STUDIES OF THE SANDS OF A PART OF THE THAR DESERT IN DISTRICT JAISALMER, RAJASTHAN

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THESIS SUBMITTED By P. C. MOHAN

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FOR THE DEGREE OF DOCTOR OF PHILOSOPHY in APPLIED GEOLOGY



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FRONTISPIECE_A view of barchan dune field at Dhanana, district Jaisalmer, Rajasthan.





Certificate

The thesis entitled 'STUDIES OF THE SANDS OF A PART OF THE THAR DESERT IN DISTRICT JAISALMER, RAJASTHAN' presented by Sri P. C. Mohan, for the award of the Degree of Doctor of Philosophy in Applied Geology, embodies results of investigations carried out by him from January, 1973 to August, 1977 under our supervision and guidance. This is further to certify that this work has not been submitted for the award of any other degree.

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P.c.M. ha

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STUDIES OF THE SANDS OF A PART OF THE THAR DESERT IN DISTRICT JAISALMER RAJASTHAN

ABSTRACT

The Thar desert in India occupies about 155,000 sq.km of western Rajasthan. During recent times it has attracted investigators with varied types of problems including those of defence, traction and geomorphology. However, geological and geotechnical aspects have received scant attention. The present study is an attempt to fill this gap.

In this investigation an exhaustive and systematic sedimentological study of desert areas around Sam, Dhanana, Lunar and Murar in Jaisalmer district has been made. Various bedforms, namely, ripples, barchans, transverse dunes, longitudinal dunes and sand piles have been described and their probable origin is discussed.

Samples collected from the various bedforms and sand flats have been analysed for (i) textural attributes of sand grains, (ii) minerological composition and (iii) engineering properties of the desert sands.

Grain size distribution, roundness and sphericity of the desert sands have been investigated in detail. For statistical analysis of grain size data, graphical moments for central tendency, dispersion, symmetry and peakedness of the distributions have been calculated with the help of a digital computer, using various formulae given by different workers. The intermediate percentile values used in these formulae were calculated by interpolating between the experimental points using normal distribution. Plots of the statistical parameters have been made and their correlations discussed and interpreted in terms of grain size populations and modes of transport. In addition, spatial variability of grain size parameters in the area, and also within the barchans, has been studied.

Fields of the various environments have been delineated on plots between different grain size parameters by different investigators. Grain size parameters from the area under investigation have been plotted on some of these diagrams such as C-M diagrams, skewness-mean size diagram, mean size standard deviation diagram, Md vs. QDa diagram, QDa vs. Ska diagram etc., with a view to evaluate their efficacy as accurate environment indicators.

Heavy and light minerals of the desert sands have been identified and detailed petrographic modal analyses made. Variations of constituent modes with grain size and in space have been studied with a view to determine the provenance of the sands.

Determination of the various engineering properties of the sands is an essential step for any engineering project in deserts. Representative samples from different localities of the area have been subjected to shear strength and compaction tests. Also maximum dry density and optimum moisture content were determined. Further, to investigate the mortar properties of the desert sands, samples were mixed with coment and water for castin cubes in ratios prescribed by the Indian Standards Code. These sand cement cubes were then autoclaved and tested for compressive strength by Universal Testing Machine. The data so obtained were then analysed and correlated with the grain size parameters. Permeability of a few typical samples has been determined. The soil groups of desert sands of the area have also been determined.

In brief, emphasis throughout the study is on a closer understanding of the energy-environment relationship which manifests in grain size parameters, bedforms, grain attributes and petrography of the area.

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CHAPTER-1

INTRODUCTION

1.1 RATIONALE

The Thar desert of India has remained neglected perhaps due to difficult terrain and hostile climatic conditions. Consequently, scant information is available regarding the nature and behaviour of sands. Lately, the problems posed by this vast destitute of sand have come to prominence due to its strategic location near the international border, particularly from defence and traction view points.

The area is almost virgin and there is a great potential for its future development. Keeping these points into consideration coupled with the author's interest in the vast expanse of sands typifying aeolian environment, where winds have free play in shaping and modifying the desert surface, the present type area was selected for detailed investigations presented in this dissertation.

It is hoped that the studies of bedforms and their orientation and textural, petrographic and geotechnical investigations of the aeolian sands should provide an insight into the processes responsible for the initiation, growth and maintenance of the deserts, aeolian transport and deposition, and the possibility of desert contraction or expansion, if any. The study of engineering properties of the sands will be of use for future engineering works that may be carried out in this area.

It is also hoped that this work may attract the attention of more workers to probe the mysteries of the deserts for the betterment of mankind.

1.2 AREA OF STUDY

The area under investigation covers a part of the Thar desert falling between latitudes $26^{\circ}30^{\circ}$ to $26^{\circ}52^{\circ}$ and longitudes $70^{\circ}0^{\circ}$ to $70^{\circ}33^{\circ}$. The village Sam lies in the northcast of the area which extends to the southwest right upto international Indo-Pakistan border including remote border outposts like Murar, Dhanana and Lunar (Fig. 1.1). In all, it occupies about 3,000 square kilometers of the arid expanse in the district of Jaisalmer (Lat. $26^{\circ}55^{\circ}N$, Long. $70^{\circ}56^{\circ}E$), Rajasthan. It falls under the Survey of India sheet numbers 40 J/1, 40 J/2, 40 J/5, 40 J/6, 40 J/S and 40 J/10. The largest city in the vicinity of the area is Jaisalmer which supports a population of about 30,000 and is well connected with Jodhpur (Lat. $26^{\circ}18^{\circ}N$, Long. $73^{\circ}01^{\circ}E$).

The area is conveniently approachable from Jaisalmer which is connected by a metalled road to Sam and Dhanana. However, rest of the interior is accessible with the help of a camel or a power vehicle.

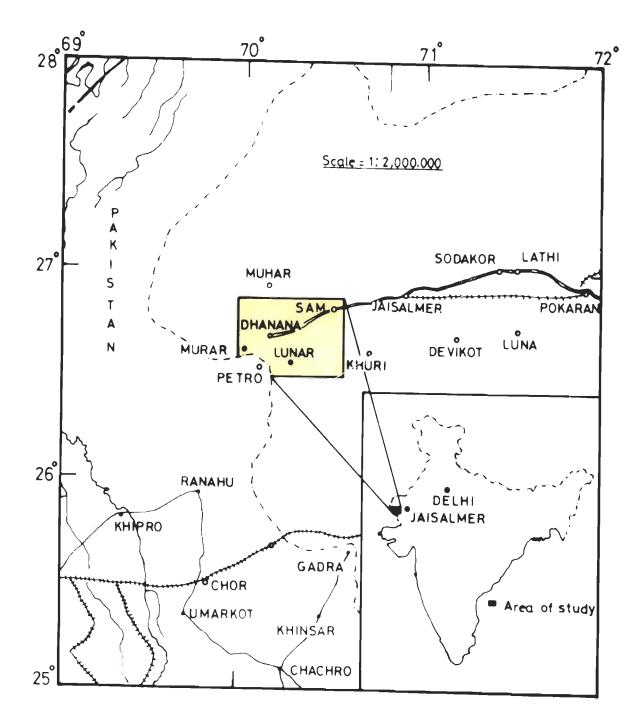


Fig. 1.1__ Location map of the area.

1.3 CLIMATE

The general characteristics of the Thar desert are typical of a hot desert such as slight rainfall, large variability of rainfall, large diurnal variation of temperatures and high maximum temperatures during summers, large evaporation, nonorigin of any permanent river, scanty vegetation, practically no agriculture, dependence of man on animals and a sparse and nomadic population (Pramanik, 1952).

4

1.3.1 Rainfall

The annual rainfall in the Thar desert is less than 25 cm. The average rainfall of western Rajasthan is 24.83 cm with the highest rainfall from 77.5 cm to the lowest rainfall 4.7 cm with a coefficient of variability 49 (Pramanik, 1952). Though the average rainfall is low, intense and sporadic falls may occur pouring large quantities of water in a considerably short duration of time. Torrential rains have been reported from deserts when the rainfall equals to one and a half times or even more of the annual rainfall in a single day (Pramanik, 1952). According to Pramanik (1952) Jaisalmer has more daily intensity of rainfall in monsoon as compared to places like Calcutta and Bombay which are situated in rainy regions.

1.3.2 Temperature

The temperatures in the Thar desert are of extreme

nature. Winters are quite cold with temperatures going 2° C to 5° C below zero. Similarly summers are characterised by intense heat with strong hot winds. Due to rocks and sandy nature of the soils lacking sufficient vegetation cover and dry atmosphere with clear skies, the variation of high day temperature to low night temperature is considerable and with a sharp change. The mean maximum temperature in May is 38° C to 46° C over most part of Rajasthan with a mean minimum at 24° C to 27° C (Pramanik,1952).

1.3.3 Humidity

In winters the relative humidity is generally 50% to 60% in the morning hours and 25% to 35% in the afternoon hours. During summers humidity is in general 35% to 60% in the morning hours and 10% to 30% in the afternoon hours except for the month of June which has higher mean value due to the advent of rainy season near its end (Pramanik, 1952).

1.4 VEGETATION

In general the area lacks vegetation and there is near absence of trees. However, there are sparse and scanty patches of shrubs, thorny bushes and wild grasses. It is a vast barren land showing a typical desert destitute with thin population. There are some tiny settlements scattered in the desert and the major occupation of the inhabitants is cattle rearing (mainly cows). Some of the

villages have grown around tiny wells dug in clusters of 8 to 10 in number which are commonly called 'Beris'. Water table occurs at twenty to thirty metres depth and these wells usually get dried up in summers. The inhabitants move to other areas with their herds during summers and in times of drought, which are fairly common.

1.5 PHYSIOGRAPHY

Regionally, the area consists of low relief with scarps of yellow limestones around the city of Jaisalmer. Most of the area is of undulating topography consisting of barron rock wastes with occasional mounds of sands forming different types of dunes. The area around the city of Jaisalmer is dissected by numerous 'nallas' and gullies giving rise to ophomeral rivulets like the Mussurdi which flows in northwestern direction. Similarly, the Kakni river and its tributarics flow towards north. As one moves towards Murar (Fig.1.3), sand accumulations increase steadily with a general tendency of the sand cover to thicken in the southwest until Dhanana where barchans and seifs practically cover the entire area and the true sandy desert starts. The interdune areas are comparatively firm and flat which occasionally get a darker colour tone due to surface accumulation of small ferruginous concretions.

In general, it may be concluded that the various physiographic features have largely been controlled by

climate typical of a wind governed terrain.

1.6 DRAINAGE

Drainagewise the area can be divided into two major units controlled by the lithology i.e. (i) consisting of compact rock wastes and (ii) wind blown sediments forming dunes. The area, for obvious reasons, is not drained by any perennial river. The drainage is mostly internal. On the barren rocky desert, as around Jaisalmer, the drainage pattern is dendritic. A number of small nallas' and rivulets start from rocky slopes and culminate into a local depression forming small ponds which may remain dry through most of the year. The chief water tanks around Jaisalmer are Gadi Sar, Govind Sar, Gulab Sagar, Sudha Sar, Kheta Sar, Gajroop Sagar, Mobta Sar, Amar Sagar etc.

On the hill slopes deep ravines have been cut by mallas' which flow in the rainy season. At places these mallas' have cut deep channels in the wind deposited sands. Elsewhere, there may be formation of alluvial cones adjoining comparatively high scarps where the mallas' have reworked the wind blown sediments.

In the sandy desert there is no well established drainage pattern and no 'nallas' or gulley cuttings are observed due to quick and easy mobility of sands by strong summer wind currents.

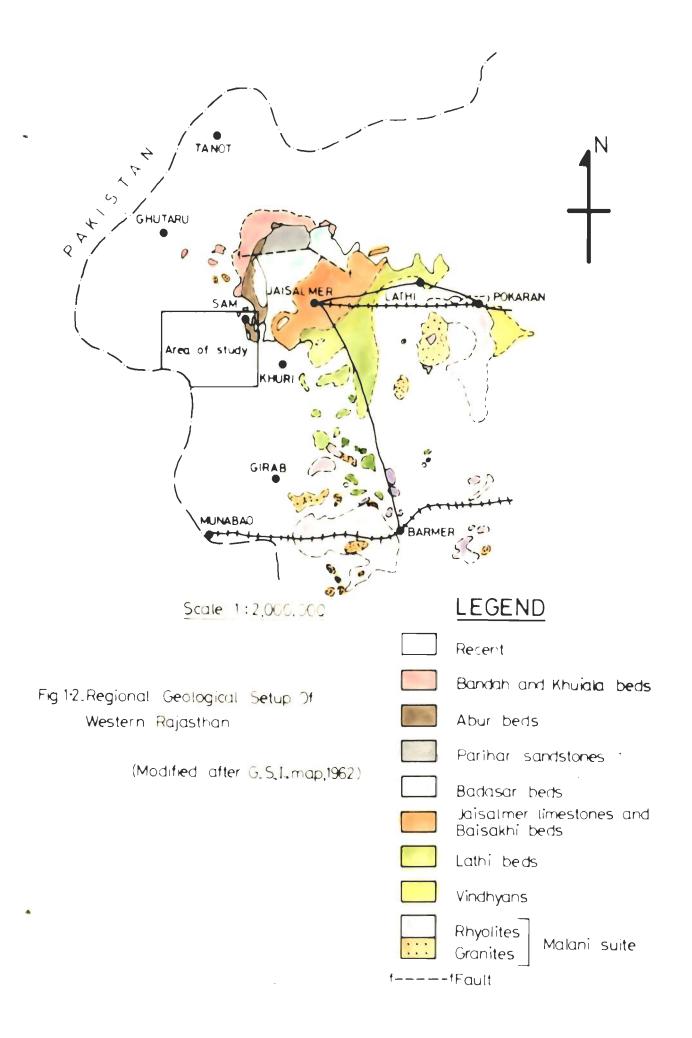
1.7 GEOLOGY OF THE AREA

The regional geological setup is shown in Figure 1.2. The oldest rocks exposed in the Jaisalmer district are Malani suite of igneous rocks which consist of granites and rhyolites. These are overlain unconformably by the Vindhyans composed of dolomites with cherty layers.

The fossiliferous Badhaura Formation, consisting of yellow calcareous sandstones and brown clays, occur as isolated patches overlying unconformably on the Vindhyans. These are thought to be of Permo-Carboniferous age. Though no exposures of Triassic sediments are known, Permo-Triassic sequence has been recorded in the subsurface (Das Gupta, 1975b).

The Jurassic sequence is represented by the Lathi Beds (L. Jurassic), Jaisalmer Beds (Callovian to Oxfordian), Baisakhi Beds (Oxfordian to Kimmeridgian) and Badesar Beds (Upper Jurassic). The Lathi Beds, which are 330 m thick, consist chiefly of sandstones with some layers of limestone in the upper parts. The Jaisalmer Beds are 160 m thick. These are formed of buff to yellow oolitic and shell limestones and calcareous sandstones. The Baisakhi Beds are 600 m thick and consist of gypseous shales and sandstones. A 110 to 300 meter thick horizon, consisting of ferruginous sandstones and grits, constitutes the Badesar Beds.

The Parihar Sandstones which are 600 to 850 m thick are thought to be of Lower Cretaceous age. These consist of ferruginous and feldspathic sandstones and quartzites.



A comparatively thin formation of about 60 to 90 m consisting of brown to yellow shell limestone with subordinate bands of grit, clays and shales constitutes the Abur Beds. These belong to the Aptian age. The Bandah and Khuiala Beds of Eocene age, about 50 m thick, rest unconformably over the Abur Beds. They consist of siliceous limestones with Fuller's earth and clay.

The Shumar Beds, about 30 to 316 m thick, rest unconformably over the Bandah and Khuiala Beds. These consist of ferricrusted, bouldery, arenaceous limestones, sandstones and limestones. These are the youngest formation belonging to the Sub-Recent age. It has not been possible to include Shumar Beds in the geological map (Fig.1.2) since the published geological maps are of small scale and indistinct. hest of the area is mainly covered by unconsolidated, sandy soils constituting the aeolian sodiments. These are thought to be of Recent age. Table 1.1 gives general stratigraphic succession in the Jaisalmer district as determined by various workers of Geological Survey of India and Oil and Natural Gas Commission (Narayanan, 1964; Lukose, 1972; Das Gupta, 1973; Lukose, 1974; Lukose and Misra, 1974; Das Gupta et al. 1974; Das Gupta, 1975a, b; Pareck, 1975; Verma, 1975).

The Mesozoic and Tertiary rocks form a gentle arch which plunges towards Mari in Sindh, Pakistan, in the northwest direction. The whole sedimentary sequence thickens in the west and northwest and attains a thickness

| Table | 1.1- | General stratigraphic succession of |
|-------|------|-------------------------------------|
| | | Western Rajasthan. Modified after |
| | | Krishnan (1968, p.361). |

| Formation | Thickness | Lithology | Age |
|-----------------------------|--|--|--|
| Unconsolidated Sediments | | Aeolian Sediments | Recent |
| Shumar Beds | 30-316 m | Ferricrusted, bouldery arenaceous limestones, sandstones and limestones | ?Sub-Recent |
| | Фармальный Ф.К. 19 19 19 19 19 1 9. | Unconformity | |
| Bandah and Khuiala Beds | ?50 m | Siliceous limestones with fuller's earth and clay | Eocene |
| | | -Unconformity | |
| Abur Beds | 60-90 m | Limestone, subordinate grits, clays and shales | Low.Creta- ceous(Aptian) |
| Parihar Sand- stones | ?600-850 m | Ferruginous and feldspa- thic sandstones and quartzites overlapped at places by Eocene beds | Low.Creta- ceous(Neoco- mian) |
| Badesar Beds | 110-300 m | Ferruginous sandstones and grits | Up. Jurassic |
| Baisakhi Beds | 600 m | Sandstones and Shales (gypseous) | Up. Jurassic (Oxfordian to Kimmeridgian) |
| Jaisalmer Beds | 160 m | Buff to yellow oolitic and shell limestones and calcareous sandstones | Up Jurassic (Callovian to Oxfordian) |
| Lathi Bods | 330 m | Sandstones and some layers of limestones in the upper part | Low.Jurassic |
| Badhaura Fornation | | Unconformity Yellow, calcareous sand- stones, brown clays Unconformity | Permo-Carbo- niferous |
| <i>J</i> indhyans | | Grey dolomite with chert layers and nodules | Pre-Cambrian |
| Malani Formation | n | - Unconformity Rhyolites and granites | Pre-Cambrian |

of about 6,000 m. A large fault on the western side of the arch is indicated by geophysical surveys (Krishnan, 1968, p. 362).

1.8 PREVIOUS WORK

The area under investigation has remained practically neglected from the geological view point perhaps due to its remote location, lack of transport facilities and climatic hazards, though some work has been initiated by the Central Arid Zone Research Institute (CAZRI), Jodhpur in some other parts of the Thar desert.

Frere (1870) and Blanford (1876) are the early workers who reported that most of the Thar desert is occupied by parallel longitudinal dunes. Blanford (1876) was the first to establish the parallelism of the present wind direction and longitudinal dunes.

The Planning Commission of India reported in the First Five Year Plan (Anon., 1952) that the Thar desert had been advancing outwards in a great convex arc at an alarming rate of 0.8 km per year. This resulted in a symposium on the Rajputana desert i.e. the Indian part of the Thar desert, in March, 1952 organised by the National Institute of Sciences (now Indian National Science Academy) in an effort to discuss suitable steps to arrest its unchecked outward march. A symposium on the problems of the Thar desert and a workshop on the desert geology had been organised by the UNESCO and Geological Survey of India in 1964 and 1975 respectively.

More recently Gupta and Prakash (1975) have compiled environmental aspects of the Thar desert in the form of a book. All these works are referred to appropriately in the text.

Most of the workers like Banerji (1952), Pramanik (1952), Kendrew (1961) and Krishnan (1968) have suggested climatic (conditions for the origin of the Thar desert. Roy and Pandey (1970) and Ahmad (1975) advocate an important role of tectonism in its genesis. Bryson and Baerreis (1967) think that atmospheric dust caused by human activity may trigger an extreme dry cycle. Wadia (1955,1960) thought that the general desiccation following the Pleistocene glaciation as the major cause of the desert.

Studies on geomorphology and land-use planning in the marginal areas of the desert have been mainly undertaken by the CAZRI and the Geological Survey of India.Various dune forms and landforms of the Luni Basin have been described by Pande et al.(1964), Ghose et al.(1966), Singh(1969-70), Verstappen et al.(1969), Singh et al.(1971) and Ghosh (1975). Dunes and geomorphological land units of the Bikaner district are described by Singh et al.(1975). Bhattacharya (1956) has discussed the nature and origin of dunes on the western side of Mount Abu. Land forms of the northern part of Jaisalner have been described by Babu and Rao (1974). Morphometric analyses of drainage basins of the desert have been made by Singh et al.(1969-71), Pandey et al.(1972), Singh and Ghose (1973) and Ramadurai and Gupta (1975).

