43.850	CTW1 54.700	DTW1 10.850	H1 633.16	
		TW3 60.700	TL3 44.750	CTW3 60.150	DTW3 15.400	H3 446.10	
		AVGTW= 57.659		AVGDTW= 13.509		AVGH= 508.56	
71	11755.73	TWO 60.950	TL0 43.850	CTWO 60.010	DTWO 16.160	HO 727.45	
		TW1 57.325	TL1 43.850	CTW1 56.385	DTW1 12.535	H1 937.82	
		TW3 64.400	TL3 44.750	CTW3 63.460	DTW3 18.710	H3 628.31	
		AVGTW= 59.951		AVGDTW= 15.801		AVGH= 743.95	
72	16559.44	TWO 64.150	TL0 43.850	CTWO 62.826	DTWO 18.976	HO 872.64	
		TW1 60.500	TL1 43.850	CTW1 59.176	DTW1 15.326	H1 1080.47	
		TW3 65.550	TL3 44.750	CTW3 64.226	DTW3 19.476	H3 850.24	
		AVGTW= 62.076		AVGDTW= 17.926		AVGH= 923.76	
73	22137.40	TWO 65.550	TL0 43.850	CTWO 63.780	DTWO 19.930	HO 1110.75	
		TW1 61.850	TL1 43.850	CTW1 60.080	DTW1 16.230	H1 1363.96	
		TW3 66.700	TL3 44.750	CTW3 64.930	DTW3 20.180	H3 1096.98	
		AVGTW= 62.930		AVGDTW= 18.780		AVGH= 1178.76	
74	26055.98	TWO 66.550	TL0 43.850	CTWO 64.466	DTWO 20.616	HO 1263.81	
		TW1 62.550	TL1 43.850	CTW1 60.466	DTW1 16.616	H1 1568.04	
		TW3 68.050	TL3 44.750	CTW3 65.966	DTW3 21.216	H3 1228.07	
		AVGTW= 63.633		AVGDTW= 19.483		AVGH= 1337.33	
75	33893.13	TWO 68.500	TL0 43.850	CTWO 65.790	DTWO 21.940	HO 1544.78	
		TW1 64.150	TL1 43.850	CTW1 61.440	DTW1 17.590	H1 1926.80	
		TW3 70.800	TL3 44.750	CTW3 68.090	DTW3 23.340	H3 1452.12	
		AVGTW= 65.107		AVGDTW= 20.957		AVGH= 1617.26	

TABLE B-3 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING ETHANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	LIQUID TEMPERATURE DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
p=98.18 KN/SQ.M      TS=78.00 DEG.C						
76	3307.89	TWO 84.250	TLO 78.000	CTWO 83.985	DTWO 5.985	HO 552.65
		TW1 84.000	TL1 78.100	CTW1 83.735	DTW1 5.635	H1 586.97
		TW3 84.600	TL3 78.450	CTW3 84.335	DTW3 5.885	H3 562.04
		AVGTW= 84.018		AVGDTW= 5.835		AVGH= 566.85
77	6870.23	TWO 85.450	TLO 78.250	CTWO 84.900	DTWO 6.650	HO 1033.00
		TW1 85.575	TL1 78.250	CTW1 85.025	DTW1 6.775	H1 1013.94
		TW3 85.575	TL3 78.450	CTW3 85.025	DTW3 6.575	H3 1044.78
		AVGTW= 84.984		AVGDTW= 6.667		AVGH=1030.42
78	11755.73	TWO 87.350	TLO 78.250	CTWO 86.410	DTWO 8.160	HO 1440.62
		TW1 88.100	TL1 78.350	CTW1 87.160	DTW1 8.810	H1 1334.33
		TW3 86.550	TL3 78.700	CTW3 85.610	DTW3 6.910	H3 1701.22
		AVGTW= 86.393		AVGDTW= 7.960		AVGH=1476.81
79	14351.15	TWO 88.250	TLO 78.250	CTWO 87.102	DTWO 8.852	HO 1621.10
		TW1 89.350	TL1 78.350	CTW1 88.202	DTW1 9.852	H1 1456.57
		TW3 88.325	TL3 78.700	CTW3 87.177	DTW3 8.477	H3 1692.81
		AVGTW= 87.494		AVGDTW= 9.061		AVGH=1583.83
80	16539.44	TWO 89.100	TLO 78.250	CTWO 87.777	DTWO 9.527	HO 1735.92
		TW1 90.125	TL1 78.350	CTW1 88.802	DTW1 10.452	H1 1582.30
		TW3 88.675	TL3 78.700	CTW3 87.352	DTW3 8.652	H3 1911.47
		AVGTW= 87.977		AVGDTW= 9.544		AVGH=1732.89
81	19592.88	TWO 90.000	TLO 78.250	CTWO 88.433	DTWO 10.183	HO 1923.95
		TW1 91.000	TL1 78.350	CTW1 89.433	DTW1 11.083	H1 1767.73
		TW3 89.350	TL3 78.700	CTW3 87.783	DTW3 9.083	H3 2156.94
		AVGTW= 88.550		AVGDTW= 10.116		AVGH=1936.63
82	22137.40	TWO 91.000	TLO 78.450	CTWO 89.230	DTWO 10.780	HO 2053.52
		TW1 91.650	TL1 78.450	CTW1 89.880	DTW1 11.430	H1 1936.74
		TW3 90.200	TL3 79.000	CTW3 88.430	DTW3 9.430	H3 2347.49
		AVGTW= 89.180		AVGDTW= 10.546		AVGH=2098.95
83	26055.98	TWO 91.400	TLO 78.450	CTWO 89.316	DTWO 10.866	HO 2397.73
		TW1 92.600	TL1 78.450	CTW1 90.516	DTW1 12.066	H1 2159.28
		TW3 90.650	TL3 79.000	CTW3 88.866	DTW3 9.566	H3 2405.10
		AVGTW= 89.466		AVGDTW= 10.833		AVGH=2405.10

TABLE B-3 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING ETHANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K					
		p=84.85 KN/SQ.M			TS=73.25 DEG.C						
E4	11755.73	TWO	83.650	TL0	73.275	CTWO	82.710	DTWO	9.435	HO	1245.94
		TW1	84.000	TL1	73.275	CTW1	83.060	DTW1	9.785	H1	1201.38
		TW3	83.500	TL3	73.950	CTW3	82.560	DTW3	8.610	H3	1365.33
		AVGTW=	82.776			AVGDTW=	9.276			AVGH=	1267.21
E5	14351.15	TWO	84.400	TL0	73.275	CTWO	83.252	DTWO	9.977	HO	1438.32
		TW1	84.950	TL1	73.275	CTW1	83.802	DTW1	10.527	H1	1363.18
		TW3	84.250	TL3	73.950	CTW3	83.102	DTW3	9.152	H3	1567.97
		AVGTW=	83.386			AVGDTW=	9.886			AVGH=	1451.66
86	16539.44	TWO	85.075	TL0	73.275	CTWO	83.752	DTWO	10.477	HO	1578.53
		TW1	85.575	TL1	73.275	CTW1	84.252	DTW1	10.977	H1	1506.63
		TW3	84.700	TL3	73.950	CTW3	83.377	DTW3	9.427	H3	1754.33
		AVGTW=	83.794			AVGDTW=	10.294			AVGH=	1606.64
87	19592.88	TWO	86.200	TL0	73.275	CTWO	84.633	DTWO	11.358	HO	1724.93
		TW1	86.700	TL1	73.275	CTW1	85.133	DTW1	11.858	H1	1652.20
		TW3	85.750	TL3	73.950	CTW3	84.183	DTW3	10.233	H3	1914.55
		AVGTW=	84.650			AVGDTW=	11.150			AVGH=	1757.16
E8	22137.40	TWO	86.600	TL0	73.275	CTWO	84.830	DTWO	11.555	HO	1915.79
		TW1	86.900	TL1	73.275	CTW1	85.130	DTW1	11.855	H1	1867.31
		TW3	86.000	TL3	73.950	CTW3	84.230	DTW3	10.280	H3	2153.40
		AVGTW=	84.730			AVGDTW=	11.230			AVGH=	1971.23
E9	26055.98	TWO	86.900	TL0	73.275	CTWO	84.816	DTWO	11.541	HO	2257.50
		TW1	88.450	TL1	73.275	CTW1	86.366	DTW1	13.091	H1	1990.23
		TW3	86.700	TL3	73.950	CTW3	84.616	DTW3	10.666	H3	2442.68
		AVGTW=	85.266			AVGDTW=	11.766			AVGH=	2214.33
E0	33893.13	TWO	88.700	TL0	73.275	CTWO	85.990	DTWO	12.715	HO	2665.51
		TW1	90.100	TL1	73.275	CTW1	87.390	DTW1	14.115	H1	2401.14
		TW3	88.000	TL3	73.950	CTW3	85.290	DTW3	11.340	H3	2988.70
		AVGTW=	86.223			AVGDTW=	12.723			AVGH=	2663.77

TABLE B-3 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING ETHANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	LIQUID TEMPERATURE DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
		P=71.32 KN/SQ.M			TS=69.00 DEG.C	
91	6870.23	TWO 77.575	TL0 68.700	CTWO 77.025	DTWO 8.325	HO 825.18
		TW1 77.100	TL1 68.700	CTW1 76.550	DTW1 7.850	H1 875.10
		TW3 78.250	TL3 69.150	CTW3 77.700	DTW3 8.550	H3 803.46
		AVGTW= 77.092		AVGDTW= 8.242		AVGH= 833.52
92	11755.73	TWO 79.800	TL0 68.700	CTWO 78.860	DTWO 10.160	HO 1157.04
		TW1 79.700	TL1 68.700	CTW1 78.760	DTW1 10.060	H1 1168.54
		TW3 80.000	TL3 69.150	CTW3 79.060	DTW3 9.910	H3 1186.23
		AVGTW= 78.893		AVGDTW= 10.043		AVGH=1170.48
93	16539.44	TWO 81.500	TL0 68.700	CTWO 80.177	DTWO 11.477	HO 1441.00
		TW1 81.500	TL1 68.700	CTW1 80.177	DTW1 11.477	H1 1441.00
		TW3 80.700	TL3 69.150	CTW3 79.377	DTW3 10.227	H3 1617.11
		AVGTW= 79.911		AVGDTW= 11.061		AVGH=1495.28
94	22137.40	TWO 82.800	TL0 68.700	CTWO 81.030	DTWO 12.330	HO 1795.38
		TW1 82.800	TL1 68.700	CTW1 81.030	DTW1 12.330	H1 1795.38
		TW3 82.050	TL3 69.150	CTW3 80.280	DTW3 11.130	H3 1988.94
		AVGTW= 80.780		AVGDTW= 11.930		AVGH=1855.57
95	26055.98	TWO 83.800	TL0 68.700	CTWO 81.716	DTWO 13.016	HO 2001.70
		TW1 83.800	TL1 68.700	CTW1 81.716	DTW1 13.016	H1 2001.70
		TW3 83.000	TL3 69.150	CTW3 80.916	DTW3 11.766	H3 2214.33
		AVGTW= 81.450		AVGDTW= 12.600		AVGH=2067.89
96	33893.13	TWO 84.900	TL0 68.700	CTWO 82.190	DTWO 13.490	HO 2512.39
		TW1 84.000	TL1 68.700	CTW1 81.290	DTW1 12.590	H1 2691.98
		TW3 84.950	TL3 69.150	CTW3 82.240	DTW3 13.090	H3 2589.16
		AVGTW= 81.907		AVGDTW= 13.057		AVGH=2595.77