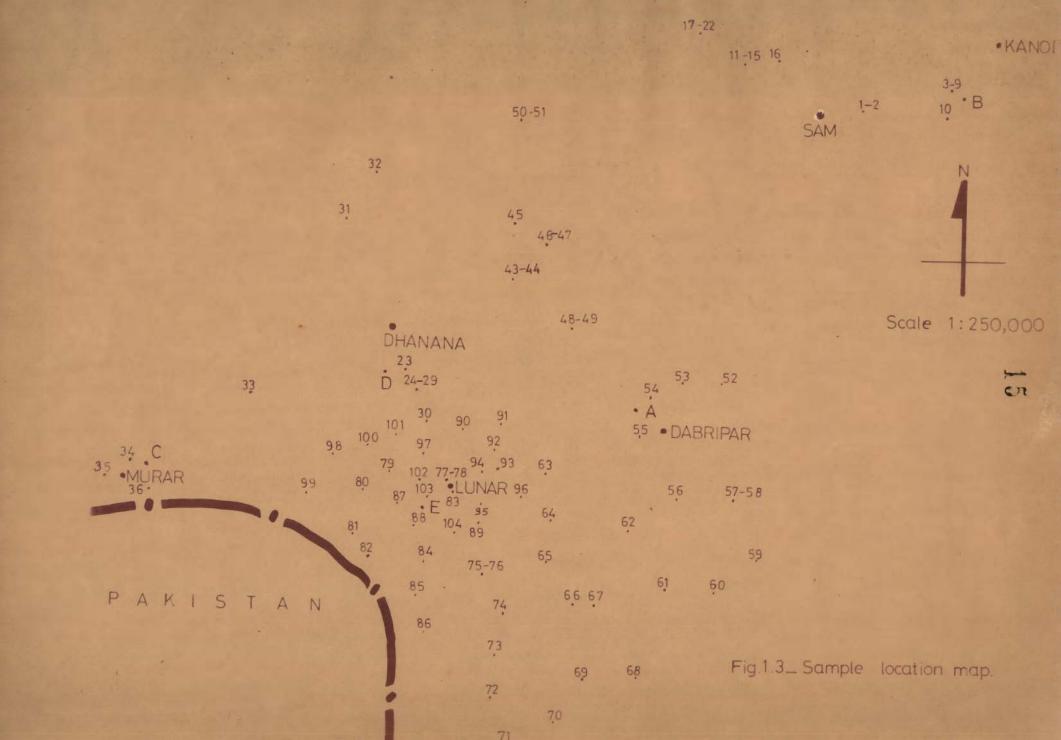
Holland and Christie (1909) think that salt contents of the salt lakes of the Thar desert have been brought from the Rann of Kutch by Vind. Godbole (1952) postulates that salt basins are relics of the extended area of the Arabian sea. Panday and Chatterji (1970) find that location of some of the Ranns (saline depressions) is controlled by faults. Ghose (1964,1965) thinks that these Ranns are due to internal drainage and salts are obtained by chemical weathering of adjoining rocks.

Gupta (1958) and Rao (1962) have described mineralogy of the desert sands. Ghosh (1952) and Chakarabarti(1968) have studied grain size distributions. Roy and Pandey (1970) have reviewed the problem of expansion of the Thar desert.

1.9 SCOPE OF THE PRESENT WORK

In the present study, an exhaustive and systematic sedimentological analysis and geotechnical investigations of the desert sands in areas around Sam, Dhanana, Lunar and Murar in Jaisalmer district have been made. Various bedforms like seifs, barchans, transverse dunes, ripples and sand piles have been recognised and all the geometric dimensions necessary for defining their shape and any special features noted.

More than one hundred samples have been collected. Locations of the samples are shown in Figure 1.3 and



descriptions regarding their position on the bedforms are given in Appendix I. Locations of a few samples collected from areas near Ramgarh $(27^{\circ}23': 70^{\circ}30')$ and Ludharwa $(70^{\circ}48'30'': 26^{\circ}25'0'')$ which do not fall in Figure 1.3 are also given in Appendix I. The samples have been analysed for the following aspects:

- (i) Textural attributes of sand grains, that is, grain size, roundness and sphericity,
- (ii) Mineralogical composition, and

(iii) Engineering properties and behaviour.

All the findings regarding the above aspects have been systematically presented in this work which consists of seven chapters. Chapter 1 entitled 'INTRODUCTION' describes the location, accessibility, climate, vegetation, geomorphology. drainage, geology of the area under investigation and a brief review of the relevant previous work on the Thar desert.

Chapter 2 with the title 'REVIEW OF ORIGIN AND CHARAC-TERISTICS OF DESERT ENVIRONMENTS WITH SPECIAL REFERENCE TO THE THAR DESERT' describes various views about the formation of deserts of the World and the Thar desert in particular. The controversial problems of age of the Thar desert and its expansion and contraction are critically reviewed.

Chapter 3 titled as 'BEDFORMS' includes areal distribution o bedforms, their geometry and orientation with respect to the prevailing wind direction and grain size variation within the different

bedforms.

V

Chapter 4 entitled 'TEXTURAL STUDIES' exhaustively deals with grain size analysis and grain attributes such as grain roundness and sphericity. Desert sand samples were analysed for grain size distribution studies using ASTM sieves. For statistical analysis, the graphical moments were determined for central tendency, dispersion, symmetry and peakedness of the distributions. Moment measures using the various formulae are calculated with the help of a computer and compared. The required percentile values used in the calculation of moment measures are determined by interpolating between the adjacent experimental points using normal distribution. Modality of sand samples of the area has been studied from the cumulative curves plotted on arithmatic-probability paper. Plots of grain size statistical parameters have been made and their correlations discussed and interpreted in terms of grain size populations and processes of transportation by wind. Regional variability of the various statistical parameters in the desert area is probably being reported for the first time in the present work. Spatial variability of the various grain size parameters within barchans is critically analysed.

Diagrams of plots between different grain size parameters have been given by different researchers and fields for various environments have been delineated on these plots. Grain size statistical parameters obtained

from the desert sands of the arca under investigation have been plotted on C-M diagram, QDa-Md diagram, QDa-SKa diagram etc., with a view to develop grain size analysis as an accurate environmental indicator.

For grain roundness studies, slides of representative samples are made and roundness of quartz grains in each slide is determined by visual comparison method. Accuracy and consistency of the visual comparison method are also evaluated. Variation of roundness in the area and with grain size in individual samples has been analysed in the study. Also sphericity of the aeolian sands has been studied by measuring axial ratio of quartz grains from half phi fractions of a few sand samples.

Chapter 5, which bears the title 'PETROGRAPHIC STUDIES' deals with separation and detection of both light and heavy minerals in the representative sand samples of the area. Light and heavy mineral slides are made and petrographical and modal analysis is carried out. Mineralogical data so collected is then analysed to study their variability in space and with grain size and also to establish provenance of the sands.

Chapter 6 entitled 'ENGINEERING PROPERTIES' constitutes a very important applied aspect of the present investigation. Determination of the various engineering properties of sands is an inevitable step preceding any construction project in deserts. Representative sand samples from different

localities of the area have been subjected to shear strength and compaction tests in order to evaluate their suitability for foundations. To investigate mortar making properties of the desert sands, representative sand samples of the area were mixed with cement and water in the ratios prescribed by Indian Standards Code and cubes casted. These sandcement cubes were autoclaved and then tested for compressive strength by Universal Testing Machine. Compressive strength data so obtained were then analyzed and correlated with grain size parameters. The hydrologic potential of desert sand samples was also evaluated by subjecting these to permeability tests.

The final Chapter 7 is titled as 'SUMMARY AND CONCLU-SIONS' which summarises the findings of Chapters 1 to 6. The salient results of the investigations are brought out and important conclusions are drawn. Finally suggestions for further studies in sedimentology of the Indian desert are outlined.

The present thesis thus embodies a systematic study of the desert sands in the western part of Rajasthan. The emphasis throughout the work is on a closer understanding of the energy-environment relationships which manifest variously in bedforms, grain size parameters, grain attributes and petrography and engineering properties of the sands of the area.

CHAPTER-2

REVIEW OF ORIGIN AND CHARACTERISTICS OF DESERT ENVIRONMENTS WITH SPECIAL REFERENCE TO THE THAR DESERT

2.1 THEORIES OF DESERT FORMATION

Deserts are the reflections of climatic conditions which are responsible for their creation, growth and sustenance. Thus all those factors which influence climatic conditions ultimately also affect the formation and location of the deserts. The atmospheric conditions have their origin from the planetary system of high and low pressure belts. There is circulation of winds between the hot equitorial regions and the cooler polar areas. The existence of high pressure belts 30° north and south of equator causes clear skies which are not favourable to rains.

The deserts of the world are the result of one or many conditions like geographic location, topographic barriers and their orientation with respect to the direction of moisture laden winds, the effect of oceanic currents, low relief of the area or natural winds with insufficient moisture. Roy and Pandey(1970) suggest three different situations and conditions such as (i) the presence of persistent anticyclonic conditions (North African desert), (ii) impinging of cold ocean currents on the coasts (Peru desert, Namib desert) and (iii) topographic barriers which shut out the moisture laden winds (Gobi desert). Most of the deserts of the world are located in regions where moist winds either originate or pass over land areas under clear skies causing little or no rains. Whenever they are obstructed by any land barrier such as a mountain range the rain occurs whereas desiccating conditions remain prevalent in the leezone. Australian desert and the Kalahari desert of South Africa are the examples.

2.2 THE THAR DESERT

A considerably large area (about 640 km long and 160 km wide) of the western and southwestern Rajasthan, India, and Sind, Pakistan form the Great Indian Desert which is called the Thar desert. The desert, in general, is covered by a several meter thick sand which at places thickens, thins or is absent to bare the rocky floor. The sands are moved by the predominantly southwest winds to form various types of dunes and other characteristic desert bedforms. The desert gradually grades into a semi-arid region on its northern and eastern borders.

The whole region starting from the western coast of north Africa to the Thar desert in the east appears to be almost meteorologically homogeneous (Sajnani, 1964) with nearly identical physiographic and anthrogeographical conditions (Roy and Pandey, 1970). Thus the Thar desert seems to be the eastern limit of a large desert tract which includes the North African Sahara and Arabian deserts also.

2.2.1 Origin of the Thar Desert

The chief causes which are thought to be responsible for the origin of the Thar desert are:

- (a) Geographical location in the desert belt of the world,
- (b) Topographical factors,
- (c) Meteorological factors,
- (d) Tectonism and
- (e) Other factors.

(a) Geographical location in the desert belt of the world — Most of the deserts of the world lie in a belt between 30° north and south of equator. Generally, these are low pressure areas characterised by clear skies which are not conducive to rainfalls. The Thar area of India also falls in this region. Therefore, the occurrence of desert here is not unexpected. In fact, it has been thought as an eastern limit of a great desert that includes even African Sahara (Sajnani, 1964).

(b) <u>Topographical factors</u> — The main factors which influence the climate of the Indian subcontinent as a whole and also constitute one of the major causes of origin of the Thar desert are the location of the high Himalayas, the Kirthars and the Sulaiman mountain ranges and the Tibetan plateau (Roy and Pandey, 1970). The cumulative effect of these natural barriers is such that the western part of Rajasthan gets very meagre rainfall. Similarly, whatever moisture is left from the moist winds passing over the Ganges plains gets precipitated on the eastern flanks of the Aravallis, whereas desiccating conditions prevail in the west beyond (Glennie, 1970, p.5).

(c) <u>Meteorological factors</u> — The chief climatic causes responsible for the origin of the Thar desert are the presence of low pressure over western part of India and central part of Pakistan, dry northwest upper air and shallow southwest monsoon currents (Roy and Pandey, 1970).

According to Banerji (1952) the mechanism of monsoon in India is influenced by a pressure gradient setup between a low pressure over the Thar desert and a relatively high pressure in the south Indian Ocean. The low pressure is attributed to higher temperatures resulting from the bare desert rocks and sands that get quickly heated and to the hydrodynamic consequence caused by the natural barrier to the airflow by the Himalayan, the Sulaiman and the Kirthar ranges in the form of a 'corner' (Roy and Pandey, 1970).

Moist air can cause precipitation only when it cools and condenses by ascending up. But according to Ramanathan (1972) and Pramanik (1952) there exists dry, warm, subsiding, anticyclonic air over the Thar desert and its neighbourhood which overlies the maritime shallow surface winds drawn in during the monsoons. Thus the ascending moist airs are absorbed by these anticyclonic winds thereby dissipating clouds, if any. Pramanik (1952) states that so long these

anticyclonic winds prevail over the Thar desert there is little possibility of increase in the rainfall in this region.

The monsoon from the Arabian Sea is strong only south of The Gulf of Cambay and almost fades out in the north. Hence a very feeble monsoon air passes over the Thar desert. Winds coming across the Arabian sea loose most of their moisture by travelling over North Africa and Abyssinian plateau. This makes it amply clear that due to either complete denial or very weak monsoons desertic environment thrives in the Thar region.

(d) <u>Tectonism</u> — The Thar region experienced faulting and regional domal upwarping in association with complementary rising of the Aravallis in the Holocene times. Faulting resulted in a horst in Rajasthan and a graben in Sind. As a consequence to this the arm of the sea occupying the Thar region was forced out. There resulted a massive course shifting of rivers like the Indus, the Sutlej and the Beas westward. This caused floods which destroyed Mohanjodaro and Harappa civilizations. Headward erosion of the Jamuna captured the river Drishadwati. The head-waters of the Saraswati were affected by the rising Himalayas which could not succeed in cutting through the Siwalik barrier (Ahmad, 1975).

Thus massive course shifting of the life sustaining rivers of the region coupled with total loss of rivers like

Drishadwati and Saraswati partly due to tectonism, rendered the area a desert. Of course, general worldwide warming up of the climate following the Pleistocene glaciation is also one of the contributory factors (Ahmad, 1975).

(e) <u>Other factors</u> — Massive deforestation, unplanned grazing of animals and unplanned cultivations are the other reasons which add to the aridity of the region. Bryson and Baerries (1967) think that the dust cover raised by excessive human activity is the cause for the spread of the desert.

2.2.2 Age of the Thar Desert

Wadia (1956, 1959) thinks that the Asian deserts are a product of the Post-Pleistocene glaciation aridity phenomenon, and these may be as young as 10,000 to 20,000 years in age.

Roy and Pandey (1970) argue that climatic condition like scanty or no rainfall due to very feeble monsoon over the Rajasthan desert region is the ultimate cause which is responsible for the formation of the desert. Also the present monsoon system was established in the Indian sub-continent during Mid. Miocene period when the Himalayan ranges came into existence. Different lithologies deposited from the Eocene to Pleistocene in this region are indicative of the period of desert formation. Thus the Thar desert came into existence during the Mid.Miocene, though its development was thwarted temporarily by humid climates(Ahmad, 1969). The prevalence of aridity during the Mid. Miocene in the southwestern desert of North America (Axelrod, 1950; Axelrod and Ting, 1960) is cited as a supporting evidence.

Recent geophysical studies of the Indian ocean (McKenzie and Sclater, 1971; Fisher et al., 1971; Sclater and Harrison, 1971; Laughton et al., 1972) have made it possible to trace the movement of the Indian Peninsula with time. Paleogeographic reconstruction based on these studies by Laughton et al. (1972, Fig. 4) suggest that the equator passed through areas around Madras during the Middle Miocene indicating thereby that the part of Indian Peninsula now occupied by the Thar desert was way down to the south and probably lay in a humid, moist region. Thus it seems that the Thar desert per se could not be older than the time when the Peninsula came to occupy more or less the present position.

The presence of the Pleistocene Bap Boulder Bed in Rajasthan and Sub-Recent Shumar Formation of alluvial origin with a subsurface thickness of more than 300 m in the heart of the desert suggest that humid conditions prevailed in the area till Sub-Recent times.

Historical evidence regarding the age of the desert Archud is rather unequivocal and has been reviewed by Gupta and Prakash (1975). However, Singh et al. (1974) have reported on the basis of pollen studies from the saline lake cores that more than 10,000 years B.P. intense arid conditions prevailed and that between 10,000 and 3,000 years B.P. climate was rather humid. Since 3000 years B.P. climate has become arid again.

Goudie et al. (1973) have suggested that in this region stabilized dunes are formed whenever rainfall per annum exceeds 25 cm and active ones if rainfall is less than 25 cm. It will be shown later that the area has stabilized as well as active dunes. It is suggested that the Thar desert probably came into existence more than 10,000 years back and old dunes were formed, which were stabilized during the humid period that followed. Fresh, active dunes have developed since the onset of the present aridity cycle starting some 3000 years back.

2.2.3 Expansion or Contraction of the Thar Desert

It has long been feared that the Thar desert is encroaching on the fertile lands in its im ediate neighbourhood. The Planning Commission reported in the First Five Year Plan (Anon.,1952) that the Thar desert is advancing in a great convex arch towards Delhi and Aligarh at the rate of about 0.8 km per year.

Roy and Pandey (1970) argue against the expansion of the desert. According to them if the rate of advancement is taken as 0.8 km per year, then the present boundary should have been 40 km ahead of what it is today. They further argue that if the age of the desert is taken as 5,000 years, as thought by many workers, and the rate of advance as 0.8 km per year then by now the desert would have advanced to at

least the foothills of the Himalayas if not upto somewhere in central Asia.

Meteorological data of the past 70 years suggest no climatological change over the Thar desert and adjoining areas which should be if the desert were advancing (Pramanik, 1952). Rao (1961) examines rainfall data of 80 years of the Thar desert and opines that there is no significant change in the annual regional rainfall of arid Rajasthan.

The present study also suggests that the sands of the Thar desertwore brought in by the rivers which shifted their courses westwards, thus leaving the sediments behind for the free play of winds. It appears that no significant expansion of the desert is taking place.

CHAPTER-3

29

BEDFORMS

3.1 INTRODUCTION

Bedform is a regularly repeated surface feature which develops invariably on the wind blown sand deposits. These resemble with the pattern developed under water. Bedforms have been reported to develop on loess (Rozycki, 1967), in alluvium or even solid rock (Grove, 1960; Wilson, 1971). Cornish (1974) has reported them to develop on snow.

Different bedforms reported by various descrt workers are wind formed draas, dunes, ripples, megaripples, gravel ridges, current lineations, sand ribbons, parallel ridges, linguoid dunes, criss-cross lines, net works and oblique echelon lines.

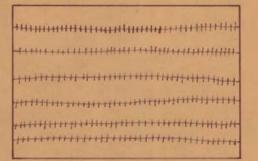
Some basic irregularity on the ground surface or some local disturbance in the wind stream may initiate a particular bedform. This pattern then grows in size and migrates downwind from the site of its origin. Some of the irregularities which may be the ultimate cause of origin of a particular pattern may be listed as a rock outcrop, bush, man made structure, lithology of the surface rock, some erosional or topographical feature, a termite mound or even the older bedforms. A local turbulence of the wind current or change in grain size of the sands may result into a particular type of pattern. Similarly size, shape and orientation of these nuclei may trigger a mechanism which results in different bedforms.

3.2 BEDFORMS OF THE AREA

In the area under investigation, mainly three types of bedforms-ripples, dunes and sand piles, are observed. A brief description of these is attempted below.

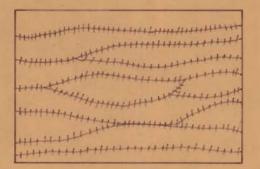
3.2.1 Ripples

Ripples are present ubiquitously in the area. These are asymmetrical in nature and may occur in long straight ridges (Fig. 3.1a). Generally the ripples tend to occur as parallel ridges with wavy crest lines (Figs. 3.1b, 3.2) Another interesting sedimentary structure is sand shadow observed in Figure 3.2 developed behind pebbles. Wavy ripples may run continuously along their general strike for over 30m. Sometimes it has been observed that ripples branch out from the crests (Figs. 3.1c, 3.3). When they branch, it is the crest that bifurcates. The branch of the ripple may join and merge in the adjoining crestline. At times, branching is such that a sort of island of low lying trough is enclosed (Fig. 3.1c). Also ripple crests may occur as crescentic ridges which may be called as arcuate ripples (Fig. 3.1d). Well developed arcuate ripples are observed in the dune field at Dhanana (Fig. 3.4). There is a general tendency of the arcuate ripples to straighten and attain the shape of parallel ripples which are transverse to the dominant wind direction.



(a) Straight parallel ripples

(b) Wavy parallel ripples



(c) Branching ripples

(d) Arcivate ripples

Fig.31_Typical ripples in the area.

Fig. 3.2_ Sinuous asymmetrical ripples are observed in area A. Sand shadows behind pebbles are observed in region B. Location near Dhanana.

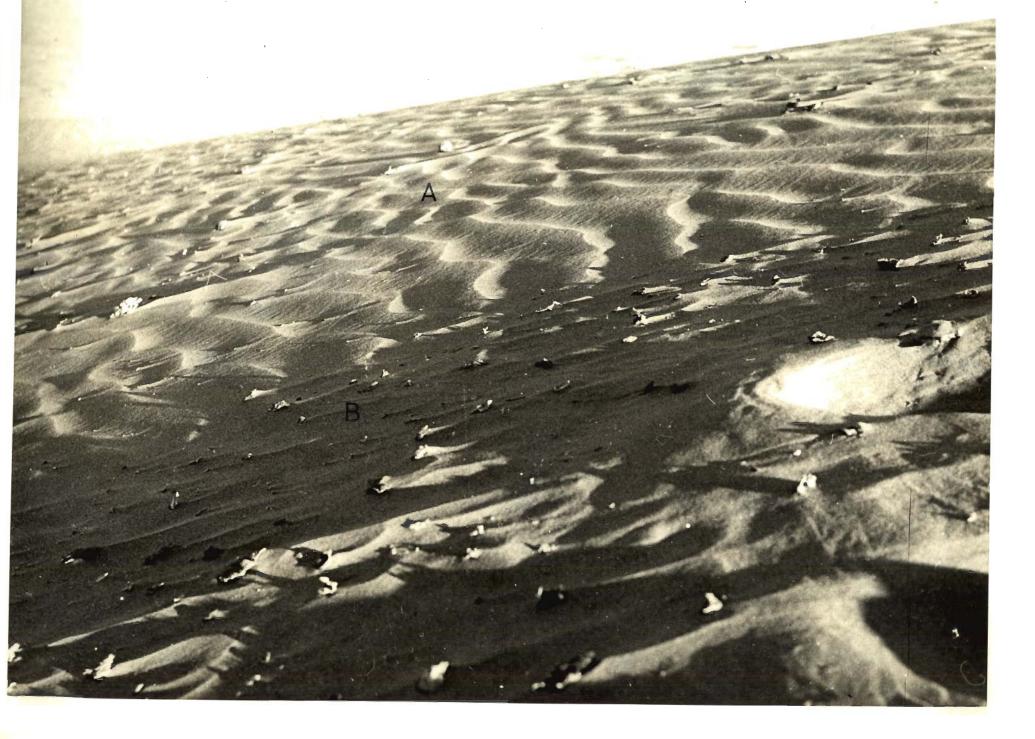
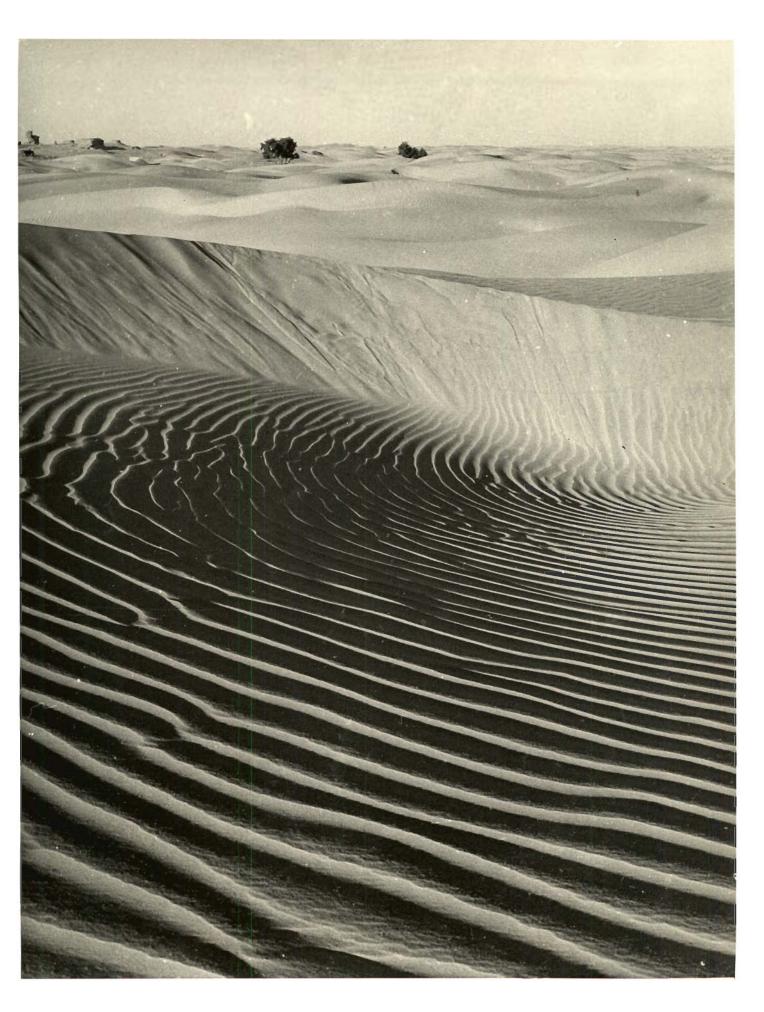


Fig.3·3_Two sets of ripples with crests trending almost at right angles to each other formed at the back of a barchan. Crests of some ripples are discontinuous and those of others show bifurcation. Ripples are truncated by sand avalanche. Location near Dhanana.