TAELE B-3 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING ETHANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
		P=44.65 KN/SQ.M		TS=59.00 DEG.C		
97	6870.23	TWO 68.775	TL0 58.775	CTWO 68.225	DTWO 9.450	HO 726.95
		TW1 68.475	TL1 58.775	CTW1 67.925	DTW1 9.150	H1 750.78
		TW3 71.150	TL3 59.550	CTW3 70.600	DTW3 11.050	H3 621.70
		AVGTW= 68.917		AVGDTW= 9.884		AVGH= 695.08
98	11755.73	TWO 70.800	TL0 58.775	CTWO 69.860	DTWO 11.085	HO 1060.49
		TW1 70.475	TL1 58.775	CTW1 69.535	DTW1 10.760	H1 1092.52
		TW3 72.350	TL3 59.550	CTW3 71.410	DTW3 11.860	H3 991.19
		AVGTW= 70.268		AVGDTW= 11.235		AVGH=1046.33
99	16539.44	TWO 72.300	TL0 58.775	CTWO 70.977	DTWO 12.202	HO 1355.39
		TW1 72.050	TL1 58.775	CTW1 70.727	DTW1 11.952	H1 1383.73
		TW3 73.550	TL3 59.550	CTW3 72.227	DTW3 12.677	H3 1304.60
		AVGTW= 71.311		AVGDTW= 12.277		AVGH=1347.11
100	22137.40	TWO 74.500	TL0 58.775	CTWO 72.730	DTWO 13.955	HO 1586.32
		TW1 73.625	TL1 58.775	CTW1 71.855	DTW1 13.080	H1 1692.43
		TW3 75.050	TL3 59.550	CTW3 73.280	DTW3 13.730	H3 1612.31
		AVGTW= 72.621		AVGDTW= 13.588		AVGH=1629.12
101	26055.98	TWO 75.450	TL0 58.775	CTWO 73.366	DTWO 14.591	HO 1785.64
		TW1 74.500	TL1 58.775	CTW1 72.416	DTW1 13.641	H1 1909.99
		TW3 76.100	TL3 59.550	CTW3 74.016	DTW3 14.466	H3 1801.07
		AVGTW= 73.266		AVGDTW= 14.233		AVGH=1830.59
102	33893.13	TWO 76.075	TL0 58.775	CTWO 73.365	DTWO 14.590	HO 2322.97
		TW1 75.575	TL1 58.775	CTW1 72.865	DTW1 14.090	H1 2405.40
		TW3 77.100	TL3 59.550	CTW3 74.390	DTW3 14.840	H3 2283.84
		AVGTW= 73.540		AVGDTW= 14.507		AVGH=2336.32

TABLE B-3 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING ETHANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K	
		p=31.32 KN/SQ.M			TS=51.00 DEG.C		
103	6870.23	TWO 63.000	TLO 51.650	CTWO 62.450	DTWO 10.800	HO 636.09	
		TW1 62.100	TL1 51.650	CTW1 61.550	DTW1 9.900	H1 693.91	
		TW3 65.350	TL3 52.350	CTW3 64.800	DTW3 12.450	H3 551.79	
		AVGTW= 62.934		AVGDTW= 11.050		AVGH= 621.70	
104	11755.73	TWO 65.200	TLO 51.650	CTWO 64.260	DTWO 12.610	HO 932.24	
		TW1 64.800	TL1 51.650	CTW1 63.860	DTW1 12.210	H1 962.78	
		TW3 67.275	TL3 52.350	CTW3 66.335	DTW3 13.985	H3 840.58	
		AVGTW= 64.818		AVGDTW= 12.935		AVGH= 908.82	
105	16539.44	TWO 66.400	TLO 51.650	CTWO 65.077	DTWO 13.427	HO 1231.74	
		TW1 66.000	TL1 51.650	CTW1 64.677	DTW1 13.027	H1 1269.55	
		TW3 68.825	TL3 52.350	CTW3 67.502	DTW3 15.152	H3 1091.51	
		AVGTW= 65.752		AVGDTW= 13.869		AVGH= 1192.51	
106	22137.40	TWO 68.650	TLO 51.650	CTWO 66.880	DTWO 15.230	HO 1453.52	
		TW1 68.200	TL1 51.650	CTW1 66.430	DTW1 14.780	H1 1497.77	
		TW3 70.000	TL3 52.350	CTW3 68.230	DTW3 15.880	H3 1394.02	
		AVGTW= 67.180		AVGDTW= 15.296		AVGH= 1447.18	
107	26055.98	TWO 70.000	TLO 51.650	CTWO 67.916	DTWO 16.266	HO 1601.77	
		TW1 68.650	TL1 51.650	CTW1 66.566	DTW1 14.916	H1 1746.74	
		TW3 71.150	TL3 52.350	CTW3 69.066	DTW3 16.716	H3 1558.66	
		AVGTW= 67.850		AVGDTW= 15.966		AVGH= 1631.87	
108	33893.13	TWO 71.700	TLO 51.650	CTWO 68.990	DTWO 17.340	HO 1954.57	
		TW1 70.325	TL1 51.650	CTW1 67.615	DTW1 15.965	H1 2122.91	
		TW3 72.750	TL3 52.350	CTW3 70.040	DTW3 17.690	H3 1915.90	
		AVGTW= 68.882		AVGDTW= 16.998		AVGH= 1993.86	

TABLE B-3 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING ETHANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	LIQUID TEMPERATURE DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
		P=19.33 KN/SQ.M			TS=41.25 DEG.C	
109	6870.23	TWO 53.750	TL0 40.950	CTWO 53.200	DTWO 12.250	HO 560.80
		TW1 52.800	TL1 40.950	CTW1 52.250	DTW1 11.300	H1 607.94
		TW3 56.050	TL3 41.675	CTW3 55.500	DTW3 13.825	H3 496.92
		AVGTW= 53.650		AVGDTW= 12.459		AVGH= 551.42
110	11755.73	TWO 56.550	TL0 40.950	CTWO 55.610	DTWO 14.660	HO 801.88
		TW1 55.500	TL1 40.950	CTW1 54.560	DTW1 13.610	H1 863.74
		TW3 58.875	TL3 41.675	CTW3 57.935	DTW3 16.260	H3 722.97
		AVGTW= 56.035		AVGDTW= 14.843		AVGH= 791.98
111	16539.44	TWO 58.075	TL0 40.950	CTWO 56.752	DTWO 15.802	HO 1046.62
		TW1 57.000	TL1 40.950	CTW1 55.677	DTW1 14.727	H1 1123.01
		TW3 61.175	TL3 41.675	CTW3 59.852	DTW3 18.177	H3 909.87
		AVGTW= 57.427		AVGDTW= 16.236		AVGH= 1018.68
112	22137.40	TWO 59.400	TL0 40.950	CTWO 57.630	DTWO 16.680	HO 1327.16
		TW1 58.075	TL1 40.950	CTW1 56.305	DTW1 15.355	H1 1441.69
		TW3 63.700	TL3 41.675	CTW3 61.930	DTW3 20.255	H3 1092.92
		AVGTW= 58.621		AVGDTW= 17.430		AVGH= 1270.06
113	26055.98	TWO 60.700	TL0 40.950	CTWO 58.616	DTWO 17.666	HO 1474.84
		TW1 59.350	TL1 40.950	CTW1 57.266	DTW1 16.316	H1 1596.87
		TW3 65.000	TL3 41.675	CTW3 62.916	DTW3 21.240	H3 1226.63
		AVGTW= 59.600		AVGDTW= 18.408		AVGH= 1475.42
114	33893.13	TWO 63.000	TL0 40.950	CTWO 60.290	DTWO 19.340	HO 1752.45
		TW1 60.950	TL1 40.950	CTW1 58.240	DTW1 17.290	H1 1960.23
		TW3 65.500	TL3 41.675	CTW3 62.790	DTW3 21.115	H3 1605.14
		AVGTW= 60.440		AVGDTW= 19.248		AVGH= 1760.80

TABLE B-4 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING METHANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
		p=98.64 KN/SQ.M			TS=64.00 DEG.C	
115	6870.23	TWO 72.600	TL0 64.450	CTWO 72.050	DTWO 7.600	HO 903.89
		TW1 71.300	TL1 64.450	CTW1 70.750	DTW1 6.300	H1 1090.38
		TW3 74.250	TL3 65.150	CTW3 73.700	DTW3 8.550	H3 803.46
		AVGTW= 72.167		AVGDTW= 7.484		AVGH= 917.98
116	11755.73	TWO 74.250	TL0 64.450	CTWO 73.310	DTWO 8.860	HO 1326.80
		TW1 73.800	TL1 64.450	CTW1 72.860	DTW1 8.410	H1 1397.80
		TW3 75.650	TL3 65.150	CTW3 74.710	DTW3 9.560	H3 1229.65
		AVGTW= 73.626		AVGDTW= 8.943		AVGH=1314.44
117	16539.44	TWO 75.650	TL0 64.600	CTWO 74.327	DTWO 9.727	HO 1700.23
		TW1 75.400	TL1 64.600	CTW1 74.077	DTW1 9.477	H1 1745.08
		TW3 76.850	TL3 65.250	CTW3 75.527	DTW3 10.277	H3 1609.25
		AVGTW= 74.644		AVGDTW= 9.827		AVGH=1682.93
118	22137.40	TWO 77.300	TL0 64.600	CTWO 75.530	DTWO 10.930	HO 2025.34
		TW1 76.850	TL1 64.600	CTW1 75.080	DTW1 10.480	H1 2112.30
		TW3 78.400	TL3 65.275	CTW3 76.630	DTW3 11.355	H3 1949.53
		AVGTW= 75.746		AVGDTW= 10.921		AVGH=2026.88
119	26055.98	TWO 78.100	TL0 64.600	CTWO 76.016	DTWO 11.416	HO 2282.22
		TW1 77.875	TL1 64.600	CTW1 75.791	DTW1 11.191	H1 2328.10
		TW3 79.575	TL3 65.275	CTW3 77.491	DTW3 12.216	H3 2132.77
		AVGTW= 76.433		AVGDTW= 11.608		AVGH=2244.54
120	23893.13	TWO 79.500	TL0 64.600	CTWO 76.790	DTWO 12.190	HO 2780.31
		TW1 79.425	TL1 64.500	CTW1 76.715	DTW1 12.115	H1 2797.52
		TW3 81.475	TL3 65.275	CTW3 78.765	DTW3 13.490	H3 2512.39
		AVGTW= 77.423		AVGDTW= 12.598		AVGH=2690.20

TABLE E-4 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING METHANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
		p=79.98 KN/SQ.M			TS=58.75 DEG.C	
121	6870.23	TWO 67.850	TLO 58.750	CTWO 67.300	DTWO 8.550	HO 803.46
		TW1 65.650	TL1 58.750	CTW1 65.100	DTW1 6.350	H1 1081.80
		TW3 70.450	TL3 59.200	CTW3 69.900	DTW3 10.700	H3 642.03
		AVGTW= 67.434		AVGDTW= 8.534		AVGH= 805.03
122	11755.73	TWO 70.095	TLO 58.750	CTWO 69.155	DTWO 10.405	HO 1129.79
		TW1 68.300	TL1 58.750	CTW1 67.360	DTW1 8.610	H1 1365.33
		TW3 71.100	TL3 59.200	CTW3 70.160	DTW3 10.960	H3 1072.58
		AVGTW= 68.891		AVGDTW= 9.991		AVGH=1176.53
123	16539.44	TWO 71.275	TLO 58.750	CTWO 69.952	DTWO 11.202	HO 1476.37
		TW1 69.800	TL1 58.750	CTW1 68.477	DTW1 9.727	H1 1700.23
		TW3 72.600	TL3 59.200	CTW3 71.277	DTW3 12.077	H3 1369.41
		AVGTW= 69.902		AVGDTW= 11.002		AVGH=1503.21
124	22137.40	TWO 72.600	TLO 58.750	CTWO 70.830	DTWO 12.080	HO 1832.53
		TW1 71.450	TL1 58.750	CTW1 69.680	DTW1 10.930	H1 2025.34
		TW3 73.750	TL3 59.200	CTW3 71.980	DTW3 12.780	H3 1732.16
		AVGTW= 70.830		AVGDTW= 11.930		AVGH=1855.57
125	26055.98	TWO 73.775	TLO 58.750	CTWO 71.691	DTWO 12.941	HO 2013.30
		TW1 72.370	TL1 58.750	CTW1 70.286	DTW1 11.536	H1 2258.48
		TW3 75.125	TL3 59.200	CTW3 73.041	DTW3 13.841	H3 1882.39
		AVGTW= 71.673		AVGDTW= 12.773		AVGH=2039.83
126	33893.13	TWO 74.650	TLO 58.750	CTWO 71.940	DTWO 13.190	HO 2569.53
		TW1 74.100	TL1 58.750	CTW1 71.390	DTW1 12.640	H1 2681.33
		TW3 76.970	TL3 59.200	CTW3 74.260	DTW3 15.060	H3 2250.48
		AVGTW= 72.530		AVGDTW= 13.630		AVGH=2486.58

TABLE B-4 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING METHANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
		p=66.65 KN/SQ.M			TS=54.80 DEG.C	
127	6870.23	TWO 65.550	TLO 54.675	CTWO 65.000	DTWO 10.325	HO 665.35
		TW1 62.600	TL1 54.675	CTW1 62.050	DTW1 7.375	H1 931.46
		TW3 67.350	TL3 55.350	CTW3 66.800	DTW3 11.450	H3 599.98
		AVGTW= 64.617		AVGDTW= 9.717		AVGH= 707.00
123	11755.73	TWO 66.700	TLO 54.675	CTWO 65.760	DTWO 11.085	HO 1060.49
		TW1 64.920	TL1 54.675	CTW1 63.980	DTW1 9.305	H1 1263.35
		TW3 68.050	TL3 55.350	CTW3 67.110	DTW3 11.760	H3 999.62
		AVGTW= 65.616		AVGDTW= 10.716		AVGH=1096.94
129	16539.44	TWO 67.850	TLO 54.675	CTWO 66.527	DTWO 11.852	HO 1395.41
		TW1 66.300	TL1 54.675	CTW1 64.977	DTW1 10.302	H1 1605.34
		TW3 69.750	TL3 55.350	CTW3 68.427	DTW3 13.077	H3 1264.70
		AVGTW= 66.644		AVGDTW= 11.744		AVGH=1408.28
130	22137.40	TWO 69.450	TLO 54.675	CTWO 67.680	DTWO 13.005	HO 1702.19
		TW1 68.100	TL1 54.675	CTW1 66.330	DTW1 11.655	H1 1899.35
		TW3 70.800	TL3 55.350	CTW3 69.030	DTW3 13.680	H3 1618.20
		AVGTW= 67.680		AVGDTW= 12.780		AVGH=1732.16
131	26055.98	TWO 70.700	TLO 54.675	CTWO 68.616	DTWO 13.941	HO 1868.89
		TW1 68.800	TL1 54.675	CTW1 66.716	DTW1 12.041	H1 2163.77
		TW3 72.150	TL3 55.350	CTW3 70.066	DTW3 14.716	H3 1770.47
		AVGTW= 68.466		AVGDTW= 13.566		AVGH=1920.55
132	33893.13	TWO 71.695	TLO 54.675	CTWO 68.985	DTWO 14.310	HO 2368.42
		TW1 70.800	TL1 54.675	CTW1 68.090	DTW1 13.415	H1 2526.43
		TW3 74.200	TL3 55.350	CTW3 71.490	DTW3 16.140	H3 2099.89
		AVGTW= 69.522		AVGDTW= 14.622		AVGH=2317.94

TABLE B-4 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING METHANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K	
		p=53.32 KN/SQ.M			TS=50.00 DEG.C		
133	6870.23	TWO 61.850	TLO 50.200	CTWO 61.300	DTWO 11.100	HO 618.90	
		TW1 58.650	TL1 50.200	CTW1 58.100	DTW1 7.900	H1 869.57	
		TW3 63.250	TL3 50.700	CTW3 62.700	DTW3 12.000	H3 572.48	
		AVGTW= 60.700		AVGDTW= 10.334		AVGH= 664.81	
134	11755.73	TWO 63.600	TLO 50.200	CTWO 62.660	DTWO 12.460	HO 943.46	
		TW1 61.065	TL1 50.200	CTW1 60.125	DTW1 9.925	H1 1184.43	
		TW3 64.695	TL3 50.700	CTW3 63.755	DTW3 13.055	H3 900.46	
		AVGTW= 62.180		AVGDTW= 11.813		AVGH= 995.11	
135	16539.44	TWO 64.650	TLO 50.200	CTWO 63.327	DTWO 13.127	HO 1259.88	
		TW1 62.425	TL1 50.200	CTW1 61.102	DTW1 10.902	H1 1517.00	
		TW3 66.125	TL3 50.700	CTW3 64.802	DTW3 14.102	H3 1172.78	
		AVGTW= 63.077		AVGDTW= 12.711		AVGH=1301.18	
136	22137.40	TWO 66.450	TLO 50.200	CTWO 64.680	DTWO 14.480	HO 1528.80	
		TW1 64.175	TL1 50.200	CTW1 62.405	DTW1 12.205	H1 1813.76	
		TW3 67.800	TL3 50.700	CTW3 66.030	DTW3 15.330	H3 1444.04	
		AVGTW= 64.371		AVGDTW= 14.005		AVGH=1580.65	
137	26055.98	TWO 67.050	TLO 50.200	CTWO 64.966	DTWO 14.766	HO 1764.48	
		TW1 64.700	TL1 50.200	CTW1 62.616	DTW1 12.416	H1 2098.42	
		TW3 68.500	TL3 50.700	CTW3 66.416	DTW3 15.716	H3 1657.83	
		AVGTW= 64.666		AVGDTW= 14.300		AVGH=1822.06	
138	33893.13	TWO 68.825	TLO 50.200	CTWO 66.115	DTWO 15.915	HO 2129.58	
		TW1 66.750	TL1 50.200	CTW1 64.040	DTW1 13.840	H1 2448.85	
		TW3 70.800	TL3 50.700	CTW3 68.090	DTW3 17.390	H3 1948.95	
		AVGTW= 66.082		AVGDTW= 15.715		AVGH=2156.68	

TABLE B-4 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING METHANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	LIQUID TEMP DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
		P=41.32 KN/SQ.M		TS=44.00 DEG.C		
139	6870.23	TWO 57.950	TL0 44.400	CTWO 57.400	DTWO 13.000	HO 528.45
		TW1 53.550	TL1 44.400	CTW1 53.000	DTW1 8.600	H1 798.79
		TW3 59.325	TL3 45.000	CTW3 58.775	DTW3 13.775	H3 498.72
		AVGTW= 56.392		AVGDTW= 11.792		AVGH= 582.60
140	11755.73	TWO 58.245	TL0 44.400	CTWO 57.305	DTWO 12.905	HO 910.93
		TW1 56.345	TL1 44.400	CTW1 55.405	DTW1 11.005	H1 1068.20
		TW3 60.000	TL3 45.000	CTW3 59.060	DTW3 14.060	H3 836.10
		AVGTW= 57.256		AVGDTW= 12.656		AVGH= 928.80
141	16539.44	TWO 60.350	TL0 44.400	CTWO 59.027	DTWO 14.627	HO 1130.69
		TW1 57.575	TL1 44.400	CTW1 56.252	DTW1 11.852	H1 1395.41
		TW3 62.125	TL3 45.000	CTW3 60.802	DTW3 15.802	H3 1046.62
		AVGTW= 58.694		AVGDTW= 14.094		AVGH= 1173.47
142	22137.40	TWO 62.100	TL0 44.400	CTWO 60.330	DTWO 15.930	HO 1389.65
		TW1 59.400	TL1 44.400	CTW1 57.630	DTW1 13.230	H1 1673.24
		TW3 63.650	TL3 45.000	CTW3 61.880	DTW3 16.880	H3 1311.44
		AVGTW= 59.946		AVGDTW= 15.346		AVGH= 1442.47
143	26055.98	TWO 62.800	TL0 44.400	CTWO 60.716	DTWO 16.316	HO 1596.87
		TW1 59.720	TL1 44.400	CTW1 57.636	DTW1 13.236	H1 1968.43
		TW3 64.400	TL3 45.000	CTW3 62.316	DTW3 17.316	H3 1504.65
		AVGTW= 60.223		AVGDTW= 15.623		AVGH= 1667.73
144	33893.13	TWO 64.820	TL0 44.400	CTWO 62.110	DTWO 17.710	HO 1913.74
		TW1 62.120	TL1 44.400	CTW1 59.410	DTW1 15.010	H1 2257.97
		TW3 67.220	TL3 45.000	CTW3 64.510	DTW3 19.510	H3 1737.18
		AVGTW= 62.010		AVGDTW= 17.410		AVGH= 1946.72



TABLE B-4 EXPERIMENTAL DATA OF HEAT TRANSFER TO BOILING METHANOL

RUN NO.	HEAT FLUX W/SQ.M	TEMPERATURE SURFACE DEG.C	TEMPERATURE LIQUID DEG.C	CORRECTED TW DEG.C	CORRECTED DTW DEG.C	TRANSFER COEFFICIENT W/SQ.M K
		p=27.99 KN/SQ.M		TS=36.00 DEG.C		
145	6870.23	TWO 50.200	TL0 36.150	CTWO 49.650	DTWO 13.500	HO 508.88
		TW1 46.600	TL1 36.150	CTW1 46.050	DTW1 9.900	H1 693.91
		TW3 52.600	TL3 36.650	CTW3 52.050	DTW3 15.400	H3 446.10
		AVGTW= 49.250		AVGDTW= 12.934		AVGH= 531.17
146	1755.73	TWO 51.595	TL0 36.150	CTWO 50.655	DTWO 14.505	HO 810.45
		TW1 48.745	TL1 36.150	CTW1 47.805	DTW1 11.655	H1 1008.63
		TW3 53.075	TL3 36.650	CTW3 52.135	DTW3 15.485	H3 759.16
		AVGTW= 50.198		AVGDTW= 13.881		AVGH= 846.84
147	16539.44	TWO 53.275	TL0 36.150	CTWO 51.952	DTWO 15.802	HO 1046.62
		TW1 50.375	TL1 36.150	CTW1 49.052	DTW1 12.902	H1 1281.85
		TW3 55.150	TL3 36.650	CTW3 53.827	DTW3 17.177	H3 962.84
		AVGTW= 51.611		AVGDTW= 15.294		AVGH= 1081.40
148	22137.40	TWO 54.825	TL0 36.150	CTWO 53.055	DTWO 16.905	HO 1309.50
		TW1 51.925	TL1 36.150	CTW1 50.155	DTW1 14.005	H1 1580.65
		TW3 56.625	TL3 36.650	CTW3 54.855	DTW3 18.205	H3 1215.99
		AVGTW= 52.688		AVGDTW= 16.371		AVGH= 1352.16
149	26055.98	TWO 56.050	TL0 36.150	CTWO 53.966	DTWO 17.816	HO 1462.43
		TW1 53.200	TL1 36.150	CTW1 51.116	DTW1 14.966	H1 1740.90
		TW3 58.050	TL3 36.650	CTW3 55.966	DTW3 19.316	H3 1348.87
		AVGTW= 53.683		AVGDTW= 17.366		AVGH= 1500.32