Fig.3.4_Flat crested, arcuate, asymmetrical ripples at the back of a barchan in a dune field. Barchans can be seen in the background. Location near Dhanana.



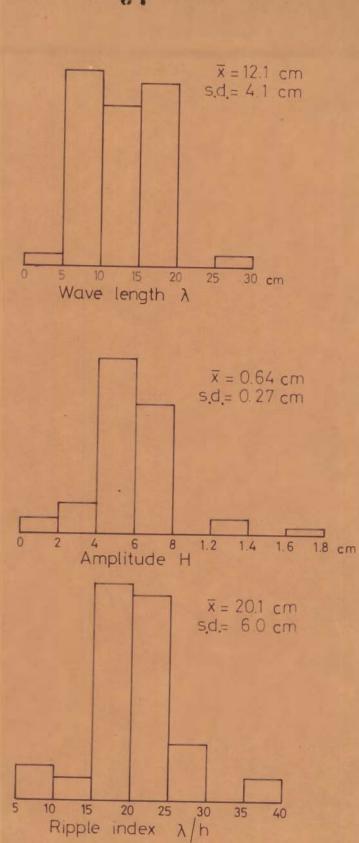
Crests of the ripples are composed of coarse grains whereas troughs are composed of comparatively finer grains. As an example, grain size analysis of samples 1 and 2 collected from the crest and trough of a ripple near Sam shows mean size of 1.78 β and 2.79 β respectively.

The ripples may show abrupt change in wave length and amplitude in downwind direction. Similarly ripples with contrasted morphology may occur in juxtaposition. In such a case the boundaries between these ripples are generally denticulated (Fig. 3.5). It is of interest to note that at both these places the same wind regime prevails. This marked change in the ripple characteristics may be due to the variation in the grain size. An increase in grain size corresponds to increase in wave length. Also, it has been observed that the ripples are rather poorly developed in coarser sediments while the finer sands support skins which are ornamented with well formed ripples.

In the area under investigation, the wave length λ and amplitude H of typical ripples from different locations have been measured and ripple index λ/H calculated. Figure 3.6 gives histograms showing distributions of λ , H and λ/H . Aeolian ripples have mean wave length and amplitude of 12.1 cm and 0.64 cm respectively and a mean ripple index of 20.1. In comparison with the present study, Bagnold (1954) and Sharp (1963) found that for aeolian ripples wave length ranged from 25 cm to 20 m and amplitude varied from 2.5 cm to

Fig.3.5_Ripples of different wave lengths and amplitudes are developed in areas A, B and C. Boundary between areas B and C is denticulated. Barchans are observed in the background. Location near point 43 in figure 13.





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Fig.3.6_Histograms showing distributions of wave length, amplitude and ripple index of aeolianripples.

60 cm. The ripple index was found to have a range of 10 to 70.

In order to find out as to whether any correlation exists between λ , H and λ/H , three plots of H versus λ , λ/H versus H and λ/H versus λ have been prepared (Figs. 3.7-3.5).

Figure 3.7 depicts the variation of H with λ . It is observed that in the range of λ from 4.5 cm to 9.0 cm, the ripple amplitude increases steeply from 0.2 cm to 0.5 cm. Thereafter the increase in H is quite small with increase in λ . For example, corresponding to an increase in λ from 9.0 cm to 17.0 cm, there is only an increase in H from 0.5 cm to 0.8 cm.

The nature of variation of ripple index with amplitude is shown in Figure 3.8. The value of λ/H first decreases rapidly with H and then after a certain critical value of H (4.0 cm to 4.8 cm), the ratio λ/H starts increasing with further increase in λ .

Figure 3.9 shows the variation of λ/H with λ . The ripple index λ/H increases more or less linearly with H.

3.2.1.1 Mechanism of Ripple Formation

The mechanism of ripple formation in fine sand was best studied by Bagnold (1941) in wind tunnel experiments and his ideas are summarised here. Wind blown sand moves

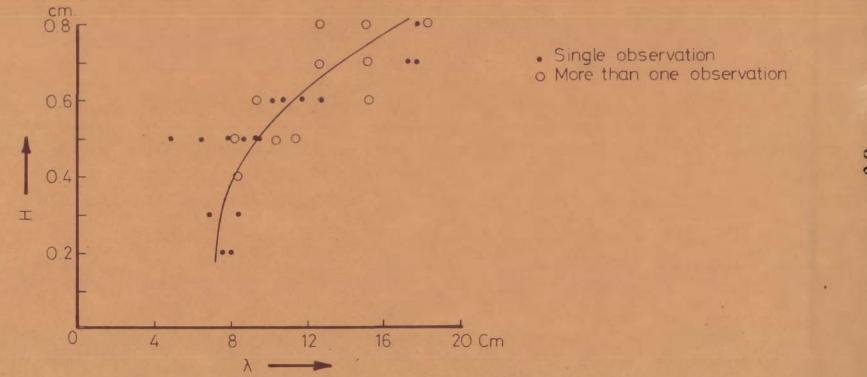


Fig.3.7_Plot of ripple amplitude H vs. wave length λ (Plot includes 46 observations, extreme values being omitted).

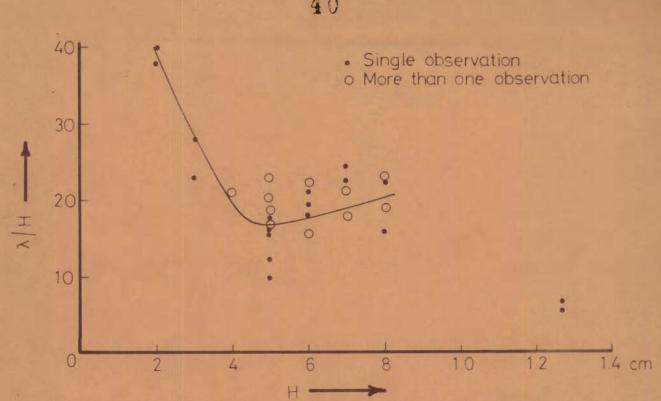


Fig. 3.8_Plot of ripple amplitude H vs.ripple index λ H. Plot includes 48 observations.

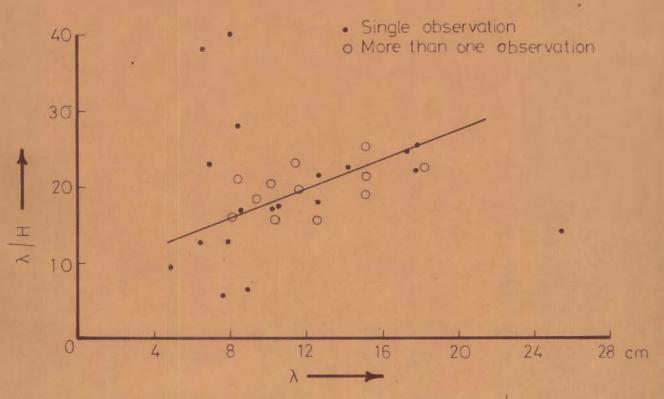


Fig 3.9_Plot of ripple wave length vs. ripple index λ/H . Plot includes all the 49 observations.

largely by saltation. The lengths of the jumps of a particular grain size vary a little from the mean path length which is a function of grain size and wind velocity. Once the saltation starts, any irregularity on the ground surface receives greater bombardment of landing grains on its windward side. Since it has greater angle of incidence with the grain paths, this results in a second zone of denser bombardment downwind at a distance of the mean jump length. This cycle may repeat itself several times downwind before fading out under random processes.

Zones of high and low bombardment are obviously the zones of high and low transport and also zones of erosion and deposition. If such a system gets established once, it would grow until the rate of sand transport at all points on the windward slopes had increased due to increasing angle of incidence with the sand flow. The angle of incidence will increase till it attains a dynamic equilibrium. The ripples thus formed will migrate downwind without changing their shape. The wave length λ of the ripples corresponds to mean jump length.

3.2.2 Dunes

Mainly three types of dunes are encountered in the area, namely, (i) Barchans, (ii) Transverse dunes, and (iii) Longitudinal dunes or seifs.

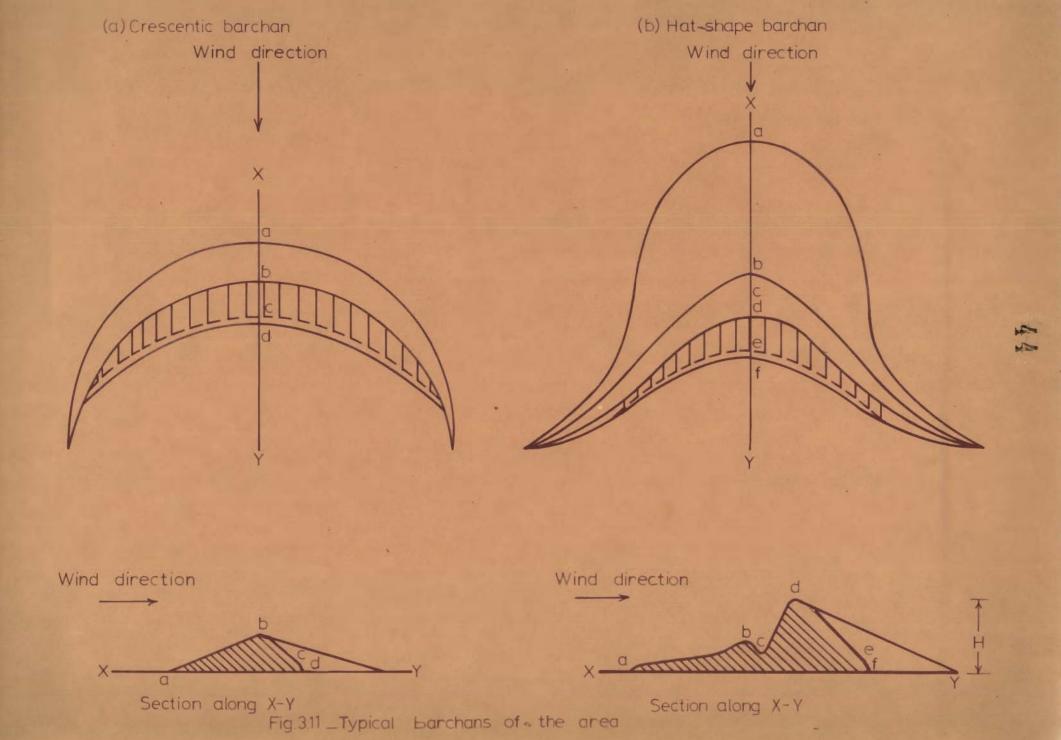
3.2.2.1 Barchans

It has been observed that barchans occur as marginal types of dunes. They attain their zenith in comparatively small areas bordering the region occupied mainly by longitudinal dunes. It appears that crescentic dunes prefer to form on comparatively firm ground or on shallow sands where the bottom of firm ground is closeby. The relatively small area covered by barchans together with their preferential marginal occurrence on comparatively firm ground or thin sand cover may perhaps be due to insufficient sand supply. The skins of barchans are ubiquitously rippled. Figure 3.10 shows leeward view of barchans near Dhanana.

Table 3.1 gives morphometric measurements of four barchans of Sam area. The windward sides of these dunes make angles of 15° to 20° and the leeward sides 26° to 32° . At most places leeside does not attain angle of 32° which is the angle of repose of these sands. It has been observed that a narrow band (0.5 m to 1 m wide) with a higher angle of slope (about 32°) invariably occurs at the foot of the leeslope making a sharp contact line with the ground surface (Fig. 3.11, points c,d). Slope longths measured from the highest point on the crest to the beginning of the slope near the ground surface on windward and leeward sides are 6 to 14 m and 3 to 10 m respectively. Height of dunes varies from 2 to 10 m or even more in Dhanana dune field. Barchans of Lunar area are quite grown up and attain heights upto 10 to

Fig. 3.10 Leeward view of barchans. Location near Dhanana.





12 m above the ground surface.

Table 3.1- Morphometric parameters of barchans

| | | | **** | | |
|--|--|------------------------|---------------------------|------------------------------------|------------------------------------|
| Sample Location in Fig.1.3 | Dune Characteristics | | | | |
| | Length L | Breadth B | Height H | Windward slope Oj | Leeward slope θ_2 |
| 3 5 7 | 20.0 m 69.7 m | 16.7 m 60.0 m | 1.8 m 1.7 m | 15 ⁰ 20 ⁰ | 26 ⁰ 32 ⁰ |
| 8 | 90.0 m 83.3 m | 73.3 m 73.3 m | 6.7 m 5.0 m | 20° 20° | 31 ⁰ 32 ⁰ |
| Length L - the distance measured parallel to the wind direction between the tip of horn and the beginning of windward slope, | | | | | |
| Breadth B | the distance between tips of horns measured at right angles to the wind direction. | | | | |
| Height H | - the maximum height of the crest above general ground surface, | | | | |
| Slopes O _l an | | nsurements in from the | parallel to highest po | o the wind bint on th | direc- e crest. |

A barchan may get stabilized due to the cohesion imparted by the moisture and compaction. In such a case it may get partially or completely buried under the consignments of sands of the subsequent seasons. Thus two families of barchans may be recognised in the area — first, that may be called as active dunes, which are loose enough to respond to the shepherding action of the winds, and the second, stabilized dunes which are apparently belonging to the previous years.

It is difficult to study the internal structure of active dunes since pitting leads to sliding of loose sediment. In the stabilized dunes, wind has scooped pits and trenches at places to expose internal lamination (Fig.3.12), which is more or less conformable to the slip face. The internal structure of a dune gets more distinct on a surface which has been reworked by the wind.

Chiefly two types of active barchans are recognised, each with its characteristic shape. The first type is more or less perfect crescent in shape (Fig.3.11a). The second variety, not reported earlier, has a shape which can be compared to a hat with curved flanks. A narrow trench, . 2 to 3 m down the crest line traverses the windward slope with the deepest point at C (Fig.3.11b). The depth of this trench varies from 0.5 to 1.5 m,from dune to dune. The trench opens up on flanks of the dune. Such hat shape dunes are well developed near Sam but were not found either in Dhanana or Lunar dune fields. The difference in the morphology of these barchans may be summarised as below:

Crescentic Barchans

(i) Perfect crescent

(ii) Flanks are arcuate with convex side facing the wind direction

Hat-shape Barchans

- (i) Appears like a hat, the domal convexity of which faces the wind direction.
- (ii) Flanks are concave on the sides.

Fig. 3·12_Foresets of cross-bedding exposed in a cut made by wind in a barchan. The foresets dip at about 30° in a northerly direction. Location near Dhanana.



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- (iii) Windward slope contin- (iii) Windward slope uous without any trench
 - has a narrow trench some distance down from the crest.
 - (iv) Slope angle of windward (iv) A high angle windward side is gentler than the lee slope.
 - face starts dipping till it terminates in the trench.

3.2.2.2 Mechanism of Formation of Barchans

Mechanism of formation of barchans is a complex process which is influenced by the sand and wind characteristics. However, formation of barchans may be visualized in the following three stages.

(i) Initiation or nucleation stage - Any irregularity of the ground surface or a chance turbulence in the wind current may trigger off a process which may initiate a sandy patch hardly resembling its future crescentic form. This may be called as the embryonic stage. The size, shape and orientation of the nucleus may determine the type of future barchan. With the subsequent onslaught of fresh consignments of sand the patch grows into a tiny mound with a round elevated head and tapering but downwind Swopt arms. Here a resemblance to a barchan appears.

(ii) Youth Stage - Addition of fresh consignments continue to pile up as wind alters its velocity after reaching raised surface of the sand mound. A gentler windward slope develops with a steeper slip face in the leeward side which steepens to angle of repose with the continued piecemeal consignments of sediments across the crest line

from the windward side. The barchan is well established. This is a stage when the barchan attains a dynamic equilibrium with the prevalent environmental conditions. Main wind current, in assistance with the lee and windward eddies, gives finishing touches to the morphology of the dune which may start migrating. Their typical crescentic shape may be ascribed to the differential rate of migration of the central part and the horns.

(iii) <u>Old Stage</u> — In this stage barchans may attain a relative stabilization due to cohesion imparted by moisture and compaction of deeper parts. A barchan may get distorted if wind direction changes or it is subjected to winds from different directions.

3.2.2.3 Wind Eddies and Barchans

Existence of wind eddies in the strong to moderate winds blowing over barchans are well recognised and are attributed to sudden break in slope at the crest of the dunes (Cornish, 1857, 1914; Hoyt, 1966). Occurrence of lee eddies and windward eddies has also been observed in the present area. A schematic representation is shown in Figures 3.13a and 3.13b. Following evidences may be cited in favour of the existence of lee eddies:

- (a) When dust was dropped it followed the trend of eddy as shown in Figures 3.13a and 3.13b.
- (b) Modification of leeslope near its foot.

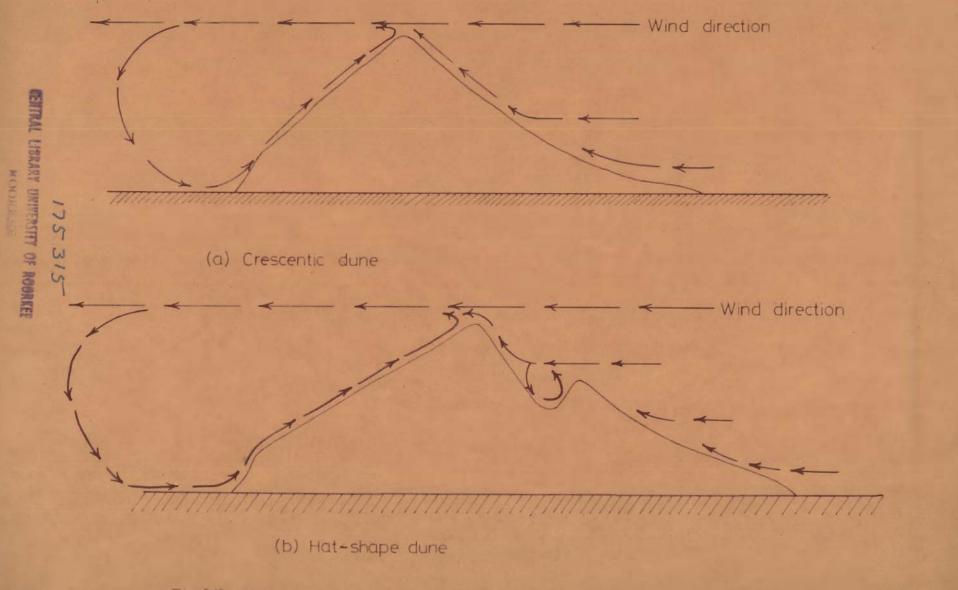


Fig.3.13 _Wind eddies around the barchans.

- (c) Well swept ground of the shadow zone.
- (d) Existence of sharp contact line of leeslope with the ground surface.

It appears that a windward eddy also occurs (Fig.13.3b) which scoopes a shallow trench and modifies the morphology of the windward slope on a hat shaped barchan.

3.2.2.4 Transverse Dunes

These arc huge dunes resembling ripples with wavy crest lines which are transverse to the dominant wind direction. These develop on sand piles where the thickness of sand is considerable. The length of a single crest line may exceed 50 m. Well developed transverse dunes are found near Sam. Transverse dunes may be sinuous with their crest lines broken at places (Fig. 3.14). The total percentage of transverse dunes is very meagre in the arca. There is absolutely no difference in the morphology of transverse dunes of Sam and Dabri areas. Here too, windward slope is gentler as compared to the leeslope which is slightly less than the angle of repose. Transverse dunes too, like other types of dunes, support a rippled skin. Barchans and transverse dunes may occur together where the former may form on flat ground surface while the latter may extend from the ground surface up the sand piles but always striking more or less at right angles to the dominant wind direction.

Fig.3·14_Wavy, parallel ripples on transverse dunes having sinuous crests. Location near Sam.