## C.3 ETHANOL

## Surface Tension

The following linear relationships correlate the surface tension of ethanol with saturation temperature:

For temperature range  $0^{\circ}\text{C} - 90^{\circ}\text{C}$

$$\sigma = 245.25454\text{E-}04 - 894.54545\text{E-}07*\text{TS}$$

For temperature range  $90^{\circ}\text{C} - 230^{\circ}\text{C}$

$$\sigma = 267.67141\text{E-}04 - 111.57142\text{E-}06*\text{TS}$$

where  $\sigma$  has the units of N/m

## Thermal Conductivity

The relationships of the following form have been obtained for the thermal conductivity of ethanol:

For temperature range  $0^{\circ}\text{C} - 110^{\circ}\text{C}$

$$k_{\ell} = 170.79485\text{E-}03 - 897.17142\text{E-}07*\text{TS}$$

For temperature range  $110^{\circ}\text{C} - 243^{\circ}\text{C}$

$$k_{\ell} = -0.57007\text{E+}00 + 0.18558\text{E-}01*\text{TS} - 0.17283\text{E-}03*(\text{TS}^{**2},) \\ + 0.70115\text{E-}06*(\text{TS}^{**3},) - 0.10648\text{E-}08*(\text{TS}^{**4},)$$

Where  $k_{\ell}$  has the units of W/m K

## Latent Heat

The following equations have been obtained to correlate latent heat:

For temperature range  $0^{\circ}\text{C} - 90^{\circ}\text{C}$

$$\lambda = 0.10485\text{E+}07 - 0.10294\text{E+}04*\text{TS} + 0.92875\text{E+}01*(\text{TS}^{**2},) \\ - 0.19893\text{E+}00*(\text{TS}^{**3},) + 0.89102\text{E-}03*(\text{TS}^{**4},)$$

## A P P E N D I X C

### PROPERTY ESTIMATION METHODS

Properties of pure liquids : distilled water, isopropanol, ethanol and methanol are readily available in literature [11], [125-134] as a function of temperature and pressure in tabular forms. However, these properties are either available in FPS or in CGS or in MKS system of units. Storing these vast number of data for computer calculations, a large amount of memory space is required. Therefore, these data were first converted in SI units and then suitable equations were obtained to express these properties as a function of saturation temperature,  $T_S$ , in degree centigrade. Method of least squares was employed to develop these equations. These equations were the basis for a subroutine which was incorporated into the main program for the calculation of these properties. Computer programs in Fortran IV were executed on IBM 360/Model 44 computer.

#### C.1 DISTILLED WATER

##### Surface Tension

The equations for surface tension of distilled water were obtained from the straight line fit of the available data. The form of correlations are:

For temperature range  $0^{\circ}\text{C} - 110^{\circ}\text{C}$

$$\sigma = 761.30636\text{E}-04 - 170.67825\text{E}-06 * T_S$$

For temperature range  $110^{\circ}\text{C} - 310^{\circ}\text{C}$

$$\sigma = 826.90126\text{E-}04 - 226.43082\text{E-}06 * \text{TS}$$

where  $\sigma$  has the units of N/m.

Thermal Conductivity

The following polynomial equations were obtained for correlating thermal conductivity of distilled water:

For temperature range  $0^{\circ}\text{C} - 110^{\circ}\text{C}$

$$k_{\ell} = 0.55081\text{E}+00 + 0.26386\text{E-}02 * \text{TS} - 0.13691\text{E-}04 * (\text{TS}^{**2}) \\ - 0.15631\text{E-}07 * (\text{TS}^{**3}) + 0.20796\text{E-}09 * (\text{TS}^{**4})$$

For temperature range  $110^{\circ}\text{C} - 310^{\circ}\text{C}$

$$k_{\ell} = 0.60666\text{E}+00 + 0.12652\text{E-}02 * \text{TS} - 0.54635\text{E-}05 * (\text{TS}^{**2},) \\ + 0.46741\text{E-}08 * (\text{TS}^{**3},) - 0.98305\text{E-}11 * (\text{TS}^{**4},)$$

where  $k_{\ell}$  has the units of W/m K

Latent Heat

The equations obtained for the latent heat are of the following form:

For temperature range  $0^{\circ}\text{C} - 100^{\circ}\text{C}$

$$\lambda = 0.25009\text{E}+07 - 0.23655\text{E}+04 * \text{TS} + 0.63545\text{E}+00 * (\text{TS}^{**2},0) \\ - 0.16820\text{E-}01 * (\text{TS}^{**3},) + 0.28206\text{E-}04 * (\text{TS}^{**4},)$$

For temperature range  $100^{\circ} - 300^{\circ}\text{C}$

$$\lambda = 0.24259\text{E}+07 - 0.55119\text{E}+03 * \text{TS} - 0.15886\text{E}+02 * (\text{TS}^{**2},) \\ + 0.55052\text{E-}01 * (\text{TS}^{**3},) - 0.11262\text{E-}03 * (\text{TS}^{**4},)$$

where  $\lambda$  has the units of J/kg.

## Specific Heat

Following relationships have been obtained for correlating specific heat of distilled water with saturation temperature:

For temperature range  $0^{\circ}\text{C} - 110^{\circ}\text{C}$

$$C_{\ell} = 0.42112\text{E}+04 - 0.21366\text{E}+01*\text{TS} + 0.35700\text{E}-01*(\text{TS}**2.) \\ - 0.16983\text{E}-03*(\text{TS}**3.) + 0.35052\text{E}-06*(\text{TS}**4.)$$

For temperature range  $110^{\circ}\text{C} - 310^{\circ}\text{C}$

$$C_{\ell} = 0.76008\text{E}+04 - 0.79556\text{E}+02*\text{TS} + 0.67767\text{E}+00*(\text{TS}**2.) \\ - 0.24695\text{E}-02*(\text{TS}**3.) + 0.34187\text{E}-05*(\text{TS}**4.)$$

Where  $C_{\ell}$  has the units of J/kg K

## Liquid Density

The following polynomials relate liquid density as a function of saturation temperature for different range of temperatures:

For temperature range  $0^{\circ}\text{C} - 110^{\circ}\text{C}$

$$\rho_{\ell} = 0.99991\text{E}+03 + 0.42965\text{E}-01*\text{TS} - 0.70786\text{E}-02*(\text{TS}**2.) \\ + 0.34295\text{E}-04*(\text{TS}**3.) - 0.93198\text{E}-07*(\text{TS}**4.)$$

For temperature range  $110^{\circ}\text{C} - 310^{\circ}\text{C}$

$$\rho_{\ell} = 0.96214\text{E}+03 + 0.8393\text{E}+00*\text{TS} - 0.12197\text{E}-01*(\text{TS}**2.) \\ + 0.39162\text{E}-04*(\text{TS}**3.) - 0.56920\text{E}-07*(\text{TS}**4.)$$

Where  $\rho_{\ell}$  has the units of  $\text{kg}/\text{m}^3$

### Vapour Density

The equations obtained for the vapour density are of the following form:

For temperature range  $0^{\circ}\text{C} - 110^{\circ}\text{C}$

$$\rho_v = 0.52558\text{E}-02 + 0.17461\text{E}-03*\text{TS} + 0.21264\text{E}-04*(\text{TS}**2.) \\ - 0.10163\text{E}-06*(\text{TS}**3.) + 0.46442\text{E}-08*(\text{TS}**4.)$$

For temperature range  $110^{\circ}\text{C} - 310^{\circ}\text{C}$

$$\rho_v = 0.28603\text{E}+02 - 0.66988\text{E}+00*\text{TS} + 0.58191\text{E}-02*(\text{TS}**2.) \\ - 0.22209\text{E}-04*(\text{TS}**3.) + ( 0.36374\text{E}-07*(\text{TS}**4.)$$

where  $\rho_v$  has the units of  $\text{kg}/\text{m}^3$

### Vapour Pressure

The following polynomial was obtained for correlating vapour pressure with saturation temperature,

For temperature range  $0^{\circ}\text{C} - 101^{\circ}\text{C}$

$$P = 0.68877\text{E}+03 + 0.10886\text{E}+02*\text{TS} + 0.39057\text{E}+01*(\text{TS}**2.) \\ - 0.38904\text{E}-01(\text{TS}**3.) + 0.99335\text{E}-03*(\text{TS}**4.)$$

Where P has the units of  $\text{N}/\text{m}^2$

### Viscosity

The viscosity data have been correlated by the following fifth order polynomials:

For Temperature range  $0^{\circ}\text{C} - 110^{\circ}\text{C}$

$$\mu_f = [179.33352\text{E}+01 - 621.36517\text{E}-01*\text{TS} + 149.86551\text{E}-02*(\text{TS}**2.) \\ - 224.41365\text{E}-04*(\text{TS}**3.) + 175.34761\text{E}-06*(\text{TS}**4.) - \\ - 536.58698\text{E} - 09*(\text{TS}**5.)] * 10^{-6}$$

For temperature range  $110^{\circ}\text{C} - 310^{\circ}\text{C}$

$$\mu_{\ell} = [635.35320\text{E}+00 - 471.85935\text{E}-02*\text{TS} + 100.70339\text{E}-04*(\text{TS}**2.) \\ + 278.65450\text{E}-07*(\text{TS}**3.) - 144.57533\text{E}-09*(\text{TS}**4.) \\ + 157.95537\text{E}-12*(\text{TS}**5.)] *10^{-6}$$

Where  $\mu_{\ell}$  has the units of  $\text{N s/m}^2$

## C.2 ISOPROPANOL

### Surface Tension

Surface tension of isopropanol is obtained as a linear relationship with saturation temperature:

For temperature range  $0^{\circ}\text{C} - 100^{\circ}\text{C}$

$$\sigma = 254.45449\text{E}-04 - 830.90818\text{E}-07*\text{TS}$$

where  $\sigma$  has the units of  $\text{N/m}$

### Thermal Conductivity

The following linear relationship relates the thermal conductivity as follows:

For temperature range  $0 - 85^{\circ}\text{C}$

$$k_{\ell} = 153.63230\text{E}-03 - 158.16800\text{E}-06*\text{TS}$$

where  $k_{\ell}$  has the units of  $\text{W/m K}$

### Latent Heat

The values of latent heat of isopropanol between temperature range  $30.2^{\circ}\text{C}$  to  $82.6^{\circ}\text{C}$  has been obtained by the application of Clausius-Clapeyron equation. These

values then have been converted in SI units and used in obtaining a Polynomial of fifth order which relates the latent heat of isopropanol with saturation temperature as follows:

For temperature range  $30.2^{\circ}\text{C} - 82.6^{\circ}\text{C}$

$$\lambda = 203.03796\text{E}+04 - 480.80087\text{E}+02 * \text{TS} + 456.30770\text{E}+00 * (\text{TS}^{**2}.) \\ - 359.94529\text{E}-03 * (\text{TS}^{**3}.) + 243.95033\text{E} - 04 * (\text{TS}^{**4}) \\ - 379.12940\text{E}-06 * (\text{TS}^{**5}.)$$

where  $\lambda$  has the units of J/kg.