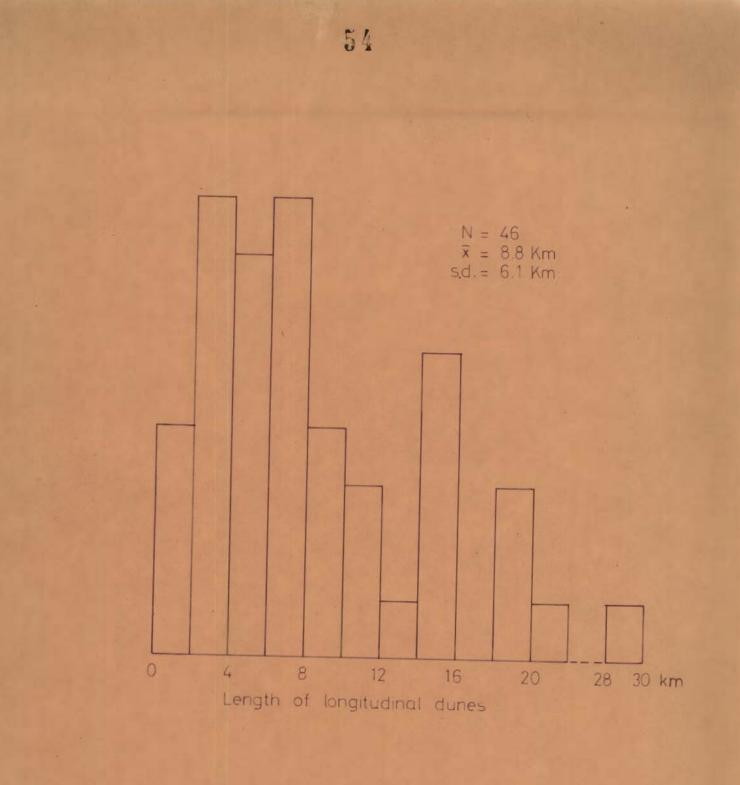
3.2.2.5 Origin of Transverse Dunes

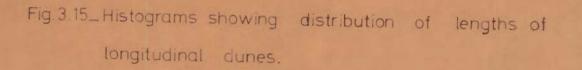
Observations in the area under study indicate that two adjacent barchans may join laterally at the horns making a deep re-entrant angle in-between. With further deposition of sands the re-entrant may get buried and ultimately may disappear altogether. Consequently crest lines of two adjoining crescents may become one to form a wavy summit line thus developing a huge transverse dune, but it does not preclude their independent development.

3.2.2.6 Longitudinal Dunes

The area southwest and north of Dhanana is occupied by longitudinal dunes. These dunes usually attain heights of about 10 m or more and have a mean length of 8.8 km as measured between two farthest ends. Figure 3.15 depicts a histogram showing distribution of lengths of longitudinal dunes in Dhanana area as measured from topographic maps. These dunes trend approximately SW-NE. These form 'Y' shaped bifurcations and invariably 'Y' opens in the southwest direction that is facing the wind direction. Flat interdune areas have widths ranging from 0.1 to 0.2 km and may be occupied by barchans. Seif dunes under consideration are stabilized and these may be eroded by wind at places exposing internal lamination. Figures 3.16 and 3.17 show horizontal internal laminations of these dunes in trenches cut by wind. Directions of the trenches are approximately

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Fig.3.16_Horizontal, parallel laminations exposed in a cut made by wind in a longitudinal dune. The cut is roughly parallel to the crest of the dune. Location near Murar.

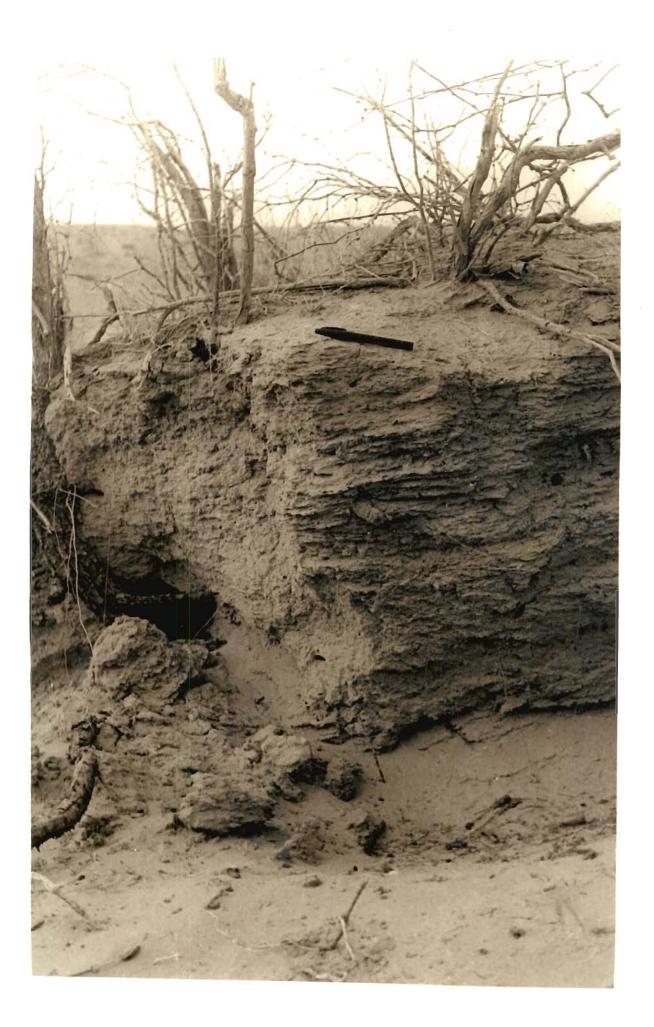


Fig.3.17_Horizontal, parallel laminations exposed in a cut made by wind in a longitudinal dune. The lower half of the face contains a small scale, solitary crossbed. The cut is roughly parallel to the dune axis. Location near Murar.



parallel to the dune axes.

3

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3.2.2.7 Origin of Longitudinal Dunes

Frere (1870) felt that longitudinal dunes were produced when the predominant winds furrow the sand and deposit them on the ridges in between.

Blanford (1876) thought the longitudinal dunes of the Thar desert to be erosional features. Enquest (1932) suggested that longitudinal dunes are formed on thick sands with deep water table. Melton (1940) suggested the term 'windrift dunes' since wind excavated blowouts in thick sands to build long parallel ridges.

Bagnold (1953) gave the idea of helicoidal air flow to explain the mechanism of formation of longitudinal dunes. According to him if moving wind is heated, convection will form paired roller-vortices in the lower atmosphere with their axes horizontal and trending in the wind direction. Such a movement will tend to sweep the sand from troughs and pile them on the intervening dunes. This process involves partly erosion and partly deposition. Folk (1971 a, b) also thought that similar mechanism was responsible for the formation of longitudinal dunes and obtained experimental evidence for the bifurcation angle of these dunes. Glennie (1970) considers that other conditions being equal, barchans develop at slow to moderate winds while seifs are formed at higher wind velocities. Stronger winds during the Pleistecene glaciation resulted in abundant seif formation.

Certain aspects about the relationship of longitudinal dunes and the wind directions are discussed further in Section 3.3.

3.2.3 Sand Piles

Large irregular sand accumulations are designated as sand piles. Many such sand bodies are found in the area which may be a couple of hundred meters in maximum length and a few meters high above the general ground surface. Sandpiles are essentially stabilized sand accumulations. At places, these have been reworked and sand has been piled into transverse and barchan dunes which may be associated with them. These are especially abundant in Lunar and Dabri areas and are associated with regular barchans and transverse dunes.

Origin of sand piles is not clear. Their general stabilized nature, predominant SW-NE trend which has been recorded in the topographic maps as linear sand accumulations coupled with the occurrence of well established longitudinal dunes in the near vicinity suggest that these sand piles are probably low longitudinal dunes which are rather difficult to recognize in the field because of their relatively low heights.

Some of the sand piles are, of course, definitely buried and stabilized barchans as observed in the field.

3.3 <u>RELATIONSHIP BETWEEN WIND DIRECTION</u> AND DUNE ORIENTATION

Blanford (1876) was the first to establish parallelism of longitudinal dunes and the present wind direction in the Thar desert. Similar relationship between the wind direction and the longitudinal dunes have been reported from Egyptian and Libyan deserts by Ball (1927), Bagnold (1931,1933), Kadar (1934) and others, and from the Australian desert by Madigan (1930, 1936, in Folk 1971a). Melton (1940) and Glennie (1970) thought that strong winds of constant direction were necessary for the windrift dunes. Other workers like Madigan (1930, 1938, 1946, in Folk, 1971a), Wingate (1934), King (1956, 1960), Veevers and Wells (1961) and Folk (1971a) have also emphasized the parallelism of seifs with one predominant wind direction, but also stressed the importance of secondary cross winds in producing crestal asymmetry and in the shepherding effect of transporting sands from troughs onto dunes.

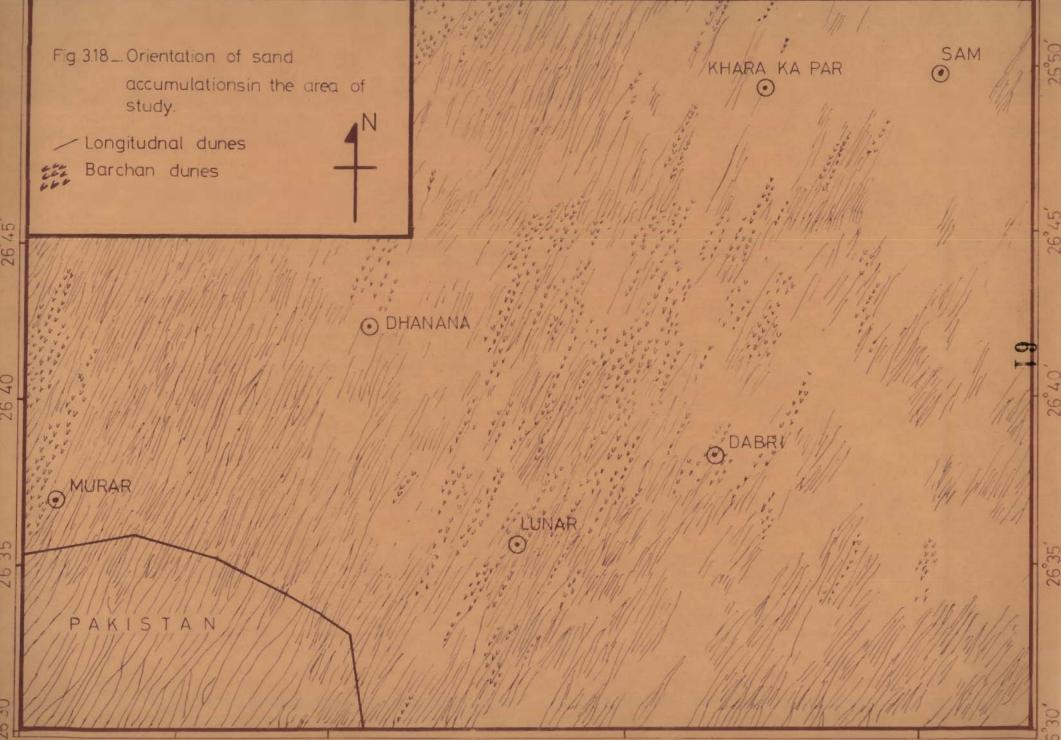
Most workers think that a strong constant wind from one principal direction is necessary for the formation of barchans (Verlaque, 1958; Finkal, 1959; Long and Sharp, 1964; Hastenrata, 1967; Clos-Arceduc, 1967).

Bagnold (1941) proposed that two or more wind patterns at an angle were necessary for the formation of longitudinal dunes which become aligned with the resultant wind direction. Later workers like Cooper (1958), Durand de Cabiac (1958) and McKee and Tibbitts (1964) seem to confirm this view by studies in different deserts. Striem (1954) found Israelite seifs to be parallel to the yearly resultant wind direction.

More recently Wilson (1972,1973) questioned earlier explanations of aeolian bedforms. He believed that patterns in aeolian bedforms result from the three dimensional geometry of fluid flow in which there were flow transverse (wave like) and flow parallel (helical, vortex) types of secondary motion. Combination of these yield flow transverse, flow parallel, sinistral and dextral flow oblique bedform elements. Thus seifs may be at an angle to a dominant flow which is determined by the geometry of secondary flow.

Warren (1976) thought that the friction at the earth's surface induces deflection of ground wind from geostrophic direction and the progressive change with height is known as the 'Ekman Spiral'. Dune fields with rougher surfaces and higher altitudes than the neighbouring areas may show such deflections from the wind direction.

Figure 3.18 shows the sand body elongations in the area under study as obtained from 1:50,000 scale topographic sheets of the Survey of India. Thus net sediment transport direction of N 5° E to N 30° E can be seen. It may be emphasized that both the stabilised and active dunes give similar sediment transport direction indicating thereby that the same wind regime has been prevailing since the formation of stabilized dune system.



Figures 3.19 to 3.21 show normal percentage frequencies of wind direction in the form of rose diagrams at Jodhpur (26°18': 73°01'), Barmer (25°45': 71°23') and Bikaner (28°00': 73°18') using the Climatological Tables of the Meteorological Office, Bombay (Anon.,1953). The percentages of number of days under eight compass directions have been taken into consideration.

The main wind speed for each month is given in Table 3.2. The data are obtained from the Climatological Tables of Meteorological Office, Bombay.

| Station | Jan | Feb | Mar. | April | May | June | July | Aug. | Sept. | Oct | Nov | Dec. |
|---------|-----|-----|------|-------|-----|------|------|------|-------|-----|-----|------|
| Jodhpur | 10 | 10 | 10 | 10 | 16 | 20 | 19 | 14 | 11 | 8 | 8 | 9 |
| Barmer | 8 | 8 | 9 | 9 | 10 | 12 | 11 | 9 | 9 | 8 | 6 | 6 |
| Bikaner | 5 | 6 | 7 | 8 | 10 | 12 | 11 | 10 | 9 | 6 | 4 | 4 |

Table 3.2 - Mean wind speed (km/hr).

The resultant wind directions at Jodhpur and Barmer in the months of May, June, July and August are S 43 W, S 47 W, S 47 W, S 47 W and S 38 W, S 49 W, S 49 W, S 46 W and s 45 W respectively (Pramanik, 1952). At Jodhpur 12, 21 and 18 percent of the total days of May, June and July respectively have the wind speed range of 20.92 - 61.15 km/hr. At Barmer 15, 15 and 6 per cent of the total number of days of May, June and July have similar range of wind speed (Pandey et al. 1964). During winter months, northwesterly

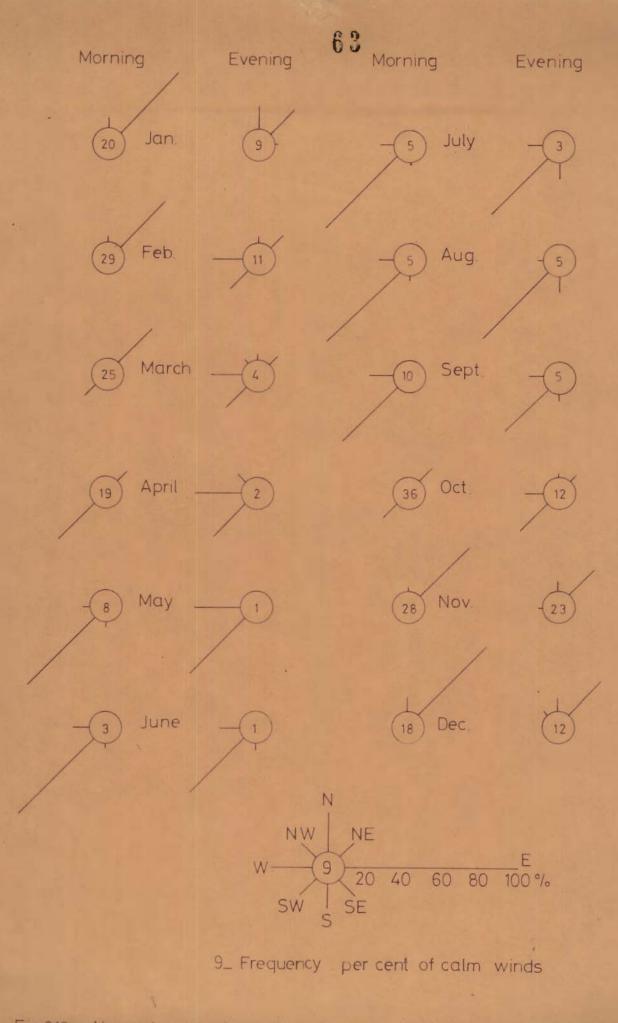


Fig.3.19 _ Normal percentage frequencies of wind direction at Jodhpur

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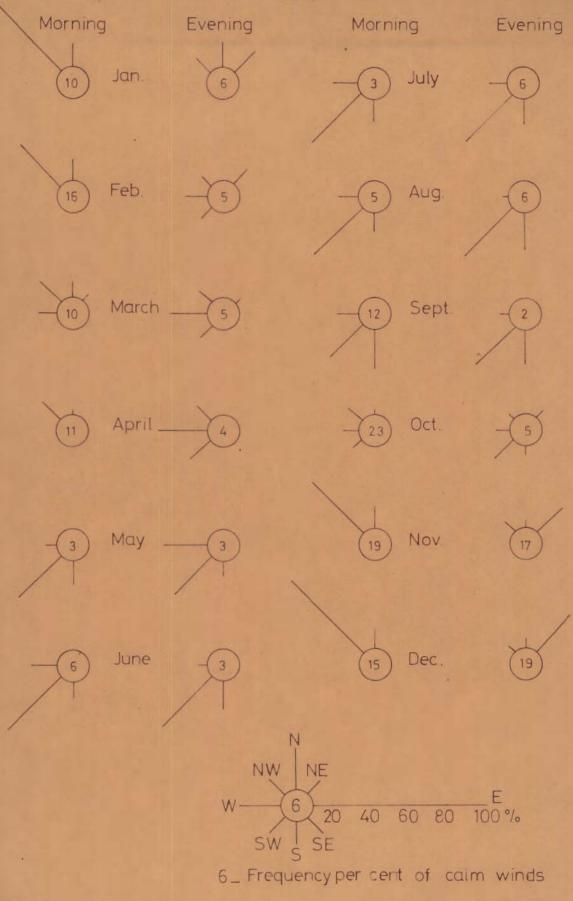


Fig.320-Normal percentage frequencies of wind direction at Barmer

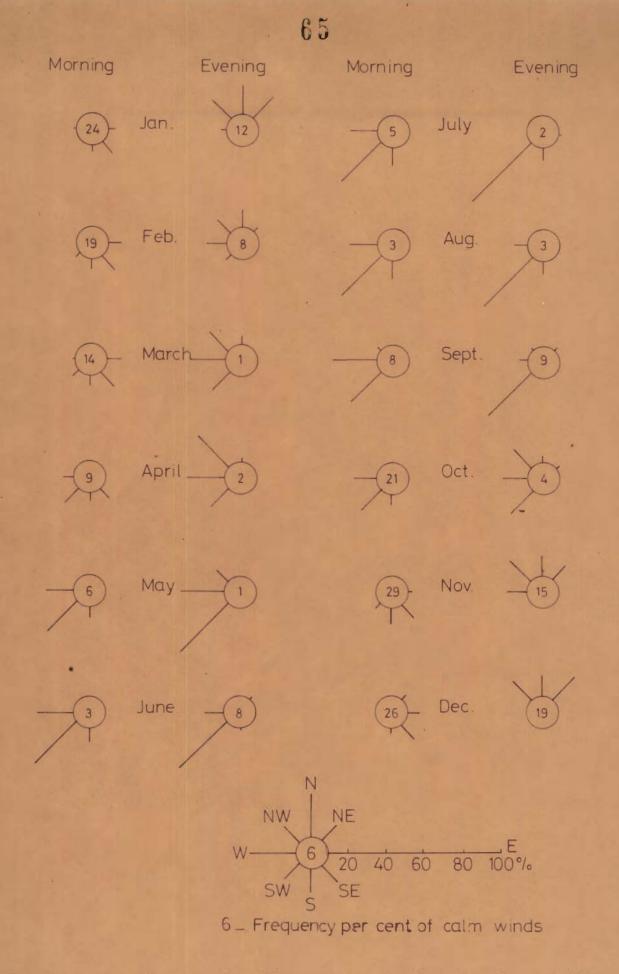


Fig.3.21_Normal percentage frequencies of wind direction at Bikaner

and northeasterly winds predominate which cannot shift sands since they are considerably weak. Similar conditions prevail at Bikaner also.

Thus, it can be concluded that summer winds commonly from S 43°W to S 47°W direction are important factors that control the formation of bedforms. This study shows that longitudinal dunes and barchans give net sediment transport direction which is consistently 15° north of the resultant of dominant summer winds. This deflection is probably due to 'Ekman Spiral' effect described by Warren (1976).

TEXTURAL STUDIES

4.1 INTRODUCTION

Each environmental setup with its complex set of physical and chemical variables leaves a distinct imprint on the sediments deposited in it. The present chapter attempts to evaluate textural attributes of the desert sediments so that these might be used for recognizing similar environments in the stratigraphic column. Chiefly grain size, roundness and sphericity have been studied and are described below.

4.2 GRAIN SIZE ANALYSIS

4.2.1 Purpose

Sediments of alluvial, beach and shallow marine environments have been studied in fair detail for their grain size distributions using modern statistical parameters. However, there is a great paucity of systematic analyses of sediments of inland desert dunes. A few limited studies have been made of these sediments. Alimen (1957) and Chavaillon (1964) have studied Saharan desert samples for mean size and sorting. Moiola and Weiser (1968) studied thirty sand samples from several deserts and showed the relationship between different parameters. Wait (1969, in Folk, 1971a) and Folk (1971a) studied variation of grain size parameters of dunes west of Texas (U.S.A.) and Simpson desert respectively. Folk (1966, 1968a) and Skocek and Saadallah (1972) emphasize widespread occurrence of bimodal sediments in deserts. Skocek and Saadallah (1972) find that statistical grain size parameters of aeclian sands of Iraq show a larger variation than previously thought. Baillieul (1975) concludes that cover sands in different parts of Botswana are largely derived locally on the basis of study of mineralogy and grain size distribution.

The present study attempts a detailed analysis of areal distribution and interrelationship of the various grain size parameters and their possible use in distinguishing desert sediments from sediments of other environments. It also investigates grain size distribution in different parts of barchans.

4.2.2 Collection of Samples

Sand samples were collected from different locations in the area which are shown in Figure 1.3 and their details are given in Appendix I. Samples were collected from the various desert bedforms i.e. barchans, transverse dunes, ripples and sand piles and flat interdune areas. Generally thin top layer was removed and 0.5 kg of sand, from surface to 8 cm depth, was taken. Fairly large number of samples were collected from the different parts of barchans.