#### Specific Heat

The following linear relationship has been obtained for the specific heat for temperature range of  $0^{\circ}\text{C}$  to  $85^{\circ}\text{C}$ ,

$$C_{\ell} = 243.92761\text{E}+01 + 126.03376\text{E}-01 * \text{TS}$$

where  $C_{\ell}$  has the units of J/kg K

#### Liquid Density

Liquid density of isopropanol is available only upto a temperature range of  $0^{\circ}\text{C}$  to  $30^{\circ}\text{C}$ . A plot between liquid density and temperature is a linear relationship and it shows that the values can be extrapolated upto  $90^{\circ}\text{C}$ .

The form of the equation is

$$\rho_{\ell} = 801.27856\text{E}+00 - 811.71419\text{E}-03 * \text{TS}$$

where  $\rho_{\ell}$  has the units of  $\text{kg}/\text{m}^3$

#### Vapour Density

The vapour density of isopropanol in the temperature range  $2.40^{\circ}\text{C} - 82.5^{\circ}\text{C}$  has been calculated by using ideal gas



law. These values then converted into SI units and a fifth order polynomial of the following form has been obtained:

$$\rho_v = 288.90611E-04 + 255.00299E-05*TS - 975.27464E-08*(TS**2.) \\ + 419.90463E-08*(TS**3.) - 420.65384E-10*(TS**4.) \\ + 386.78963E-12*(TS**5.)$$

where  $\rho_v$  has the units of  $\text{kg/m}^3$ .

#### Vapour Pressure

Following is the equation for vapour pressure :

For temperature range  $-26.1^\circ\text{C} - 82.5^\circ\text{C}$

$$P = 0.22520E+04 - 0.31228E+03*TS + 0.20468E+02*(TS**2.) \\ - 0.26690E+00*(TS**3.) + 0.29200E-02*(TS**4.)$$

where P has the units of  $\text{N/m}^2$

#### Viscosity

The viscosity data have been correlated by the following fifth order polynomials :

For temperature range  $0^\circ\text{C} - 120^\circ\text{C}$

$$\mu_l = 459.10201E-05 - 156.16738E-06*TS + 280.63930E-08*(TS**2.) \\ - 297.86025E-10*(TS**3.) + 172.56563E-12*(TS**4.) \\ - 413.69649E-15*(TS**5.)$$

For temperature range  $120^\circ\text{C} - 230^\circ\text{C}$

$$\mu_l = 130.98034E-05 - 117.39022E-07*TS - 438.09089E-11*(TS**2.) \\ + 459.53980E-12*(TS**3.) - 199.85684E-14*(TS**4.) \\ + 261.14554E-17*(TS**5.)$$

where  $\mu_l$  has the units of  $\text{N s/m}^2$

For temperature range  $90^{\circ}\text{C} - 230^{\circ}\text{C}$

$$\lambda = 0.96103\text{E}+06 + 0.25716\text{E}+04*\text{TS} - 0.47834\text{E}+02*(\text{TS}**2,) \\ + 0.24525\text{E}+00*(\text{TS}**3,) - 0.57849\text{E} - 03*(\text{TS}**4,)$$

Where  $\lambda$  has the units of J/kg

#### Specific Heat

The specific heat is represented by the following fourth order polynomial:

For temperature range  $0^{\circ}\text{C} - 140^{\circ}\text{C}$

$$C_{\ell} = .22663\text{E} + 04 + 0.58808\text{E}+01*\text{TS} + 0.47357\text{E}-01*(\text{TS}**2,) \\ - 0.29583\text{E}-04*(\text{TS}**3,) + 0.51473\text{E}-07*(\text{TS}**4,)$$

where  $C_{\ell}$  has the units of J/kg K

#### Liquid Density

The following polynomials relate liquid density of ethanol as a function of saturation temperature for different range of temperatures:

For temperature range  $2.8^{\circ}\text{C} - 95.6^{\circ}\text{C}$

$$\rho_{\ell} = 0.82547\text{E}+03 - 0.97801\text{E}+00*\text{TS} + 0.93018\text{E}-02*(\text{TS}**2) \\ - 0.18321\text{E}-03*(\text{TS}**3,) + 0.98893\text{E}-06*(\text{TS}**4,)$$

For temperature range  $95.6^{\circ}\text{C} - 246.4^{\circ}\text{C}$

$$\rho_{\ell} = -0.28369\text{E}+03 + 0.29204\text{E}+02*\text{TS} - 0.29719\text{E}+00*(\text{TS}**2,) \\ + 0.12670\text{E} - 02*(\text{TS}**3,) - 0.20228\text{E}-05*(\text{TS}**4,)$$

Where  $\rho_{\ell}$  has the units of  $\text{kg}/\text{m}^3$

### Vapour Density

The equations obtained for the vapour density are of the following form:

For temperature range  $2.8^{\circ}\text{C} - 95.6^{\circ}\text{C}$

$$\rho_v = 0.41022\text{E}-01 - 0.18142\text{E}-02*\text{TS} + 0.28808\text{E}-03*(\text{TS}**2.) \\ - 0.37326\text{E}-05*(\text{TS}**3.) + 0.42259\text{E}-07*(\text{TS}**4.)$$

For temperature range  $95.6^{\circ}\text{C} - 246.4^{\circ}\text{C}$

$$\rho_v = 0.96346\text{E}+03 - 0.26052\text{E}+02*\text{TS} + 0.25854\text{E}+00*(\text{TS}**2.) \\ - 0.11170\text{E}-02*(\text{TS}**3.) + 0.18016\text{E}-05*(\text{TS}**4.)$$

where  $\rho_v$  has the units of  $\text{kg/m}^3$

### Vapour Pressure

The following form of the polynomial was obtained for correlating vapour pressure of ethanol with saturation temperature:

For temperature range  $-31.3^{\circ}\text{C} - 87.4^{\circ}\text{C}$

$$P = 0.44420\text{E}+03 + 0.40266\text{E}+03*\text{TS} - 0.28843\text{E}+02*(\text{TS}**2.) \\ + 0.91876\text{E}+00*(\text{TS}**3.) - 0.56114\text{E}-02*(\text{TS}**4.)$$

Where P has the units of  $\text{N/m}^2$

### Viscosity

The viscosity data have been correlated by the following fifth order polynomials:

For temperature range 0°C - 70°C

$$\begin{aligned} \mu_{\ell} = & 177.35584E-03 - 332.62798E-05*TS + 190.25797E-07*(TS**2.) \\ & + 420.43859E-09*(TS**3.) - 921.65497E-11*(TS**4.) \\ & + 533.96415E-13*(TS**5.) \end{aligned}$$

For temperature range 70°C - 231.67°C

$$\begin{aligned} \mu_{\ell} = & 123.85988E-05 - 154.34408E-07*TS + 822.04773E-10*(TS**2.) \\ & - 228.68571E-12*(TS**3.) + 361.33156E-15*(TS**4.) \\ & - 314.72716E-18*(TS**5.) \end{aligned}$$

Where  $\mu_{\ell}$  has the units of N s/m<sup>2</sup>

#### C.4 METHANOL

##### Surface Tension

The equations for surface tension of methanol were obtained from the straight line fit of the available data. The form of correlations are:

For temperature range 0°C - 90°C

$$\sigma = 244.03636E-04 - 863.03030E-07*TS$$

For temperature range 90°C - 220°C

$$\sigma = 274.74213E-04 - 114.92071E-06*TS$$

where  $\sigma$  has the units of N/m

##### Thermal Conductivity

The following form of linear relationship was obtained for correlating thermal conductivity .

For temperature range  $0^{\circ}\text{C} - 75^{\circ}\text{C}$

$$k_{\ell} = 213.75939\text{E}-03 - 125.60384\text{E}-06*\text{TS}$$

where  $k_{\ell}$  has the units of  $\text{W/m K}$ .

Latent Heat

The polynomial obtained for the latent heat is of the following form:

For temperature range  $0^{\circ}\text{C} - 190^{\circ}\text{C}$

$$\lambda = 0.12087\text{E}+07 - 0.51348\text{E}+03* \text{TS} - 0.16398\text{E}+02*(\text{TS}**2.) \\ + 0.52303\text{E}-01*(\text{TS}**3.) - 0.14244\text{E}-03*(\text{TS}**4.)$$

Where  $\lambda$  has the units of  $\text{J/kg}$

Specific Heat

The following linear relationship was obtained for the specific heat of methanol:

For temperature range  $0^{\circ}\text{C} - 65^{\circ}\text{C}$

$$C_{\ell} = 240.78574\text{E}+01 + 457.93247\text{E}-02*\text{TS}$$

where  $C_{\ell}$  has the units of  $\text{J/kg K}$

Liquid Density

The following polynomial relates liquid density of methanol:

For temperature range  $0^{\circ}\text{C} - 190^{\circ}\text{C}$

$$\rho_{\ell} = 0.80955\text{E}+03 - 0.86131\text{E}+00*\text{TS} - 0.72658\text{E}-03*(\text{TS}**2.) \\ + 0.22534\text{E}-05*(\text{TS}**3.) - 0.44294\text{E}-07*(\text{TS}**4.)$$

where  $\rho_{\ell}$  has the units of  $\text{kg/m}^3$

### Vapour Density

The equations obtained for the vapour density are of the following form:

For temperature range 30°C - 100°C

$$\rho_v = 0.81702E-01 - 0.14616E-02*TS + 0.27308E-03*(TS**2.) \\ - 0.16417E-05*(TS**3.) + 0.29594E-07*(TS**4.)$$

For temperature range 110°C - 240°C

$$\rho_v = 0.12113E + 04 - 0.32479E+02*TS + 0.32134E+00*(TS**2) \\ - 0.13898E-02*(TS**3.) + 0.22486E-05*(TS**4.)$$

Where  $\rho_v$  has the units of kg/m<sup>3</sup>

### Vapour Pressure

The following form of the polynomials was obtained for correlating vapour pressure:

For temperature range - 44.0°C - 64.7°C

$$P = -0.21529E+04 + 0.15060E + 04*TS - 0.84399E+02*(TS**2.) \\ + 0.17112E+01*(TS**3.) - 0.58831E-02*(TS**4.)$$

where P has the units of N/m<sup>2</sup>

### Viscosity

The viscosity data have been correlated by the following fifth order polynomials.