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4.2.3 Sample Preparation and Sieving

Field samples were split to obtain 30 to 80 gm of representative sub-sample. A mechanical splitter was designed and fabricated to obtain the sub-sample of required size (Fig.4.1). The sample is poured at the top hopper and in passing through the splitter, it gets halved five times to give 1/32 of the original sample in one container and the rest in the other. The splitter is fitted with a 50 cycle electrical vibrator having a variable amplitude device to hasten the splitting process.

ASTM sieves with 1/20 interval were used to analyse the samples. The samples were shaken for ten minutes on a rotap. Another device which may be called a transfer-funnel (Fig.4.2) was designed and fabricated for transferring the various sample fractions retained on different sieves into weighing containers. The transfer-funnel is a big metallic funnel mounted on a stand with the funnel angle more than 45° . This is also fitted with a 50 cycle electrical vibrator to quicken the transfer of material from a sieve, which is put up side down on the funnel fitting in the spring clips, to the weighing containers. This device keeps losses of sediments due to clogging of sieves to a minimum.

Various sample fractions were accurately weighed upto one hundredth: of a gm and the data are given in Appendix II.

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Fig. 4.1_ A photograph of the sample splitter. 1/32 of the sample poured at the top is collected on the left side and the rest in the front.

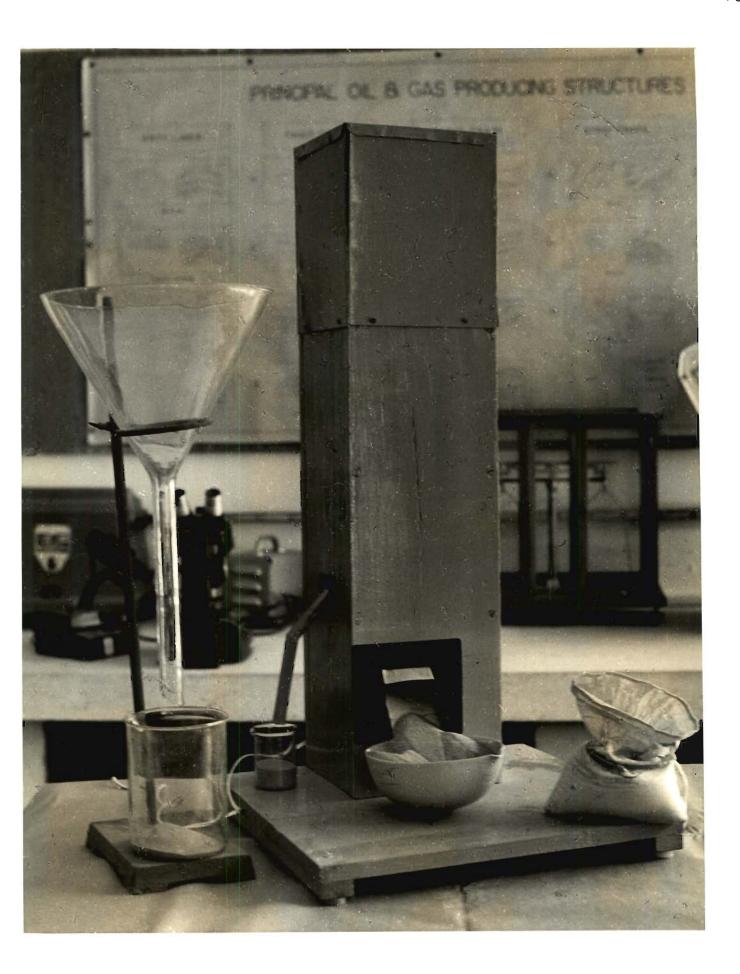


Fig.4.2_A photograph of the transfer funnel The funnel is fitted with a vibrator. The sieve to be emptied is put at the top in up side down position.



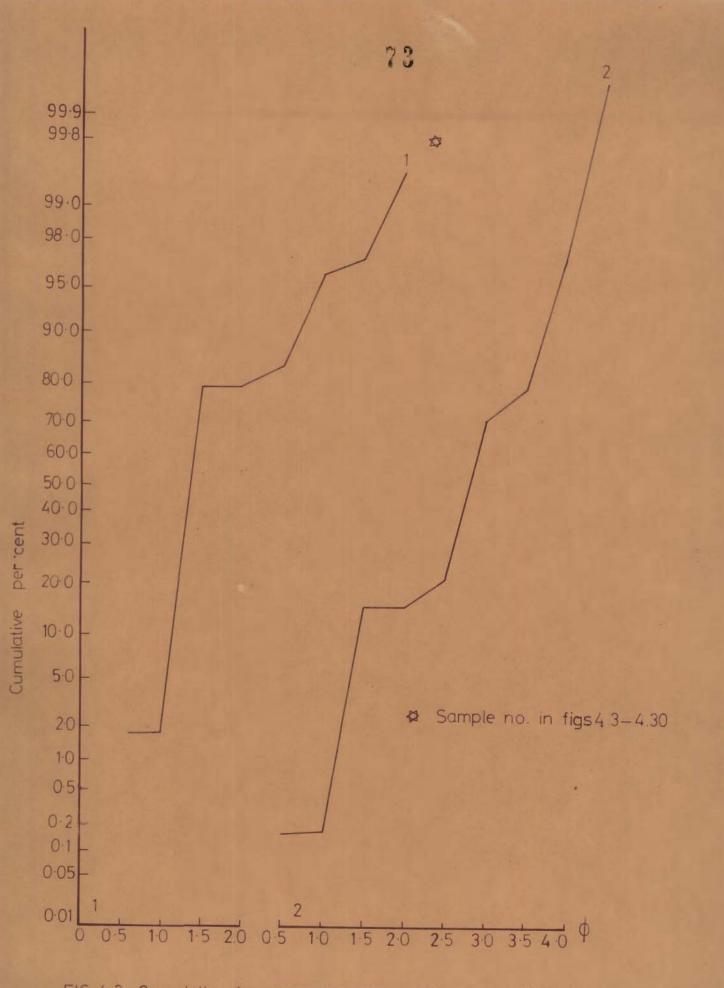
4.2.4 Analysis and Presentation of Data

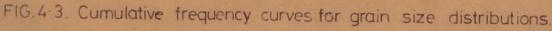
Grain size data were analysed using an IBM 1620 computer. Cumulative per cent frequencies were calculated and plotted on arithmetic probability papers as given in Figures 4.3 -4.30. Further analysis of grain size data could be carried out by two approaches. First method is to compute moment measures using all the grain size fractions. The second method is that of graphical computations. In the latter technique, a cumulative percentile curve is plotted and the various percentile values are read from it to compute the different moment statistics.

In the present study, the second method has been preferred because as pointed out by McBride (1971,p.118-119) computational technique cannot handle 'open ended' distributions well. Secondly the assumption, that all the grains within a size class are assumed to be distributed as if they have a grain size equal to the middle point of that size grade, is not strictly true. Also, results obtained from the graphical computation can be compared well with those published in literature, as this method is most popular with geologists.

Graphical grain size measures were calculated by using a computer. A cumulative per cent frequency curve was obtained by fitting normal curves between adjacent observation points and then the various percentile values needed for calculations of different graphical measures were obtained which are listed in Appendix III. A number of graphical

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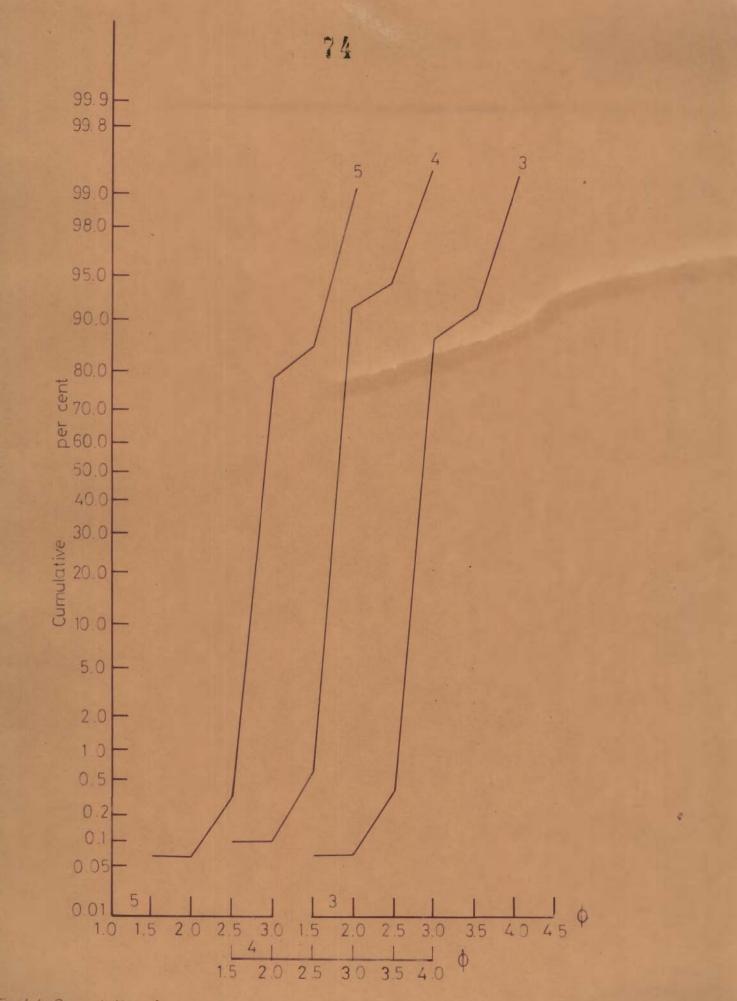


Fig. 4.4_Cumulative frequency cruves for grain size distributions.

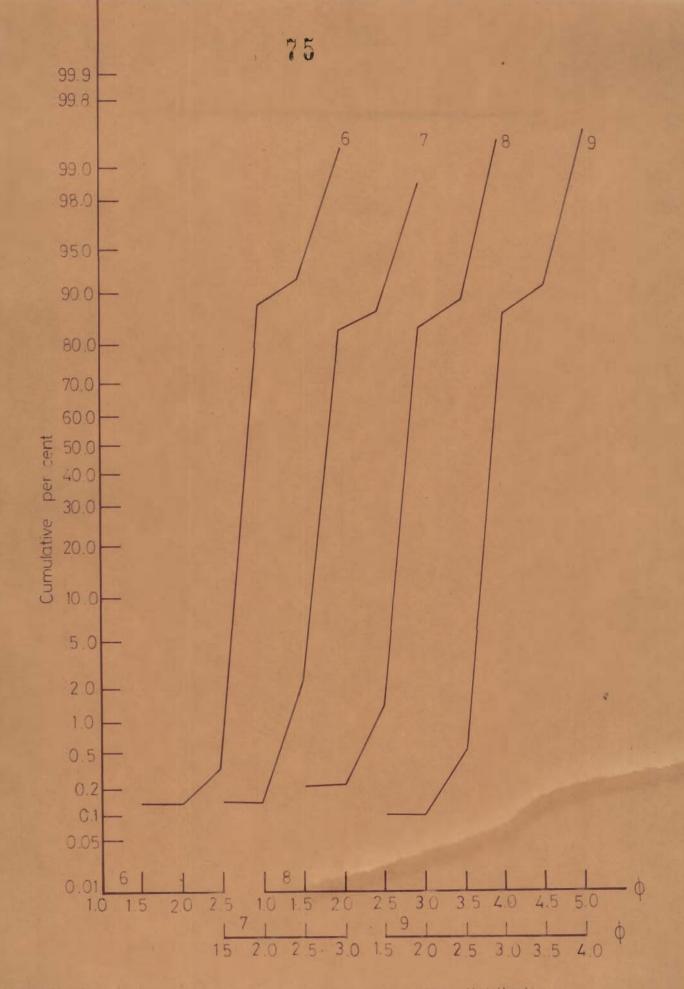


Fig.4.5_Cumulative frequency curves for grain size distributions

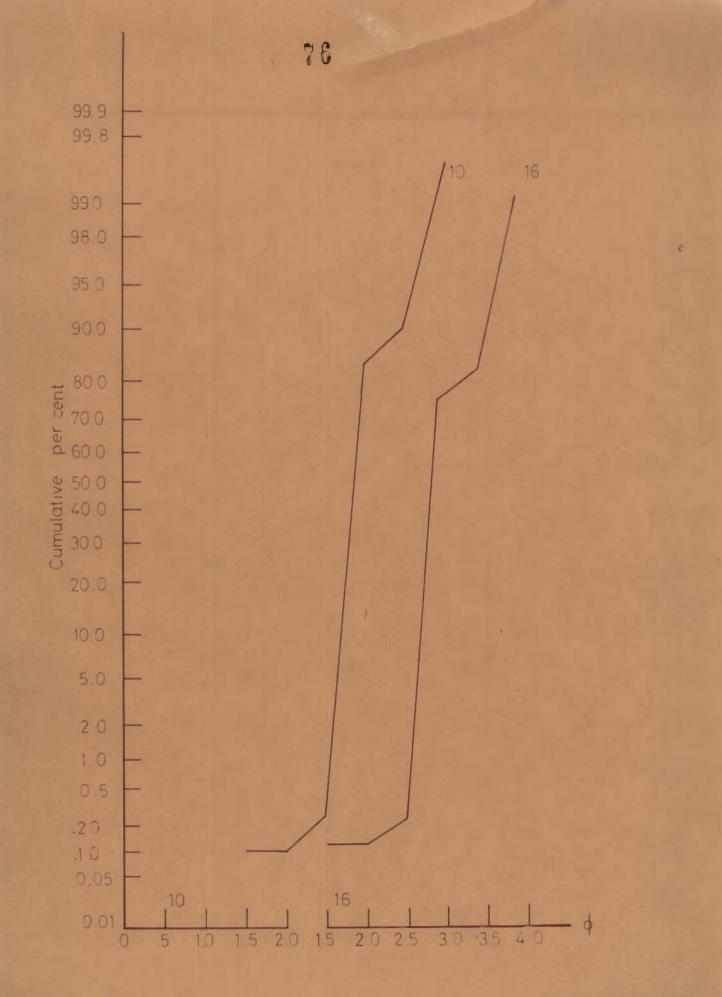


Fig 4.6_Cumulative frequency curves for grain size distributions.

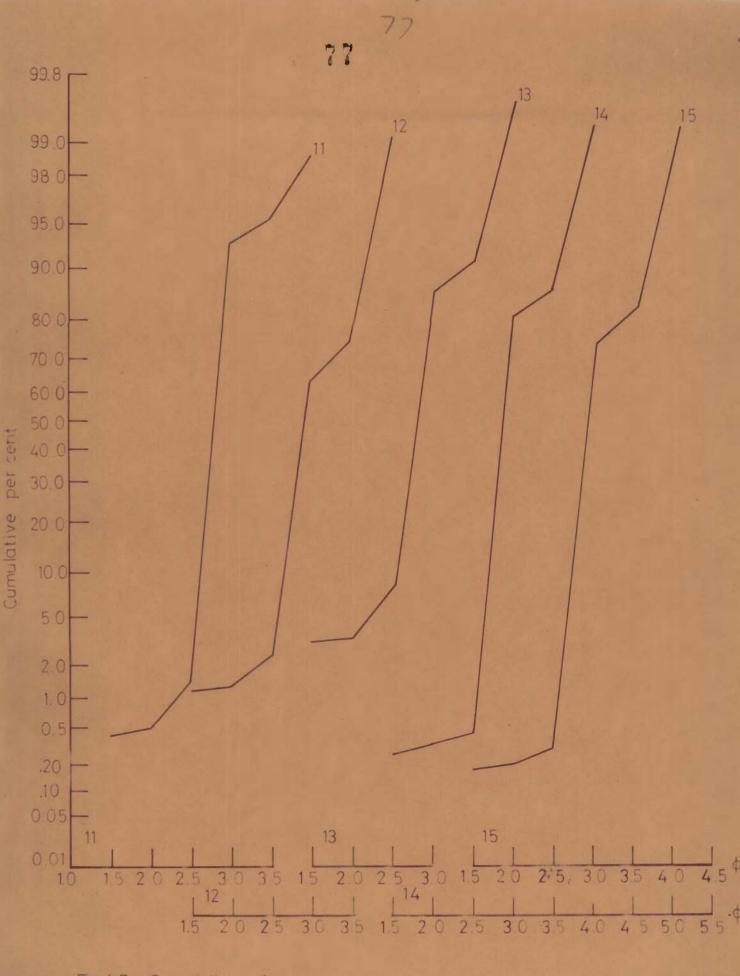


Fig. 4.7 _ Cumulative frequency curves for grain size distributions

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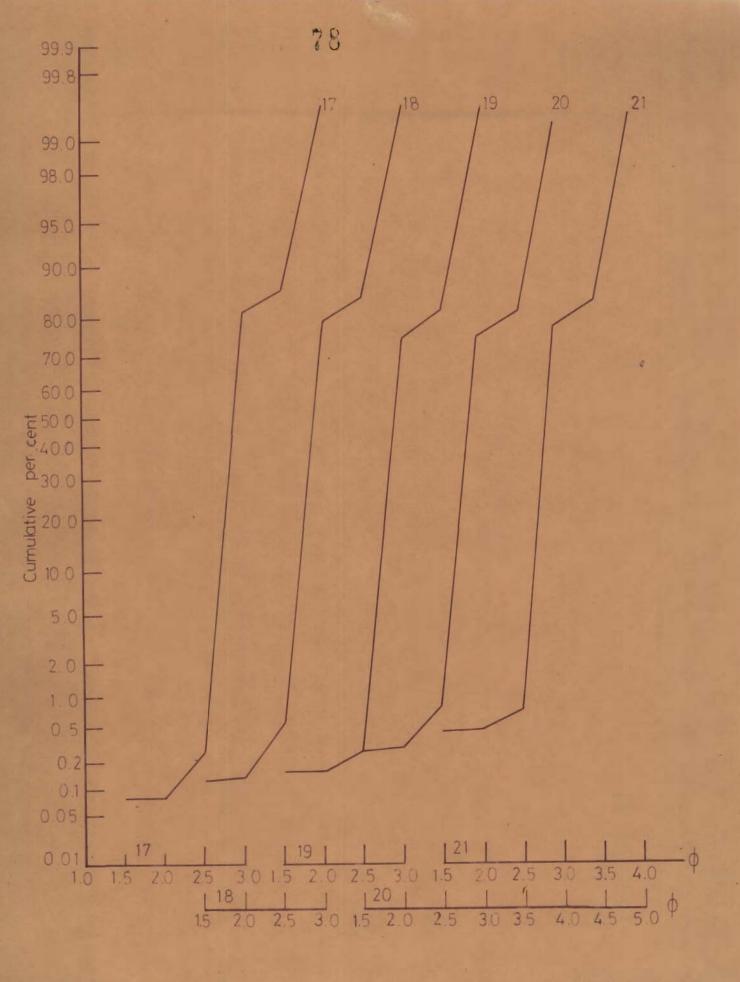
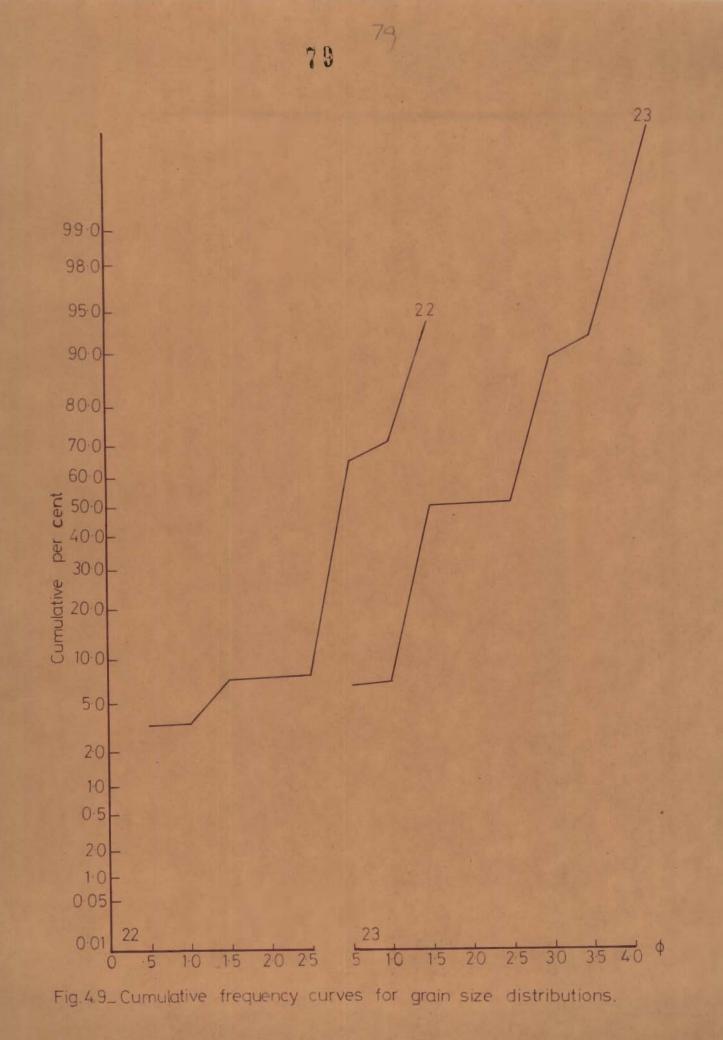


FIG.4.8 _ Cumulative frequency curves for grain size distributions

1.1



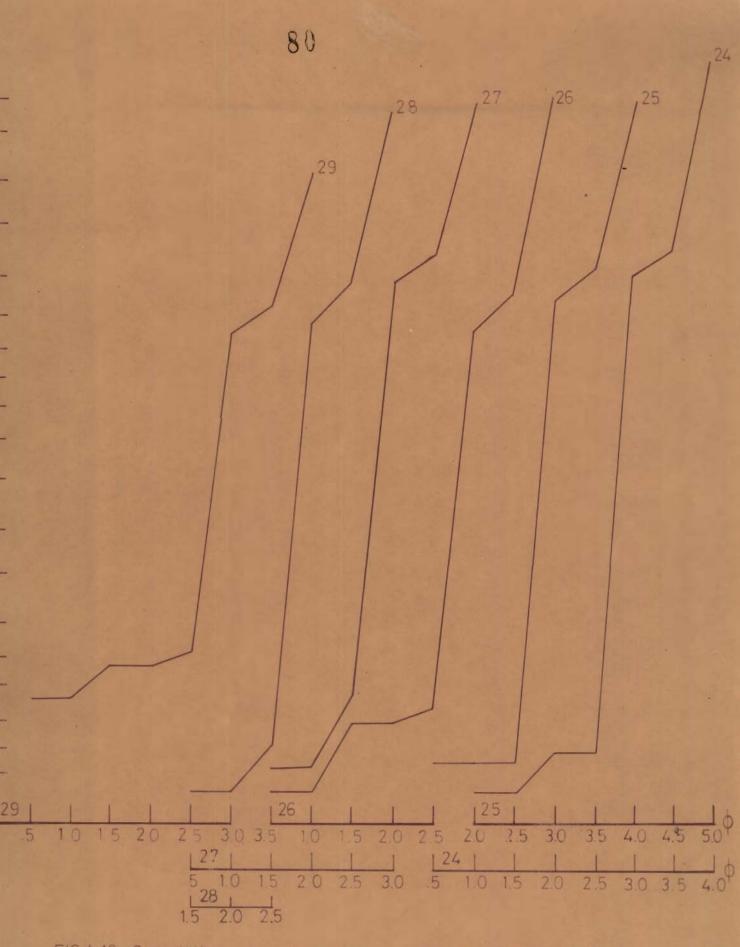


FIG.4.10_Cumulative frequency curves for grain size distributions.