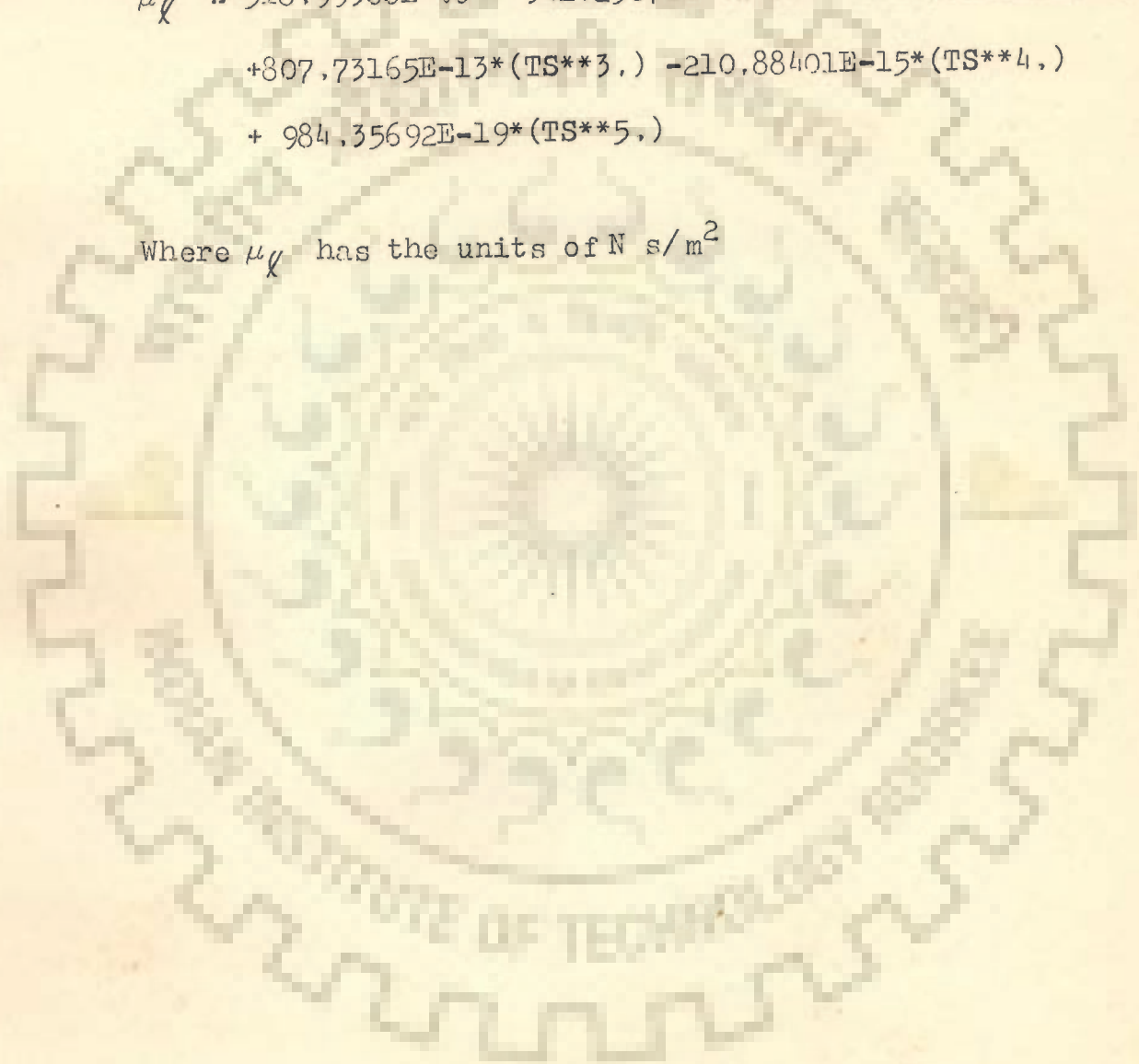
For Temperature range 0°C - 110°C

$$\mu_{\eta} = 822.70646E-06 - 384.39353E-07*TS + 174.99079E-08*(TS**2.) \\ - 373.81654E-10*(TS**3.) + 348.98035E-12*(TS**4.) - \\ - 117.53708E -14*(TS**5.)$$

For temperature range 110°C - 220°C

$$\begin{aligned}\mu_{\eta} = & 518.99366E-06 - 341.25670E-08*TS - 262.27932E-11*(TS**2,) \\ & + 807.73165E-13*(TS**3,) - 210.88401E-15*(TS**4,) \\ & + 984.35692E-19*(TS**5,)\end{aligned}$$

Where  $\mu_{\eta}$  has the units of N s/m<sup>2</sup>



## A P P E N D I X      D

### SAMPLE CALCULATIONS

Run no. 16 for distilled water is employed to demonstrate the calculational procedure. The following experimental data are taken for the run:

System pressure, P	= 47.32 kN/m <sup>2</sup>
Saturation temperature, T <sub>s</sub>	= 80.0 °C
Heat flux, q	= 16539.44 W/m <sup>2</sup>
O.D. of heating surface	= 70 mm
I.D. of heating surface	= 62 mm

Circumferential temperatures of heating surface and corresponding temperatures of fluid are:

	Temperatures, °C		
	Side	Top	Bottom
Heating surface	87.900	85.550	90.500
Test-fluid	79.900	79.900	81.450

The pertinent physico-thermal properties for distilled water at the saturation temperature (80°C) are obtained from Appendix C and are as follows:



$$\begin{aligned} \sigma &= 0.0625 \text{ N/m} & ; & \rho_{\ell} = 971.8 \text{ kg/m}^3 \\ k_{\ell} &= 0.6747 \text{ W/m } ^\circ\text{C} & ; & \rho_v = 0.2923 \text{ kg/m}^3 \\ C_{\ell} &= 4.196 \text{ kJ/kg } ^\circ\text{C} & ; & \mu_{\ell} = 0.3481 \text{ mN s/m}^2 \\ \lambda &= 2.308 \text{ MJ/kg} & ; & \alpha = 1.6546 \times 10^{-7} \text{ m}^2/\text{s} \end{aligned}$$

### SURFACE TEMPERATURE CORRECTION

For the thin walled cylinder as in the present investigation, the temperature drop across the wall is calculated by the following equation:

$$T_i - T_o = \frac{qd_o}{2k} \left( n \frac{d_o}{d_h} \right) \quad (\text{D},1)$$

Where,

$d_o$  = outside diameter of the heating surface, m

$d_h$  = inside diameter of the heating surface +

$$\frac{1}{2} (d_o - d_i)$$

$$\begin{aligned} T_i - T_o &= \frac{16539.44 \times 70 \times 10^{-3}}{2 \times 22.15 \times 1.163} \left( n \frac{70}{66} \right) \\ &= \underline{1.323} \text{ } ^\circ\text{C} \end{aligned}$$

Therefore, corrected surface temperatures are as follows:

$$T_{wo} = 87.900 - 1.323 = 86.577 \text{ } ^\circ\text{C}$$

$$T_{wl} = 85.550 - 1.323 = 84.227 \text{ } ^\circ\text{C}$$

$$T_{w3} = 90.500 - 1.323 = 89.177 \text{ } ^\circ\text{C}$$

Subscripts 0,1 and 3 represent the side, top and bottom positions of the wall thermocouples respectively.

The procedure for the calculation of point and average heat transfer coefficients is as follows:

#### AVERAGE SURFACE TEMPERATURE

Eq. (A.7) provides the calculation for average surface temperature

$$\begin{aligned}\bar{T}_w &= \frac{1}{3} [ T_{w0} + T_{w1} + T_{w3} ] && \text{(A.7)} \\ &= \frac{1}{3} [ 86,577 + 84,227 + 89,177 ] \\ &= \underline{86,660} \text{ } ^\circ\text{C}\end{aligned}$$

#### AVERAGE FLUID TEMPERATURE

$\bar{T}_f$  is calculated similar to  $\bar{T}_w$  as follows:

$$\begin{aligned}\bar{T}_f &= \frac{1}{3} [ 79,900 + 79,900 + 81,450 ] \\ &= \underline{80,416} \text{ } ^\circ\text{C}\end{aligned}$$

#### TEMPERATURE DIFFERENCE

Temperature difference at the side, at the top and at the bottom of heating surface are as follows:

$$\begin{aligned}\Delta T_0 &= 86,577 - 79,900 = 6,677 \text{ } ^\circ\text{C} \\ \Delta T_1 &= 84,227 - 79,900 = 4,327 \text{ } ^\circ\text{C} \\ \Delta T_3 &= 89,177 - 81,450 = 7,727 \text{ } ^\circ\text{C}\end{aligned}$$

and average temperature difference is

$$\begin{aligned}&\frac{1}{3} [ 6,677 + 4,327 + 7,727 ] \\ &= \underline{6,243} \text{ } ^\circ\text{C}\end{aligned}$$

## EXPERIMENTAL HEAT TRANSFER COEFFICIENT

The point values of experimental heat transfer coefficient at the side, the top, and the bottom are as follows:

$$h_o = \frac{16,539.44}{6.677} = \underline{2477.08} \text{ W/m}^2 \text{ K}$$

$$h_1 = \frac{16,539.44}{4.327} = \underline{3822.38} \text{ W/m}^2 \text{ K}$$

$$h_3 = \frac{16,539.44}{7.727} = \underline{2140.47} \text{ W/m}^2 \text{ K}$$

and average experimental heat transfer coefficient is calculated as :

$$\bar{h} = q / (\Delta T) \\ = \frac{16,539.44}{6.243} = \underline{2649.27} \text{ W/m}^2 \text{ K}$$

## WALL SUPERHEAT FROM ALAD'EV EQUATION

Theoretical wall superheat calculation is made using Alad'ev equation, Eq.(5.4) as follows:

$$\frac{\Delta T_w}{T_s} = 4.7 \times 10^{-3} \left[ \frac{10^{-6} q \lambda}{k_{\ell} T_s g} \right]^{0.3} \left[ \frac{\lambda}{C_{\ell} T_s} \right]^{1.2} \quad (5.4)$$

$$\frac{\Delta T_w}{353.0} = 4.7 \times 10^{-3} \left[ \frac{10^{-6} \times 16,539.44 \times 23.08 \times 10^5}{0.6747 \times (80+273) \times 9.81} \right]^{0.3} \times \\ \left[ \frac{23.08 \times 10^5}{4196 \times (80+273)} \right]^{1.2}$$

$$\Delta T_w = \underline{6.531} \text{ } ^\circ\text{C}$$

## BUBBLE EMISSION FREQUENCY

The frequency of bubble emission is obtained from equation, Eq.(5.7)

$$f = \frac{1}{\theta_d + \theta_w} \quad (5.7)$$

$\theta_d$  from Eq.(5.10) is:

$$\theta_d = \frac{[133.3/P]^2 [\sigma / (\rho_l - \rho_v)g]}{\pi \alpha_l J_a^2} \quad (5.10)$$

$$= \frac{[133.3/47.32]^2 [0.0625 / (971.8 - 0.2923)9.81]}{\pi \times 1.6546 \times 10^{-7} (39.47)^2}$$

$$= \underline{0.06636} \text{ s}$$

$\theta_w$  from Eq. (5.13) is:

$$\theta_w = \frac{0.867}{\alpha_l} \left[ \frac{k_l \Delta T_w}{q} \right]^2 \quad (5.13)$$

$$= \frac{0.867}{1.6546 \times 10^{-7}} \left[ \frac{0.6747 \times 6.531}{16539.44} \right]^2$$

$$= \underline{0.3793} \text{ s}$$

Therefore,

$$f = \frac{1}{0.06636 + 0.3793}$$

$$= \underline{2.243} \text{ 1/s}$$

## DETERMINATION OF CONSTANT M

For distilled water constant M is determined from Eq.(6.3a) as follows:

$$\begin{aligned}
 M &= 8.61938E-05(P)^{-4.4409803E-01} & (6.3a) \\
 &= 8.61938E-05(47.32)^{-4.4409803E-01} \\
 &= \underline{1.5545 \times 10^{-5}}
 \end{aligned}$$

HEAT TRANSFER COEFFICIENT FROM PRESENT ANALYSIS, Eq. (6.4)

Eq. (6.4) is:

$$h = M \left[ \left( \frac{\lambda^{2.5} \rho_v}{T_s^{1.5} \sigma} \right) \left( \frac{q}{k_{\ell} g} \right)^{0.3} \left( \frac{1}{C_{\ell}} \right)^{1.2} \right]^{2.33} \{f\}^{0.3683} \quad (6.4)$$

$$\begin{aligned}
 h &= 1.5545 \times 10^{-5} \left[ \left( \frac{(2308 \times 10^3)^{2.5} \times 0.2923}{(353.0)^{1.5} \times 0.0625} \right) \left( \frac{16539.44}{0.6747 \times 9.81} \right)^{0.3} \right]^{2.33} \\
 &\quad \left( \frac{1}{4196} \right)^{1.2} \left( 2.243 \right)^{0.3683}
 \end{aligned}$$

$$= \underline{2585.45 \text{ W/m}^2 \text{ K}}$$

$$\text{Deviation}^* = \frac{2649.27 - 2585.45}{2649.27} \times 100 = \underline{2.41 \%}$$

\* Deviation is calculated as percentage change with respect to the experimental value of heat transfer coefficient.