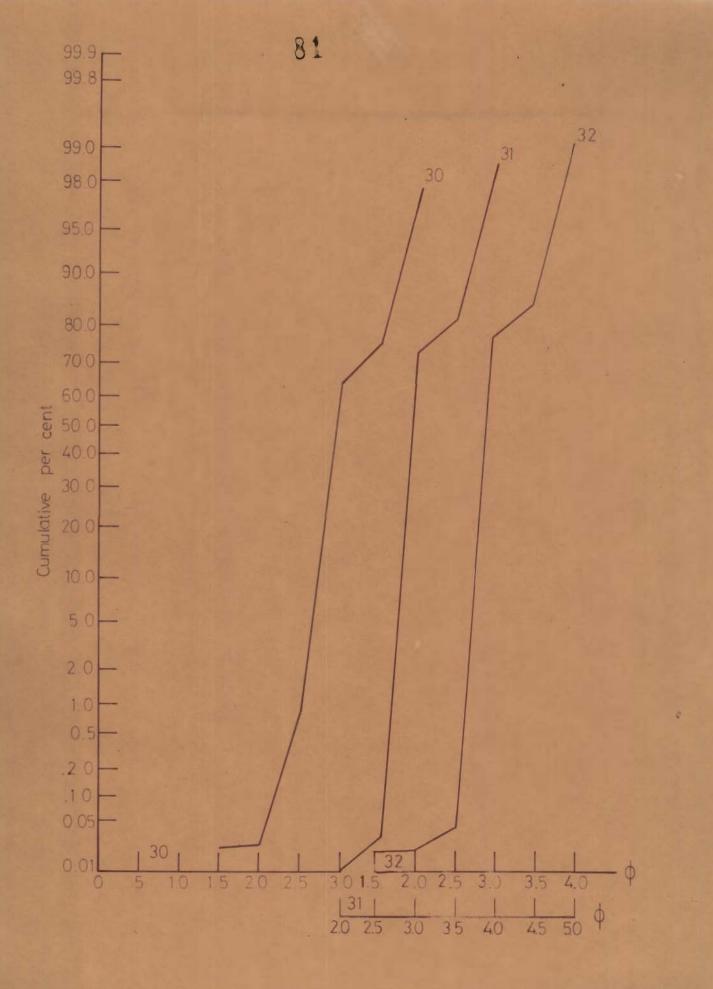


FIG.4.11 _ Cumulative frequency curves for grain size distribution.

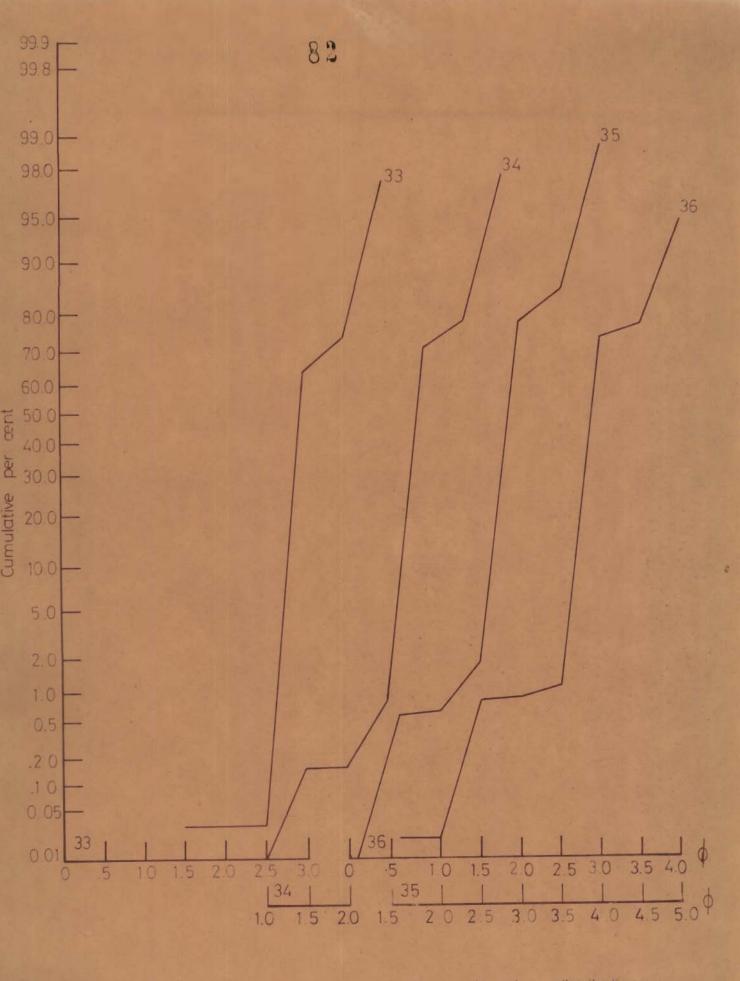


FIG.4.12 _ Cumulative frequency curves for grain size distributions

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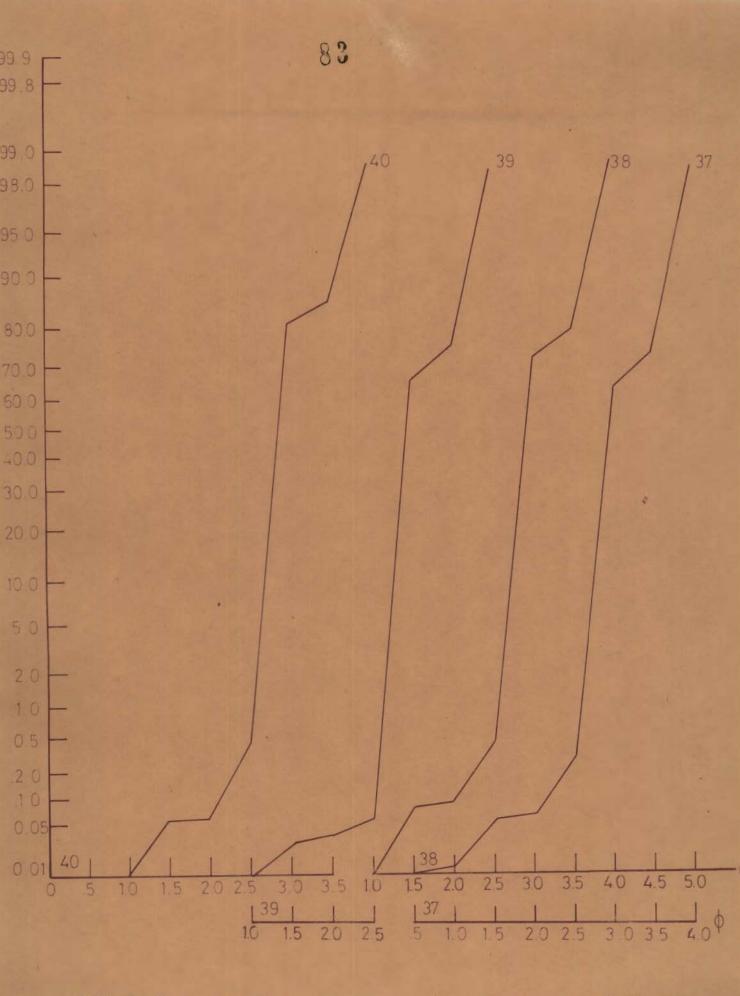


FIG.4.13 _ Cumulative frequency curves for grain size distributions

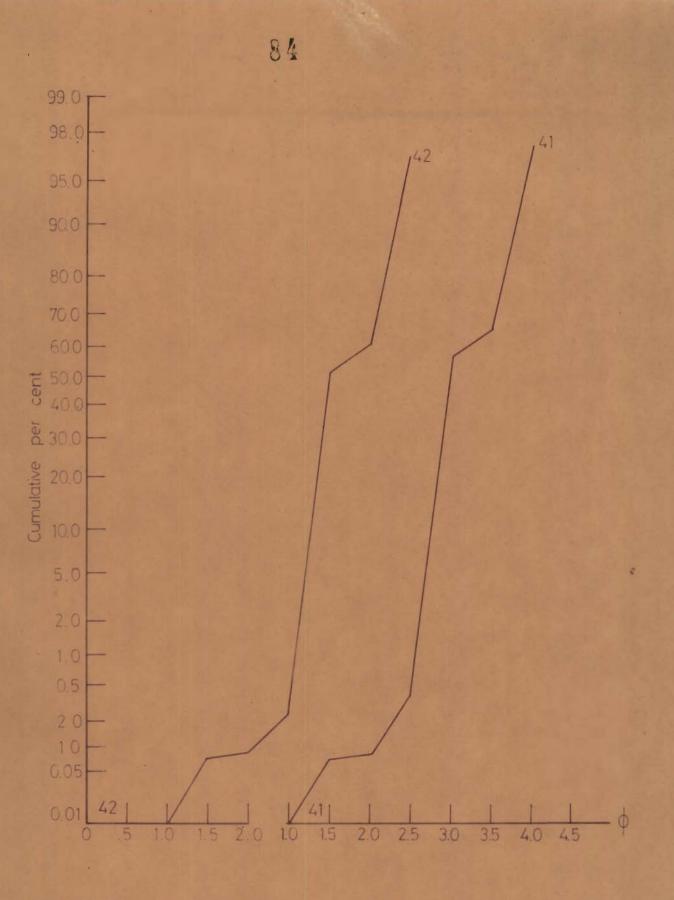


FIG.4.14 _Cumulative frequency curves for grain size distributions.

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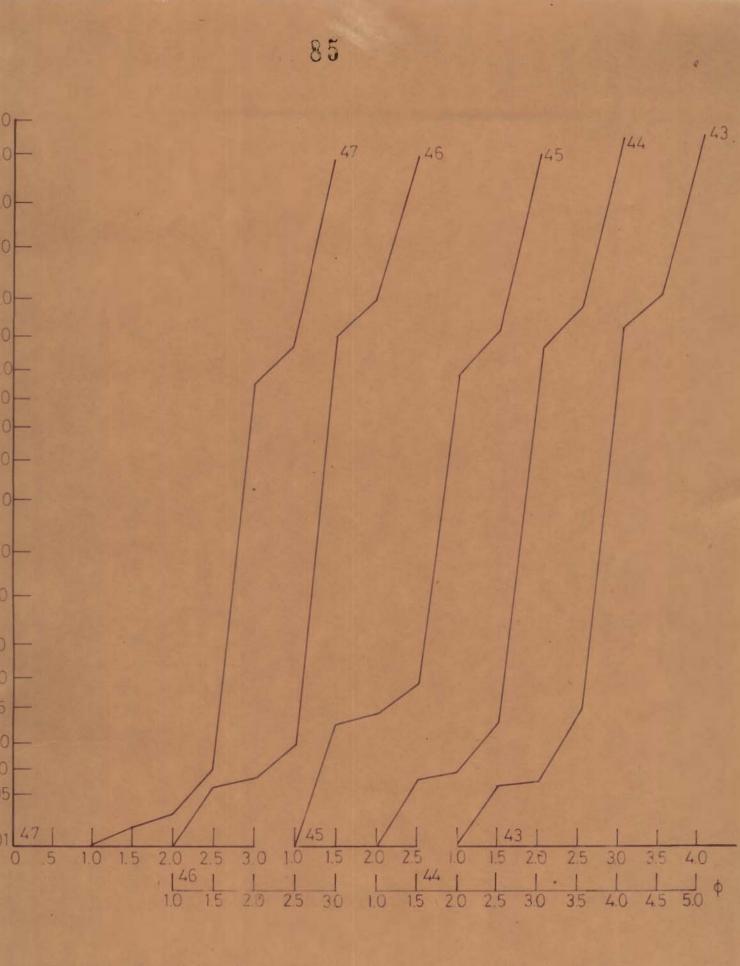
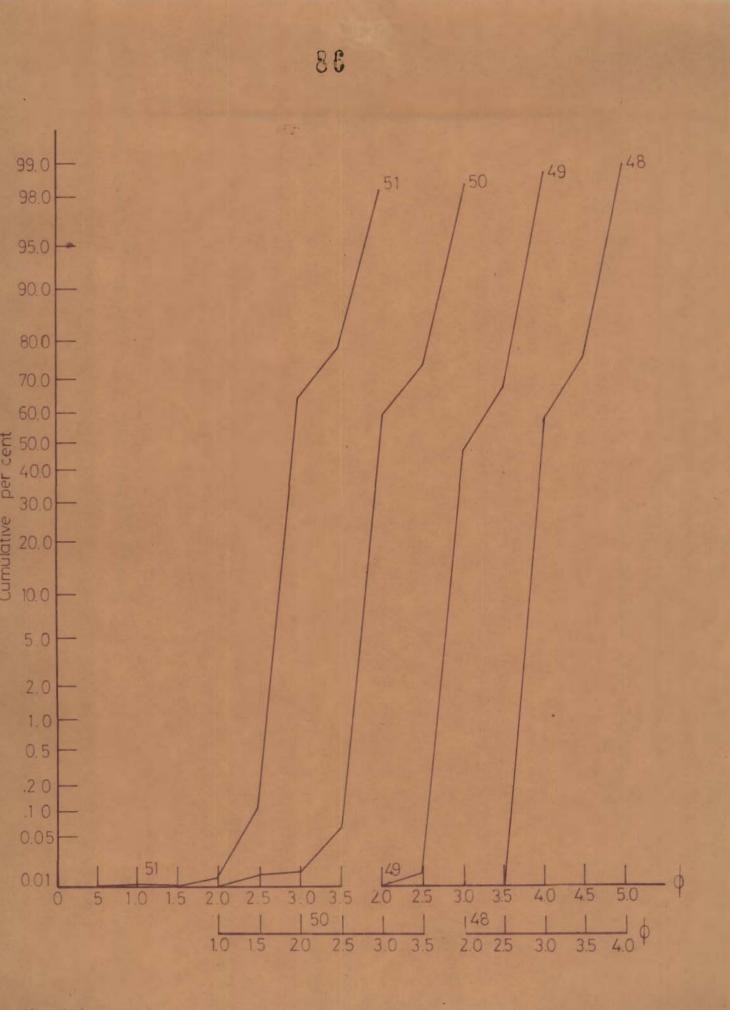


FIG.4.15 _ Cumulative frequency curves for grain size distributions.



4.16 _ Cumulative frequency curves for grain size distributions

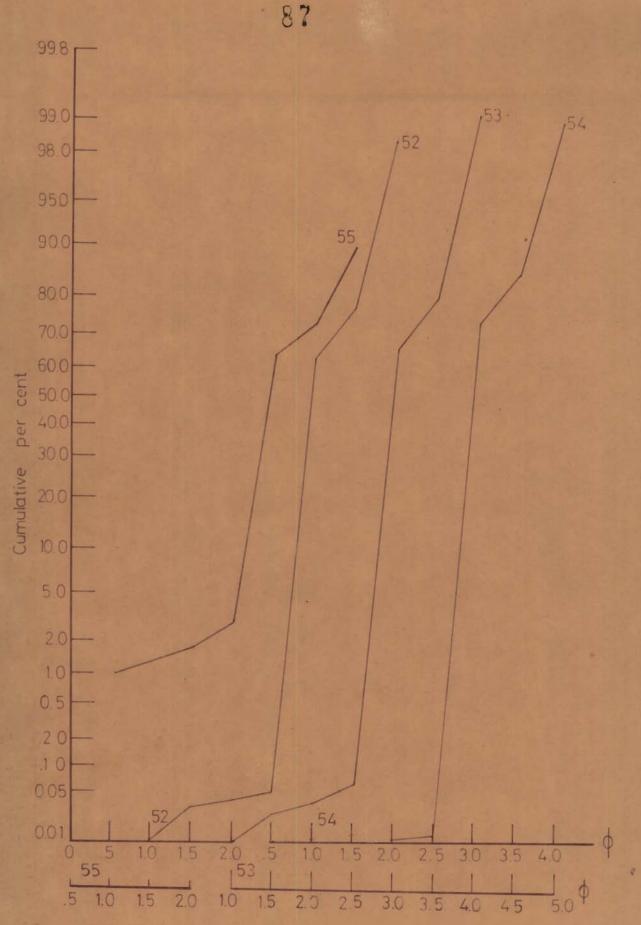
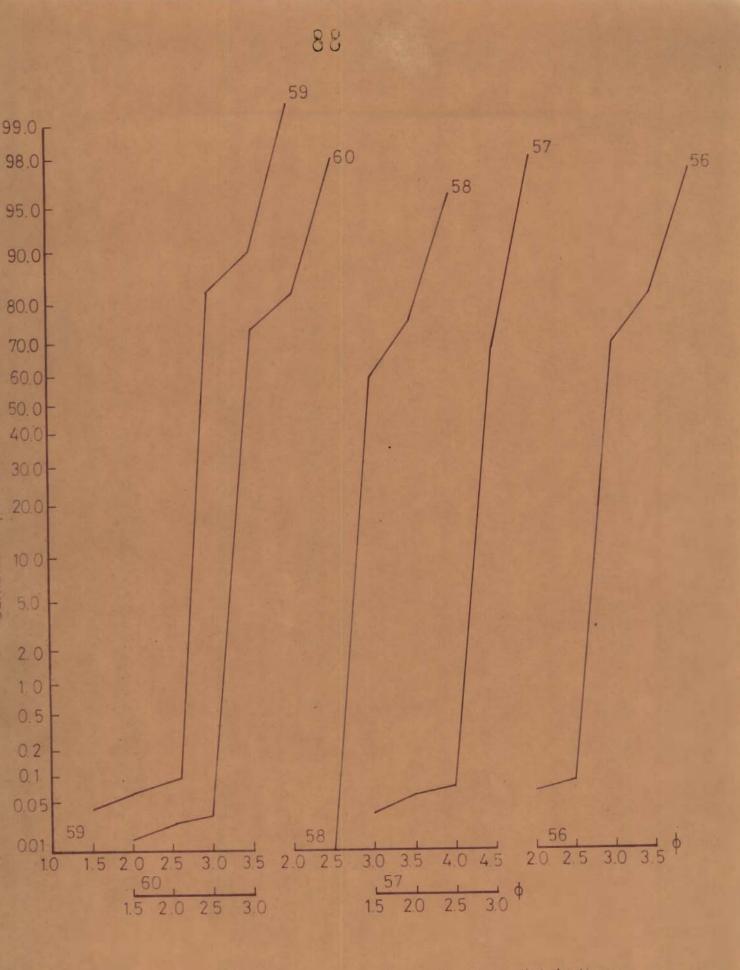
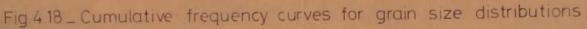


FIG.4.17 _ Cumulative frequency curves for grain size distributions





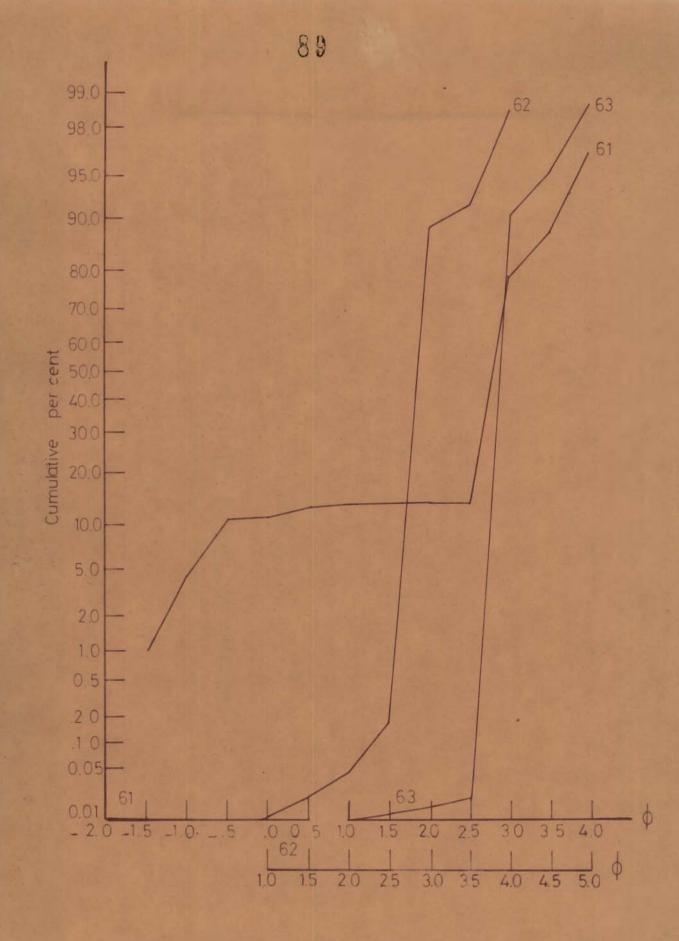


FIG.4.19 _ Cumulative frequency curves for grain size distributions

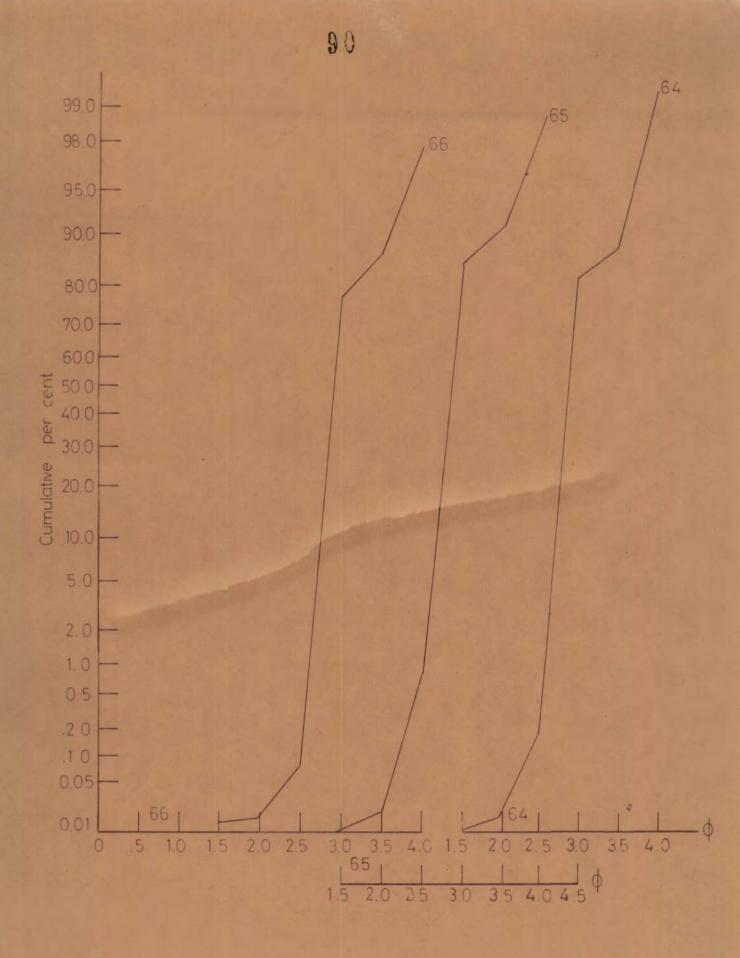


FIG.4.20 _ Cumulative frequency curves for grain size distributions

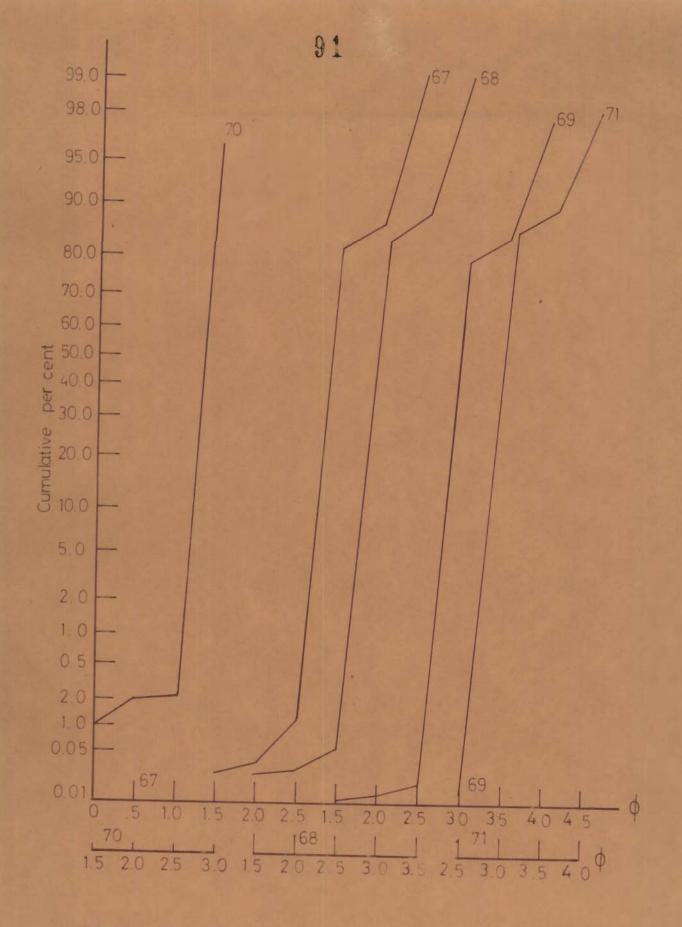


FIG. 4.21 _ Cumulative frequency curves for grain size distributions

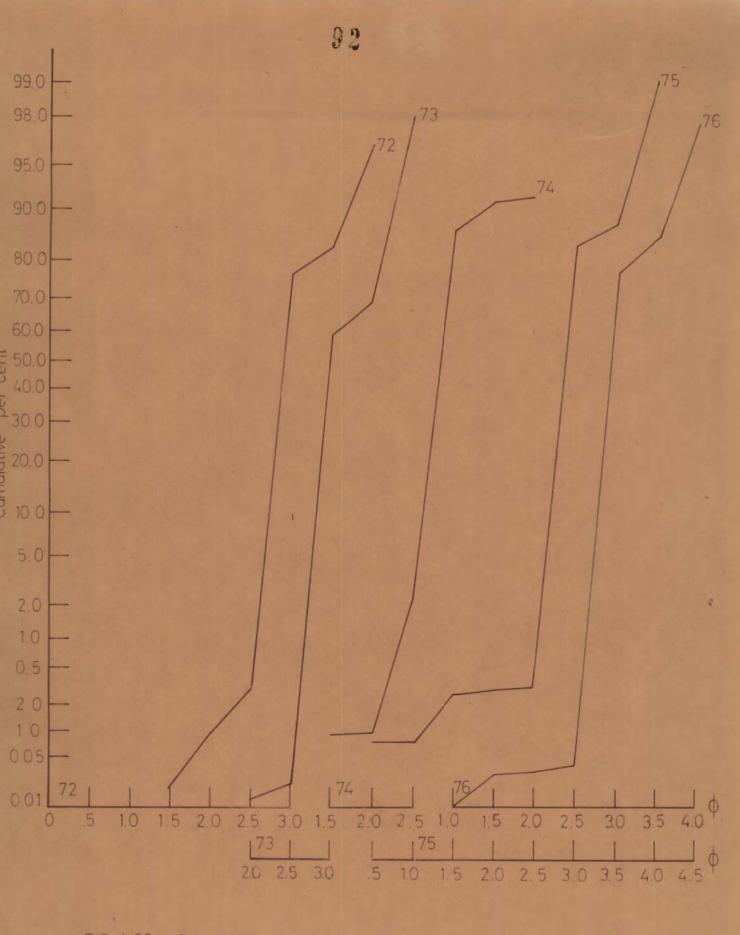


FIG. 4.22 _ Cumulative frequency curves for grain size distributions

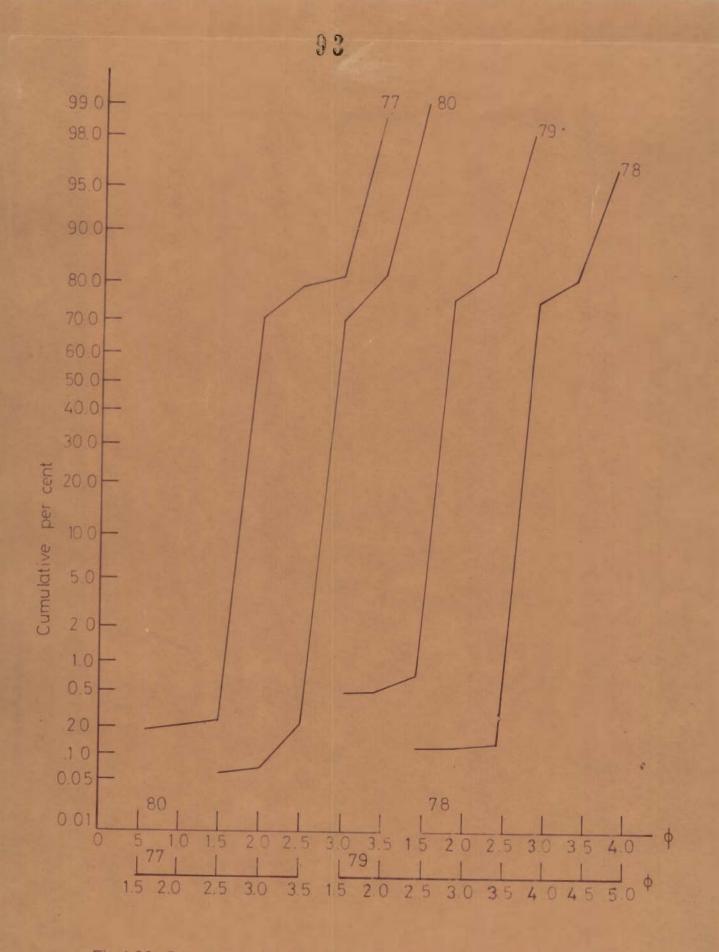


Fig.4.23_Cumulative frequency curves for grain size distributions

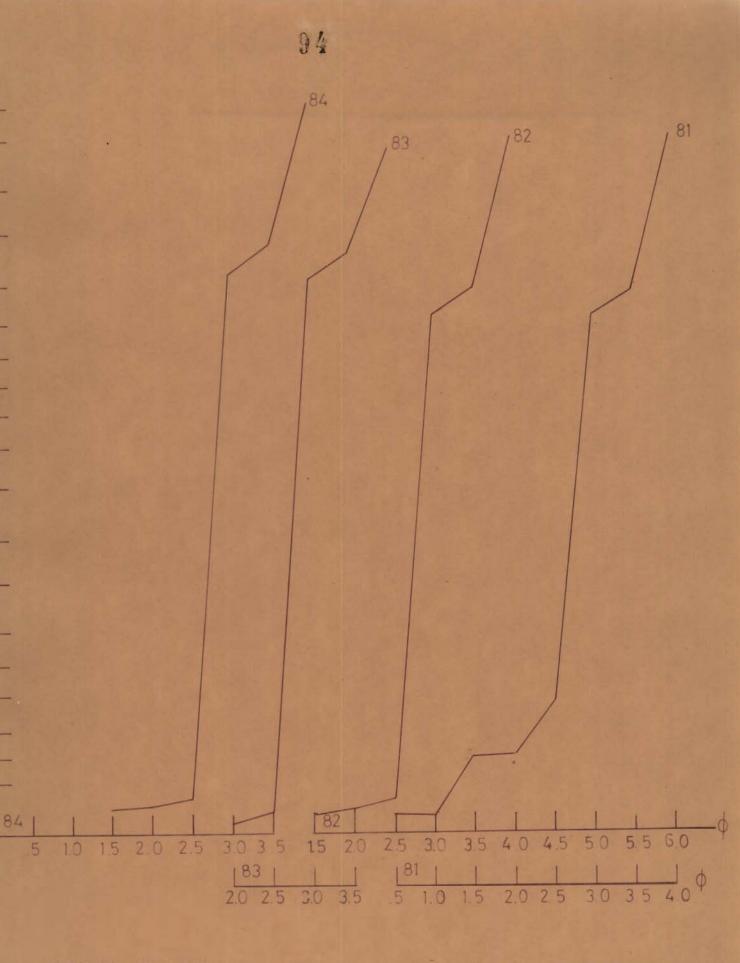


FIG.4.24 _ Cumulative frequency curves for grain size distributions.

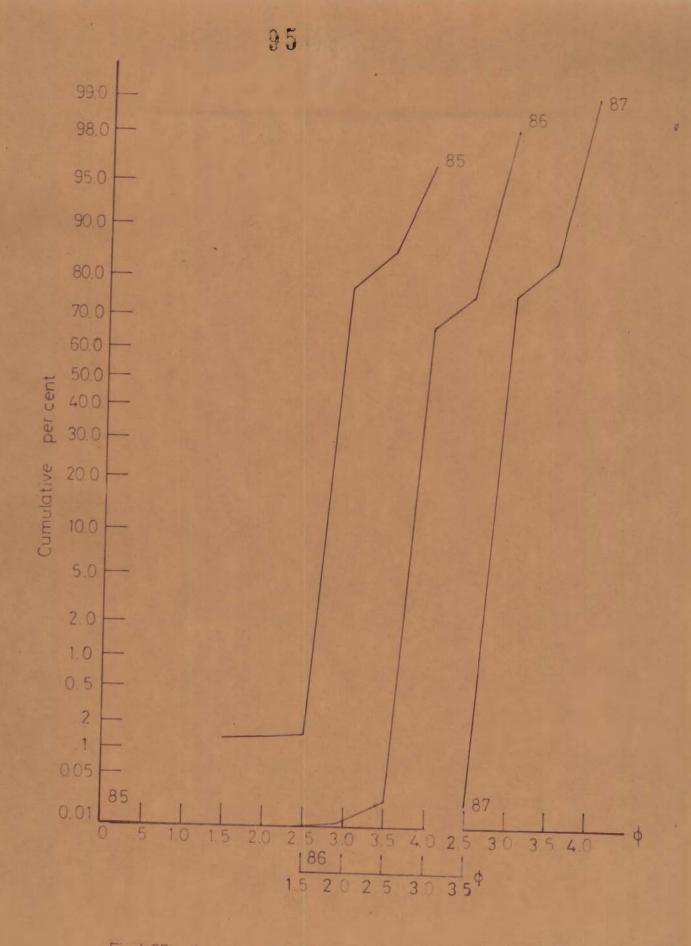


Fig.4.25 Cumulative frequency curves for grain size distribution

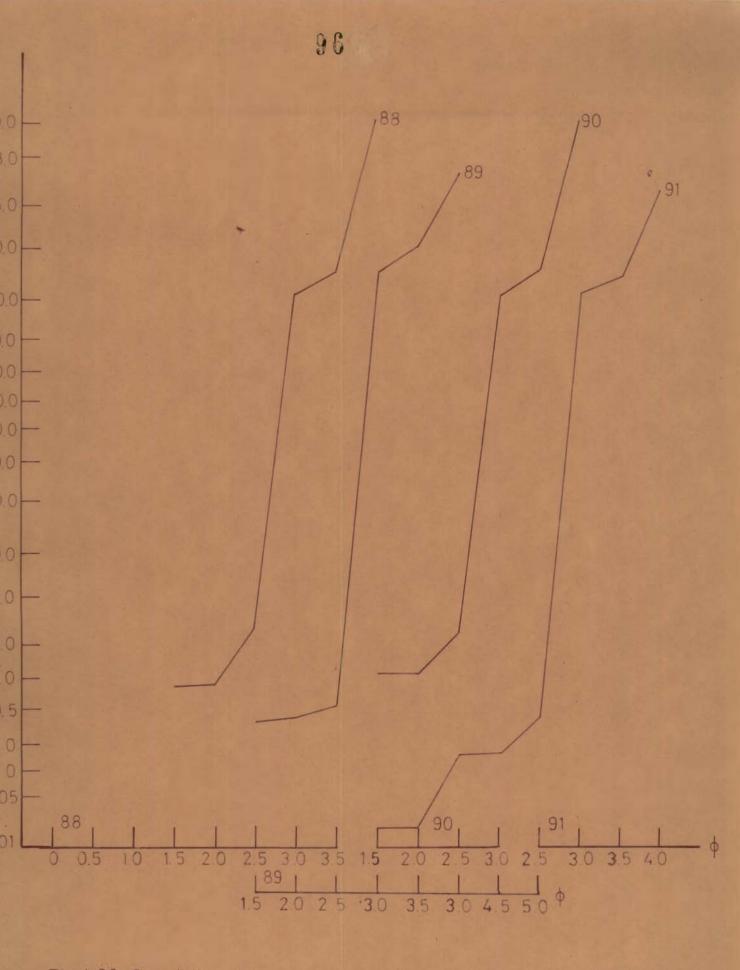


Fig. 4.26_Cumulative frequency curves for grain size distributions

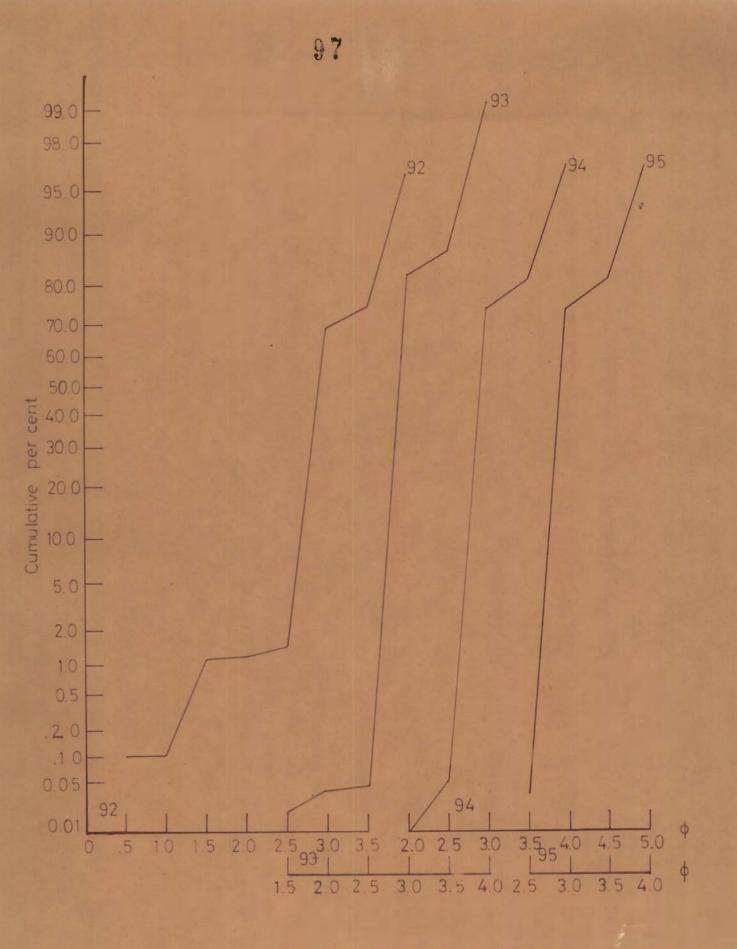


Fig.4.27_Cumulative frequency curves for grain size distributions.

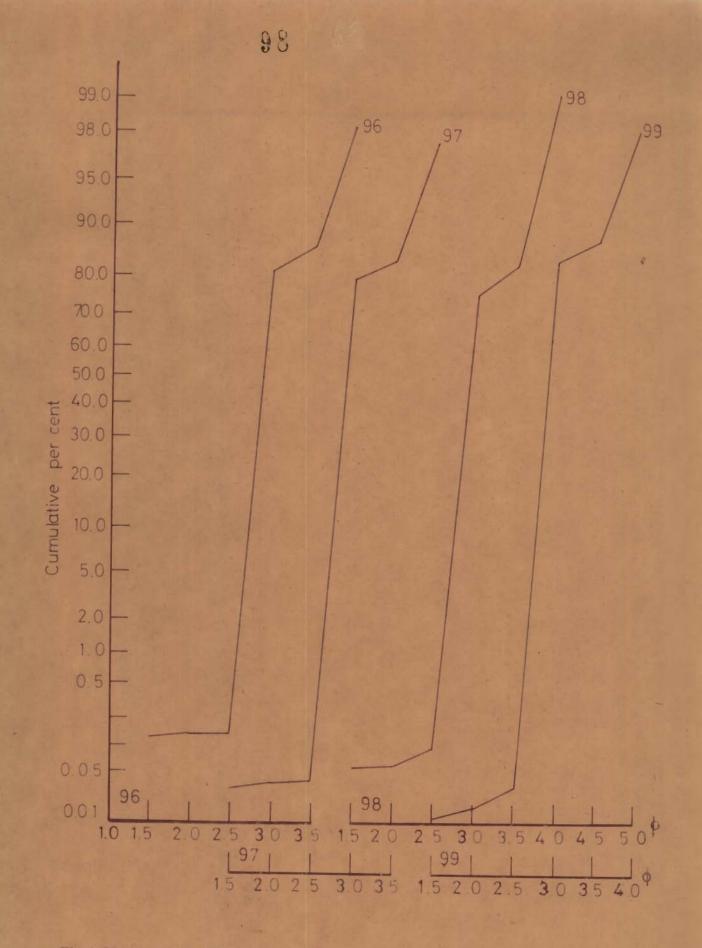


Fig.4.28_ Cumulative frequency curves for grain size distributions

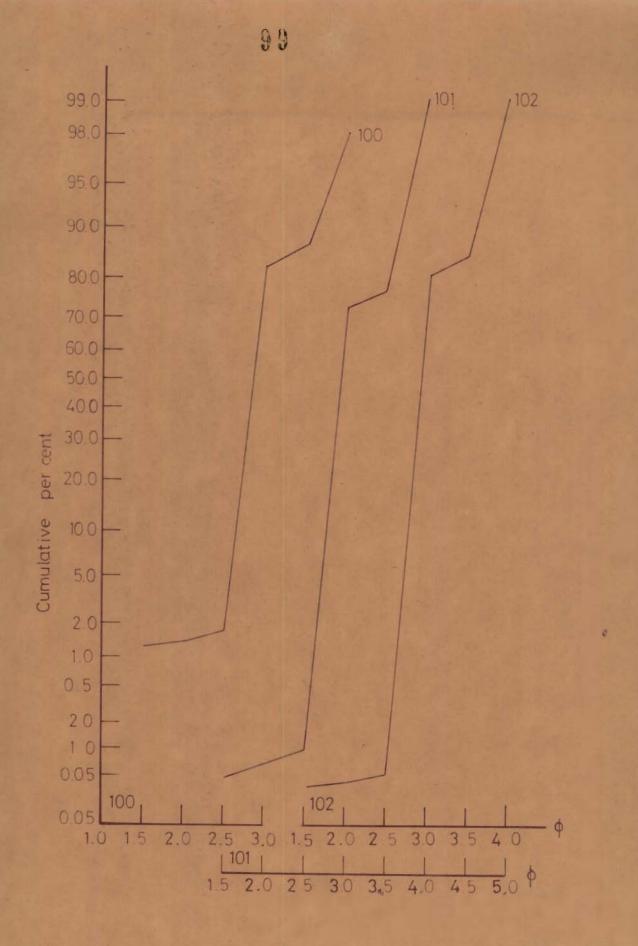


Fig.4.29 _ Cumulative frequency curves for grain size distributions

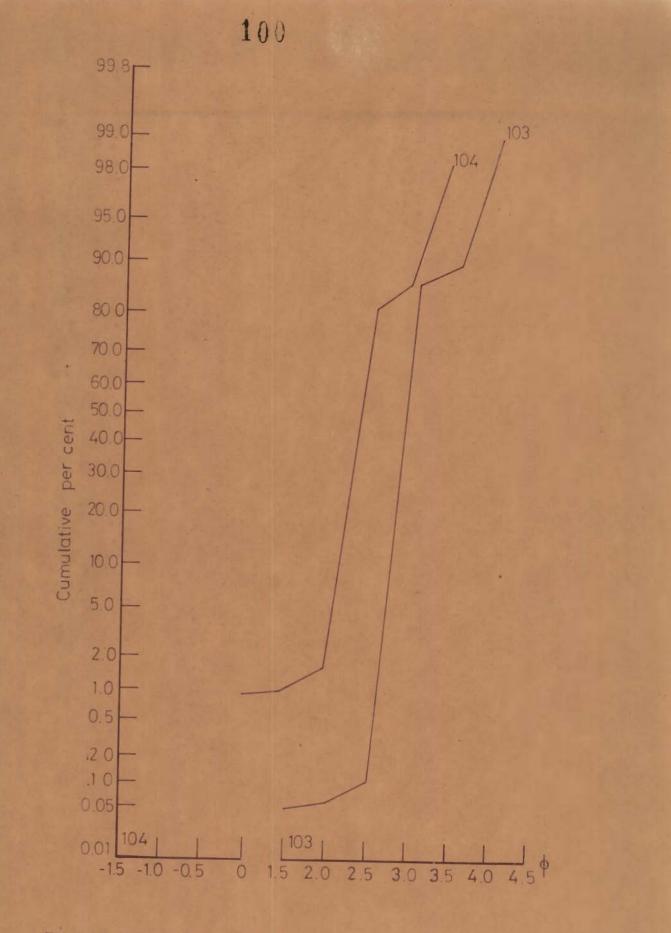


Fig.4.30_Cumulative frequency curves for grain size distributions.