DETERMINATION OF  $M/M_1$ 

The value of  $M/M_1$  is obtained from Eq. (6.5) as follows:

$$\frac{M}{M_1} = 0.95831645 \left( \frac{P}{P_1} \right)^{-0.3997825} \quad (6.5)$$

$$= 0.95831645 \left( \frac{47.32}{98.44} \right)^{-0.3997825}$$

$$= \underline{1.284374}$$

DETERMINATION OF  $h^*/h_1^*$  FROM PRESENT ANALYSIS, Eq. (6.6)

Eq (6.6) is

$$\frac{h^*}{h_1^*} = \frac{M}{M_1} \left[ \left( \frac{\lambda}{\lambda_1} \right)^{2.5} \left( \frac{\rho_v}{\rho_{v1}} \right) \left( \frac{T_{s1}}{T_s} \right)^{1.5} \left( \frac{\sigma_1}{\sigma} \right) \left( \frac{k_{\ell 1}}{k_{\ell}} \right)^{0.3} \right.$$

$$\left. \left( \frac{q}{q_1} \right)^{0.3} \left( \frac{C_{\ell 1}}{C_{\ell}} \right)^{1.2} \left. \right\} \left. \left( \frac{f}{f_1} \right) \right]^{0.3683}$$

$$= 1.284374 \left[ \left( \frac{2308 \times 10^3}{2259 \times 10^3} \right)^{2.5} \left( \frac{0.2923}{0.5784} \right) \left( \frac{372.0}{353.0} \right)^{1.5} \left( \frac{0.05923}{0.0625} \right) \right.$$

$$\left. \left( \frac{0.6826}{0.6747} \right)^{0.3} \left( \frac{16539.44}{16539.44} \right)^{0.3} \left( \frac{4218.0}{4196.0} \right)^{1.2} \right]^{2.33} \quad \times$$

$$\left. \left( \frac{2.243}{3.59511} \right) \right]^{0.3683}$$

$$= \underline{0.7454}$$

$$\text{Deviation} = \frac{0.8160 - 0.7454}{0.8160} \times 100$$

$$= \underline{8.65\%}$$

## HEAT TRANSFER PREDICTIONS FROM OTHER CORRELATIONS

The values of experimental heat transfer coefficient during saturated boiling were compared against the predicted values by a number of other correlations.

Heat Transfer Coefficient from the Correlation of Jakob and Linke [4]

The correlation is:

$$\frac{h}{k_{\ell}} \sqrt{\frac{\sigma}{(\rho_{\ell} - \rho_v)g}} = 31.6 \left( \frac{\mu_{\ell,a}}{\mu_{\ell}} \right) \left( \frac{\rho_{\ell}}{\rho_{\ell,a}} \right) \left[ \frac{\rho_{\ell,a}}{\rho_{\ell}} \times \frac{\sigma}{\sigma_a} \times \frac{q}{\rho_{v,a} \lambda_a w_b} \right]^{0.8}$$

$$\frac{h}{0.6747} \sqrt{\frac{0.0625}{(971.8 - 0.2923)9.81}} = 31.6 \left( \frac{0.2962 \times 10^{-3}}{0.3481 \times 10^{-3}} \right) \left( \frac{971.8}{959.1} \right)$$

$$\left[ \left( \frac{959.1}{971.8} \right) \left( \frac{0.0625}{0.0592} \right) \left( \frac{16539.44}{0.5784 \times 22.59 \times 10^5 \times 0.078} \right) \right]^{0.8}$$

$$h = \underline{1682.19} \text{ W/m}^2 \text{ K}$$

$$\text{Deviation}^* = \frac{2648.67 - 1682.19}{2648.67} \times 100$$

$$= \underline{36.5\%}$$

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\* Deviation is calculated as percentage change with respect to the experimental value of heat transfer coefficient.

Heat Transfer Coefficient from the Correlation of Kutateladze  
[39]

The correlation is :

$$\frac{h}{k_{\ell}} \sqrt{\frac{\sigma}{(\rho_{\ell} - \rho_v)g}} = 7.0 \times 10^{-4} \left[ \frac{\bar{q}}{\rho_v \lambda \alpha_{\ell}} \sqrt{\frac{\sigma}{(\rho_{\ell} - \rho_v)g}} \right]^{0.7} \times \left[ \frac{P}{\sqrt{g \sigma (\rho_{\ell} - \rho_v)}} \right]^{0.7} \left( \frac{C_{\ell} \mu_{\ell}}{k_{\ell}} \right)^{-0.35}$$

$$\frac{h}{0.6747} \sqrt{\frac{0.0625}{(971.8 - 0.2923)9.81}} = 7.0 \times 10^{-4} \left[ \frac{16,539.44}{0.2923 \times 23.08 \times 10^5 \times 1.6 \times 10^7} \right]^{0.7} \times \left[ \frac{0.0625}{(971.8 - 0.2923)9.81} \right]^{0.7} \left[ \frac{47321.5}{9.81 \times 0.0625 (971.8 - 0.2923)} \right]^{0.7} \left( \frac{4196 \times 0.3481 \times 10^{-3}}{0.6747} \right)^{-0.35}$$

$$h = \underline{1795.12} \text{ W/m}^2 \text{ K}$$

$$\text{Deviation} = \frac{2648.67 - 1795.12}{2648.67} \times 100$$

$$= \underline{32.2 \%}$$



## Heat Transfer Coefficient from the Correlation of Labuntsov [36]

The correlation is:

$$\frac{h}{k_{\ell}} \sqrt{\frac{\sigma}{(\rho_{\ell} - \rho_v)g}} = 0.125 \left[ \frac{q}{\rho_v \lambda \alpha_{\ell}} \sqrt{\frac{\sigma}{(\rho_{\ell} - \rho_v)g}} \right]^{0.65} \times$$

$$\left[ \frac{C_{\ell} \mu_{\ell}}{k_{\ell}} \right]^{-0.32} \left[ \frac{(\rho_v \lambda)^2}{C_{\ell} (t_s + 273) \rho_{\ell} \sqrt{\sigma (\rho_{\ell} - \rho_v)g}} \right]^{0.35}$$

$$\frac{h}{0.6747} \sqrt{\frac{0.0625}{(971.8 - 0.2923)9.81}} = 0.125 \left[ \frac{16539.44}{0.2923 \times 23.08 \times 10^5 \times 1.6 \times 10^7} \right]^{0.65} \times$$

$$\left[ \frac{0.0625}{(971.8 - 0.2923)9.81} \right]^{-0.32} \left[ \frac{4196 \times 0.3481 \times 10^{-3}}{0.6747} \right]^{0.35}$$

$$\left[ \frac{(0.2923 \times 23.08 \times 10^5)^2}{4196(80+273) 971.8 \sqrt{0.0625(971.8 - 0.2923)9.81}} \right]^{0.35}$$

$$h = 2995.11 \text{ W/m}^2 \text{ K}$$

$$\text{Deviation} = \frac{2648.67 - 2995.11}{2648.67} \times 100$$

$$= -13.1 \%$$

Heat Transfer Coefficient from the Correlation of Kichigen and Tobilevich [39]

The correlation is :

$$\frac{h}{k_f} \sqrt{\frac{\sigma}{(\rho_f - \rho_v)g}}$$

$$= 1.04 \times 10^{-4} \left[ \frac{q}{\rho_v \lambda} \sqrt{\frac{\sigma}{(\rho_f - \rho_v)g}} \right]^{0.7} \left[ \frac{P}{\sqrt{\sigma (\rho_f - \rho_v) g}} \right]^{0.7} \quad \times$$

$$\left[ \frac{g \rho_f^2}{\mu_f^2} \left\{ \frac{\sigma}{(\rho_f - \rho_v)g} \right\}^{3/2} \left( 1 - \frac{\rho_v}{\rho_f} \right) \right]^{0.125}$$

$$\frac{h}{0.6747} \sqrt{\frac{0.0625}{(971.8 - 0.2923)9.81}} = 1.04 \times 10^{-4} \left[ \frac{16539.44}{0.2923 \times 23.08 \times 10^5 \times 1.6 \times 10^{-7}} \right]$$

$$\left[ \frac{0.0625}{(971.8 - 0.2923)9.81} \right]^{0.7} \times \left[ \frac{47321.5}{\sqrt{0.0625(971.8 - 0.2923)9.81}} \right]^{0.7} \quad \times$$

$$\left[ 9.81 \left( \frac{971.8}{0.3481 \times 10^{-3}} \right)^2 \left\{ \frac{0.0625}{(971.8 - 0.2923)9.81} \right\}^{3/2} \left( 1 - \frac{0.2923}{971.8} \right) \right]^{0.125} \quad \times$$

$$h = \underline{2027.20} \text{ W/m}^2 \text{ K}$$

$$\text{Deviation} = \frac{2648.67 - 2027.20}{2648.67} \times 100$$

$$= \underline{23.4} \%$$

Wall Heat Flux from the Correlation of Forster and Greif [33]

The correlation is:

$$q = 1.2 \times 10^{-3} \left[ \frac{\alpha_{\ell} C_{\ell} \rho_{\ell} (t_s + 273)}{\lambda \rho_v \sigma^{1/2}} \right] \left[ \frac{C_{\ell} (t_s + 273) \alpha_{\ell}^{1/2}}{(\lambda \rho_v)^2} \right]^{1/4} \times$$

$$\left[ \frac{\rho_{\ell}}{\mu_{\ell}} \right]^{5/8} \left[ \frac{\mu_{\ell} C_{\ell}}{k_{\ell}} \right]^{1/3} (\Delta P)^2$$

$$= 1.2 \times 10^{-3} \left[ \frac{1.6 \times 10^{-7} \times 4196 \times 971.8 (80 + 273)}{23.08 \times 10^5 \times 0.2923 \times \sqrt{0.0625}} \right] \times$$

$$\left[ \frac{4196 (80 + 273) \sqrt{1.6 \times 10^{-7}}}{(23.08 \times 10^5 \times 0.2923)^2} \right]^{1/4} \left[ \frac{971.8}{0.3481 \times 10^{-3}} \right]^{5/8} \times$$

$$\left[ \frac{0.3481 \times 10^{-3} \times 4196}{0.6747} \right]^{1/3} (14346.65)^2$$

$$= \underline{28906.28} \text{ W/m}^2$$

$$\text{Deviation} = \frac{16539.44 - 28906.28}{16539.44} \times 100$$

$$= \underline{-74.8 \%}$$

## A P P E N D I X E

### ANALYSIS OF ERRORS

Errors in measured heat transfer coefficient may be caused by inaccuracies in the component measurements required for the calculation of heat transfer coefficient. In order to acquire an appreciation for the accuracy of the experimental data, error analysis was performed for several experimental runs. In this Appendix a sample calculation is presented using the data of Run 16.

As mentioned above that the parameter of interest to this propagation of error calculation is the uncertainty of the experimental heat transfer coefficient. The experimental uncertainty used here, is the absolute value of maximum expected deviation from the reported experimental result.

The experimental uncertainty for the average heat transfer coefficient can be defined as:

$$E_{\bar{h}} = \left[ \sum_{i=1}^n \left( \frac{\partial \bar{h}}{\partial y_i} \cdot E_{y_i} \right)^2 \right]^{1/2} \quad (E.1)$$

where  $y_i$  is any of  $n$  parameters of which the heat transfer coefficient is a function. Since  $\bar{h}$  has been calculated from

$$\bar{h} = \frac{Q}{A(\bar{T}_{wc} - \bar{T}_f)} \quad (E.2)$$

where ,

$Q$  Power input, W

$\bar{T}_{wc}$  Average corrected wall temperature , °C

$\bar{T}_\ell$  Average liquid temperature , °C

$A$  Heat transfer area,  $m^2$

Equation (E.1) can be expressed as

$$E_{\bar{h}} = \left[ \left( \frac{\partial \bar{h}}{\partial Q} E_Q \right)^2 + \left( \frac{\partial \bar{h}}{\partial A} E_A \right)^2 + \left( \frac{\partial \bar{h}}{\partial \bar{T}_{wc}} E_{\bar{T}_{wc}} \right)^2 + \left( \frac{\partial \bar{h}}{\partial \bar{T}_\ell} E_{\bar{T}_\ell} \right)^2 \right]^{1/2} \quad (E.3)$$

The partial derivatives existing in Eq.(E.3) can be evaluated by using Eq.(E.2). Thus the uncertainty in  $\bar{h}$  is

$$E_{\bar{h}} = \left[ \left( \frac{E_Q}{A(\bar{T}_{wc} - \bar{T}_\ell)} \right)^2 + \left( -\frac{Q E_A}{A^2(\bar{T}_{wc} - \bar{T}_\ell)} \right)^2 + \left( -\frac{Q E_{\bar{T}_{wc}}}{A(\bar{T}_{wc} - \bar{T}_\ell)^2} \right)^2 + \left( \frac{Q E_{\bar{T}_\ell}}{A(\bar{T}_{wc} - \bar{T}_\ell)^2} \right)^2 \right]^{1/2} \quad (E.4)$$

Thus to evaluate Eq.(E.4) , uncertainties for the power input, for the heat transfer area, for the average corrected surface temperature and liquid temperature are required to evaluate.

EVALUATION OF UNCERTAINTY IN POWER INPUT,  $E_Q$

Since,

$$Q = VI$$

Then,

$$E_Q = \left[ (VE_I)^2 + (IE_V)^2 \right]^{1/2} \quad (E.5)$$

Where

$E_I$  is uncertainty associated with ammeter reading

$E_V$  is uncertainty associated with voltmeter reading.

For Run 16,

$$I = 13 \text{ amps} \quad E_I = 0.05 \text{ amps.}$$

$$V = 50 \text{ volts} \quad E_V = 1.0 \text{ volt}$$

$$Q = VI = 50 \times 13 = 650 \text{ W}$$

and  $E_Q$  from Eq. (E.5);

$$E_Q = \left[ (50 \times 0.05)^2 + (13 \times 1)^2 \right]^{1/2}$$

$$= 13.238 \text{ W}$$

EVALUATION OF UNCERTAINTY IN HEAT TRANSFER AREA,  $E_A$

Since  $A = \pi d_o \ell$

Then  $E_A = \left[ (\pi \ell E_{d_o})^2 + (\pi d_o E_\ell)^2 \right]^{1/2}$

where,

$E_{d_o}$  is uncertainty associated with diameter measurement.

$E_\ell$  is uncertainty associated with length measurement

$$\ell = 0.179 \text{ m} \quad E_\ell = 0.0005 \text{ m}$$

$$d_o = 0.07 \text{ m} \quad E_{d_o} = 0.0001 \text{ m}$$

Therefore,

$$A = \pi \times 0.07 \times 0.179 = 3.93 \times 10^{-2} \text{ m}^2$$

$$E_A = \left[ (\pi \times 0.179 \times 0.0001)^2 + (\pi \times 0.07 \times 0.0005)^2 \right]^{1/2}$$

$$= 1.235 \times 10^{-4} \text{ m}^2$$

#### EVALUATION OF UNCERTAINTY IN TEMPERATURES $E_{\bar{T}_{wc}}$ & $E_{\bar{T}_{\ell}}$

Since the average surface temperature and liquid temperature was obtained by averaging the individual temperatures

$$\bar{T}_{wc} = \frac{\sum_{i=1}^n T_{wci}}{n} \quad (\text{E.6})$$

Therefore,

$$E_{\bar{T}_{wc}} = \left[ \sum_{i=1}^n \left( \frac{\partial \bar{T}_{wc}}{\partial T_{wci}} E_{T_{wci}} \right)^2 + \left( \frac{\partial \bar{T}_{wc}}{\partial n} E_n \right)^2 \right]^{1/2} \quad (\text{E.7})$$

where  $n = 3$  ;  $\frac{\partial \bar{T}_{wc}}{\partial n} = 0$

and  $\frac{\partial \bar{T}_{wc}}{\partial T_{wci}} = \frac{1}{n}$

Thus Eq. (E.7) gives

$$E_{\bar{T}_{wc}} = \left[ n \left( \frac{E_{T_{wc}}}{n} \right)^2 \right]^{1/2} \quad (\text{E.8})$$

Similarly,

$$E_{\bar{T}_{\ell}} = \left[ n \left( \frac{E_{T_{\ell}}}{n} \right)^2 \right]^{1/2} \quad (\text{E.9})$$

The following equation has been used to determine the corrected surface temperature  $T_{wc}$

$$T_i - T_{wc} = \frac{q d_o}{2k} \ln \frac{d_o}{dh} \quad (E,10)$$

where,

$T_i$  is inside surface temperature where thermocouple bead was located

$k$  is the thermal conductivity of metal

$$\text{or } T_{wc} = \left( T_i - \frac{q d_o}{2k} \ln \frac{d_o}{dh} \right)$$

Therefore,

$$E_{T_{wc}} = \left[ \left( E_{T_i} \right)^2 + \left( - E_q \frac{d_o}{2k} \ln \frac{d_o}{dh} \right)^2 + \left( - \frac{q}{2k} \ln \frac{d_o}{dh} \right)^2 + \left( \frac{q}{2k} \right)^2 E_{d_o}^2 + \left( + \frac{q d_o}{2k^2} \ln \frac{d_o}{dh} E_k \right)^2 + \left( \frac{q d_o}{2k} \frac{1}{dh} E_{dh} \right)^2 \right]^{1/2} \quad (E,11)$$

Where  $E_{T_i}$  is uncertainty associated with inside temperature measurement.

Now

$$E_{T_i} = 0,001 \text{ } ^\circ\text{C}$$

$$E_k = 0,0$$

$$k = 25,76 \text{ W/m K}$$

$$q = \frac{Q}{\pi d_{of}} = \pi \frac{650}{0,0393} = 16539,44 \text{ W/m}^2$$



And

$$E_q = \left[ \left( \frac{E Q}{\pi d_o \ell} \right)^2 + \left( - \frac{Q}{\pi \ell} \frac{1}{d_o^2} E_{do} \right)^2 + \left( - \frac{Q}{\pi d_o} \frac{1}{\ell^2} E_\ell \right)^2 \right]^{1/2} \quad (E,12)$$

Putting the values of  $E_Q$ ,  $E_{do}$ ,  $E_\ell$  and other quantities, we

$$\text{get} \\ E_q = \left[ \left( \frac{13,238}{0,0393} \right)^2 + \left( - \frac{650 \times 0,0001}{0,0393 \times 0,07} \right)^2 + \left( - \frac{650 \times 0,0005}{0,0393 \times 0,179} \right)^2 \right]^{1/2}$$

$$= 343,44 \text{ W/m}^2 \\ \text{Now } d_h = \frac{d_i + d_o}{2} \\ = \frac{0,062 + 0,070}{2} = 0,066 \text{ m}$$

Therefore,

$$E_{dh} = \left[ \left( \frac{1}{2} E_{di} \right)^2 + \left( \frac{1}{2} E_{do} \right)^2 \right]^{1/2}$$

$$\text{And } E_{di} = E_{do}$$

$$\text{Therefore } E_{dh} = \left[ 2 \left( \frac{1}{2} E_{do} \right)^2 \right]^{1/2} \\ = \left[ 2 \left( \frac{1}{2} \times 0,0001 \right)^2 \right]^{1/2} \\ = 7,071 \times 10^{-5} \text{ m}$$

Now putting the values of all the quantities in Eq (E,11) to determine  $E_{T_{wc}}$  :

$$E_{T_{wc}} = \left[ (0,001)^2 + \left( - \frac{343,44 \times 0,07}{2 \times 25,76} \ln \frac{0,070}{0,066} \right)^2 + \left\{ \left( - \frac{16539,44}{2 \times 25,76} \ln \frac{0,070}{0,066} - \frac{16539,44}{2 \times 25,76} \right) 0,0001 \right\}^2 + \left( \frac{16539,44 \times 0,070}{2 \times 25,76 \times 0,066} \times 7,071 \times 10^{-5} \right)^2 \right]^{1/2}$$

$$E_{T_{wc}} = 4.9877 \times 10^{-2}$$

After knowing  $E_{T_{wc}}$ ,  $E_{\bar{T}_{wc}}$  can be calculated by using Eq (E.8).

$$E_{\bar{T}_{wc}} = \left[ 3 \left( \frac{4.9877 \times 10^{-2}}{3} \right)^2 \right]^{1/2}$$

$$= 2.8808 \times 10^{-2} ; \bar{T}_{wc} = 86.66 \text{ } ^\circ\text{C}$$

And  $E_{\bar{T}_{\ell}}$  is calculated from Eq (E.9)

$$\text{Using } E_{T_{\ell}} = E_{T_i} = 0.001 \text{ } ^\circ\text{C}$$

Therefore

$$E_{\bar{T}_{\ell}} = \left[ 3 \left( \frac{0.001}{3} \right)^2 \right]^{1/2}$$

$$= 5.7735 \times 10^{-4}$$

$$\text{And } \bar{T}_{\ell} = 80.416 \text{ } ^\circ\text{C}$$

Having calculated  $E_{\bar{T}_{wc}}$  and  $E_{\bar{T}_{\ell}}$ , uncertainty in heat transfer coefficient  $E_{\bar{h}}$  can be calculated by Eq.(E.4).

Putting the pertinent values of the various quantities in Eq.(E.4), we have

$$\begin{aligned}
 E_{\bar{h}} = & \left[ \left( \frac{13.238}{0.0393(86.66-80.416)} \right)^2 + \left( - \frac{650 \times 1.235 \times 10^{-4}}{(0.0393)^2 (86.66-80.416)} \right)^2 \right. \\
 & + \left. \left( \frac{-650 \times 2.88 \times 10^{-2}}{0.0393(86.66-80.416)^2} \right)^2 \right. \\
 & + \left. \left( \frac{650 \times 5.773 \times 10^{-4}}{0.0393 \times (86.66 - 80.416)^2} \right)^2 \right]^{1/2}
 \end{aligned}$$

$$\text{or } E_{\bar{h}} = 55.936$$

$$\text{So } \bar{h} = 2649.27 \pm 55.936$$

This uncertainty represents a typical value of the other experimental runs. Therefore, it could be said with some justification that the expected experimental uncertainties of the heat transfer coefficient for the experimental program reported here were about  $\pm 10$  per cent which is an acceptable level of error keeping in view the complexities in the boiling heat transfer process.

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