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measures have been suggested by different authors and are listed in Table 4.1 along with their efficiencies (McCammon, 1962) in estimating the different grain size parameters. Calculated values of these measures are given in Appendices IV-VII.

Table 4.1 - Formulae for computing graphical grain size parameters after different workers

| | Efficiency |
|---|------------|
| Mean | per cent |
| Trask (1930) $Mzl = \emptyset 50$ | 64 |
| Otto: (1939), Inman (1952) Mz2 = (Ø 16+Ø 84)/2 | 74 |
| Folk and Ward (1957) $M_2 Mz3 = (\emptyset 16 + \emptyset 50 + \emptyset 84)$ | /3 88 |
| McCammon (1962) $M_2 - Mz4 = (\not p \ 10 + \not p \ 30 + \not p \ 50 + \not p \ 70 + \not p \ 90)/5$ | 93 |
| McCammon (1962) $Mz = (\emptyset 5 + \emptyset 15 + \emptyset 25$ | |
| +Ø 85+Ø 95)/1 Sorting | LO 97 |
| Trum? Krumbein (1934) $(QD\phi) \leftarrow \sigma_1 = (\phi 75 - \phi 25)/1.35$ | 37 |
| Otto (1939), Inman (1952) $\sigma_2 = (\emptyset \ 84 - \emptyset \ 16)/2$ | 54 |
| (Folk and Ward (1957) (σ_3 = (ϕ 84- ϕ 16)/4 | |
| T(0 5)-0 5)/0.5 | 79 |
| Mc Cammon (1962) $\sigma_4 = (\emptyset 85 + \emptyset 95 - \emptyset 5)$ | |
| - Ø 15)/5.4 | 79 |
| McCammon (1962) $\sigma = (\phi 70 + \phi 80 + \phi 90 + \phi)$ | 97 |
| -ø 3-ø 10-ø 20-ø | |
| Tanner 1958 (computer) 9.2 | 87 |

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 Skewness
 (Sk qt)

 Krumbein and Pettijohn
 Skl = [\$\overline\$ 25+\$\overline\$ 75-2 \$\overline\$ 50]/2

 Inman (1952)
 (\$\overline\$ \overline\$ \$\overline\$ \$\o

ront

 Kurtosis

 Krumbein and Pettijohn Kul = $\frac{\emptyset}{2(\emptyset} \frac{75-\emptyset}{90-\emptyset} \frac{25}{10}$

 (1538)
 (K qa)

 Inman (1952)
 (Ba) Ku2 = $(\frac{\emptyset}{95-\emptyset} \frac{95-\emptyset}{5} - (\frac{\emptyset}{984-\emptyset} \frac{84-\emptyset}{16})$

 Folk and Ward (1957)
 (Ka) Ku = $\frac{\emptyset}{2.44(\emptyset} \frac{95-\emptyset}{75-\emptyset} \frac{25}{25}$

4.2.5 Comparison of Graphical Grain Size Parameters

Middleton (1962) suggested that individual grain size parameters from a particular environment can be considered to constitute a homogeneous population. Sahu (1964) also assumed normal distribution for individual grain size parameters in determining discriminatory functions for different environments. Following this line of reasoning, different parameters are considered to constitute samples from normal populations. Histograms depicting distributions of these parameters are shown in Figures 4.31-4.34. Grand means and

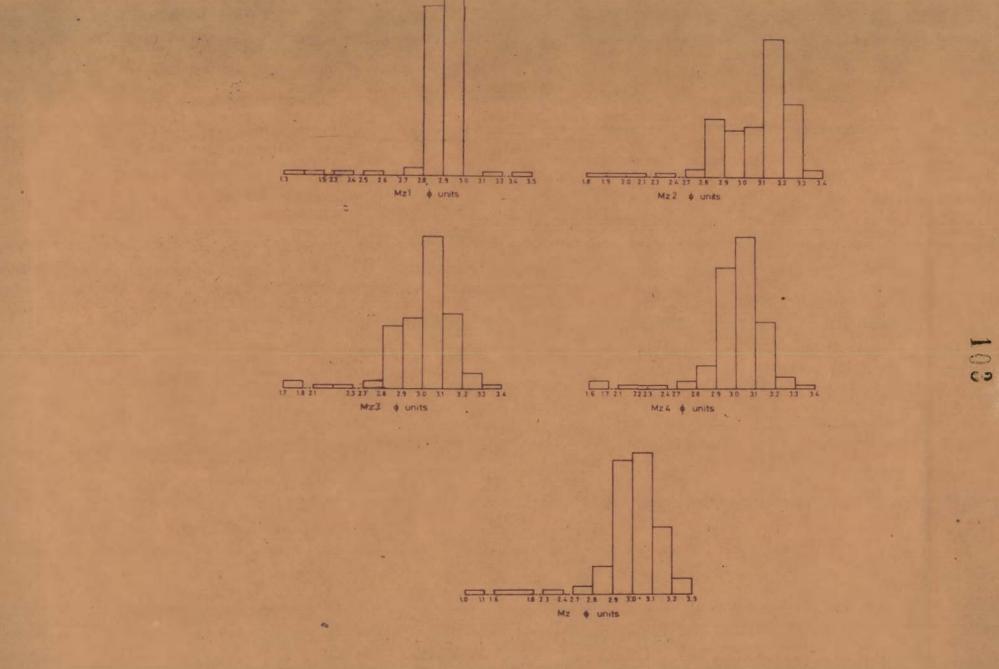


Fig.4.31_Histograms showing distributions of the various measures of mean grain size.

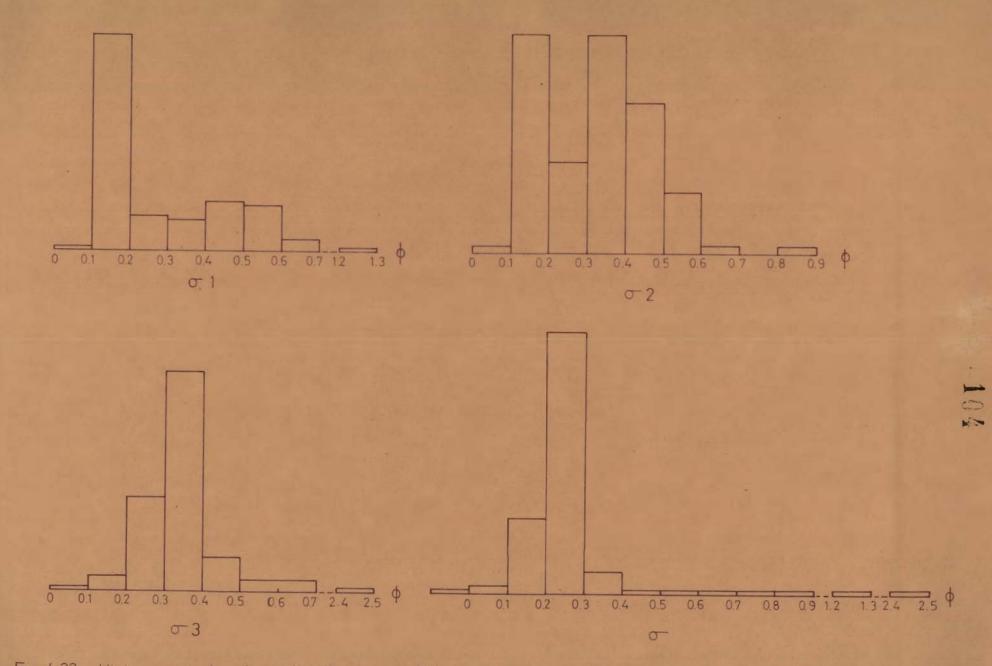


Fig. 4.32_Histograms showing distributions of the various measures of sorting.

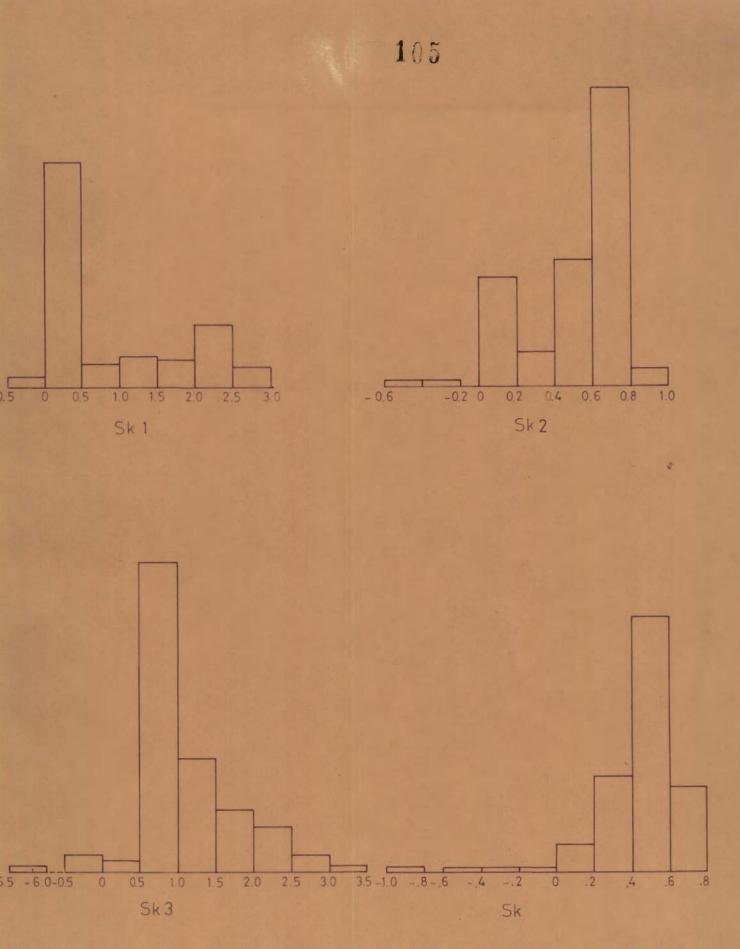
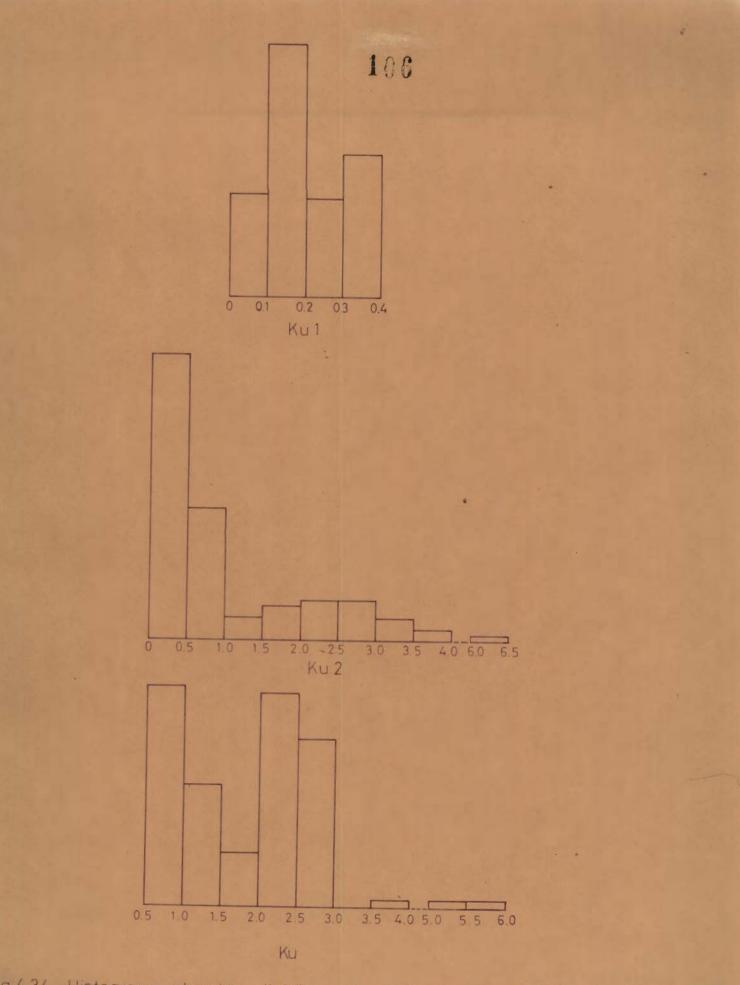


Fig 4.33_Histograms showing distributions of the various measures of skewness.



g.4.34_Histograms showing distributions of the various measures of kurtosis.

standard deviations for the various parameters after different authors and 't' values calculated for different pairs of grain size measures are listed in Tables 4.2-4.5.

A.

| | Mean Standard | | 't' values | | | |
|-----|---------------|-----------|------------|-------|-------|-------|
| | | Deviation | Mzl I | Mz2 | Mz3 | Mz4 |
| Mzl | 2.868ø | 0.330 | | | | |
| Mz2 | 3.046Ø | 0.246 | 1.381 | | | |
| Mz3 | 2.987ø | 0.232 | 0.543 | 0.557 | | |
| Mz4 | 2.974ø | 0.246 | 0.822 | 0.661 | 0.123 | |
| Mz | 2.968Ø | 0.290 | 0.726 | 0.655 | 0.182 | 0.050 |

Table 4.2 — Comparison of graphical measures for near size.

Table 4.3- Comparison of graphical measures for standard deviation

| | Mean | Standard Deviation | ידי סו | values ⁰ 2 | σ3 | σ ₄ |
|---|--|---|----------------------------------|--------------------------|----------------|----------------|
| σ ₂ σ ₂ σ ₃ σ ₄ σ | 0.271ø 0.338ø 0.365ø 0.375ø 0.366ø | 0.184 0.141 0.235 0.268 0.385 | 0.923 1.006 1.022 0.711 | 0.315 0.390 0.218 | 0.090 0.007 | 0.061 |

| | Mean | Standard Deviation | Skl 't | values Sk2 | Sk3 |
|-------------------------|----------------------------------|----------------------------------|--|----------------|-------|
| Skl Sk2 Sk3 Sk | 0.069 0.464 0.998 0.496 | 0.115 0.277 0.997 0.222 | 4.205 ^x 2.956 ^x 5.479 ^x | 1.648 0.288 | 1.569 |

Table 4.4 - Comparison of graphical measures for skewness

x Significant at 5% level of significance.

Table 4.5 — Comparison of graphical measures for kurtosis

| and a second | Mean | Standard Deviation | t' values | |
|--|-------|-----------------------|--|--|
| Kul | 0.192 | 0.099 | the second secon | |
| Ku2 | 1.082 | 1.065 | 2.657 ^x | |
| Ku | 1.800 | 0.865 | 5.897 ^x 1.671 | |

x Significant at 5% level of significance.

't' values bring out that Skl and Kul values differ respectively from other measures of skewness and kurtosis significantly (at 5% level of significance) and they are consistently lower than other measures. However, there are no significant differences between different graphic measures estimating all the four parameters viz. mean size, standard deviation, skewness and kurtosis (at 5% significance level) provided Skl and Kul are not considered. Since formulae for Skl and Kul take into account very limited portions of the distributions, these should not be used for estimating skewness and kurtosis. Though any of the graphic measures other than Skl and Kul could be used, yet the most efficient measures designated as Mz, σ , Sk, and Ku are used in further discussions.

4.2.6 Variation of Grain Size Parameters

This section describes variation in grain size parameters of samples analysed in the present study and compares them with similar studies made elsewhere.

To give an idea of dispersion, a term S-range of the parameter is used in the following pages. S-range is the calculated <u>+</u> one standard deviation of the parameter and not the counted one, as is done by Folk (1971a).

4.2.6.1 Mean Size

All the samples average about 2.97 \emptyset (0.13 mm, fine sand) with S-range from 2.78 to 3.26 \emptyset . Thus, these samples lie within typical dune size range as given by Udden (1858), Alimen (1557), and Chavaillon (1964). However, the Thar desert sands lie on the finer side of the dune range and many samples are even finer than generally described dune range.

Udden (1898) pointed out that dune crest sands tended to evolve towards fine sand size $(2-3\emptyset)$ as this

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was the favoured material for saltation load irrespective of the source from which material was available. The comparative finer nature of the sands of the Thar desert could be due to the lower velocities of the prevailing winds which are able to pick up finer material as saltation load. Also finer dust carried by the wind as suspension load may have got deposited and infiltrated to give overall finer nature to these sediments.

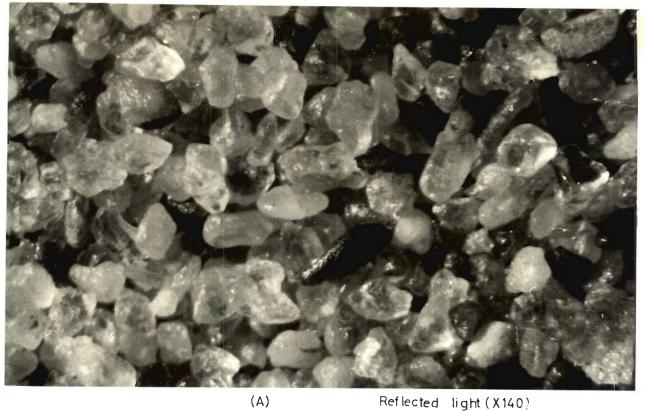
4.2.6.2 Sorting

All samples give an overall mean standard deviation of 0.37Ø and S-range of 0.00 to 0.76Ø, and are classified as well to moderately well sorted. Thus, it is obvious that inland desert dunes are more poorly sorted than the average beach dunes. However, the range of standard deviation is approximately the same, or slightly smaller; than that for beach dunes (Friedman, 1961; Moiola and Weiser, 1968).

A study of the photomicrographs and cumulative frequency curves of typical samples of the area (Figs. 4.35-4.38) shows that sorting seems to be a function of the ratios in which two or more sub-populations are mixed.

4.2.6.3 Skewness

All sand samples except three are positively skewed. The mean value is +0.50 and S-range 0.28 to 0.72. Common skewness range is from 0.05 to 0.7. Fig. 4:35_Photomicrograph (A) and cumulative frequency curve (B) for sample 63. The sample is from a sand pile. It has a mean size of 2:80 ϕ and shows good sorting (0=0.170 ϕ).



Reflected light (X140)

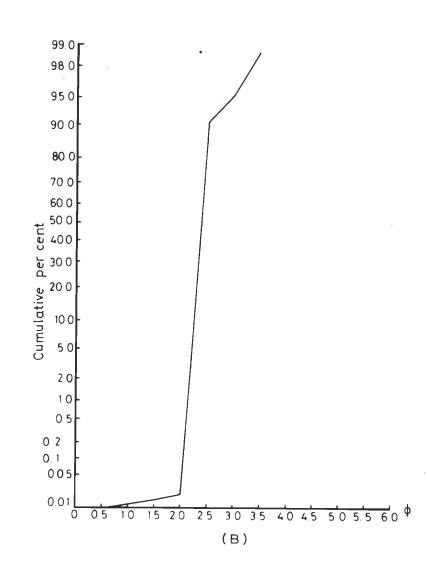


Fig. 4:36_Photomicrograph (A) and cumulative frequency curves (B) of sample 103. The sample is from a barchan having a mean size of $3.00 \, \text{Ø}$. It shows good sorting ($\mathcal{O}=0.25 \, \text{Ø}$).



(A)

Reflected light (X140)

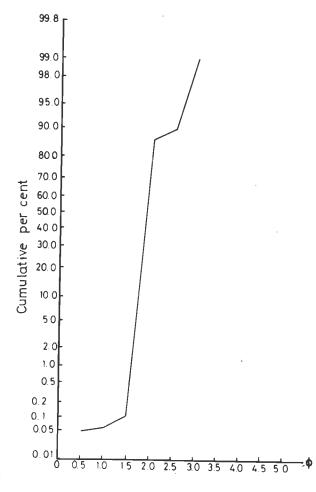
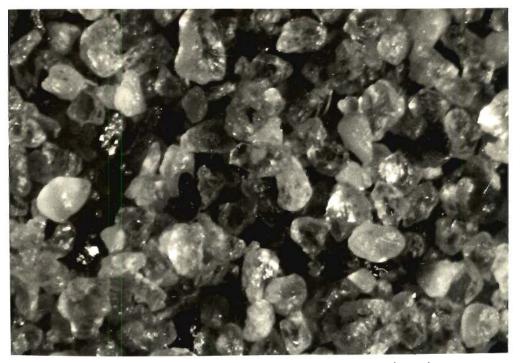


Fig.4.37_Photomicrograph(A) and cumulative frequency curve(B) of sample 77. The sample is from windward side of a barchan. It has a mean size of 3.12 φ and shows moderate sorting (σ=0.45 φ).



(A)

Reflected light (X140)

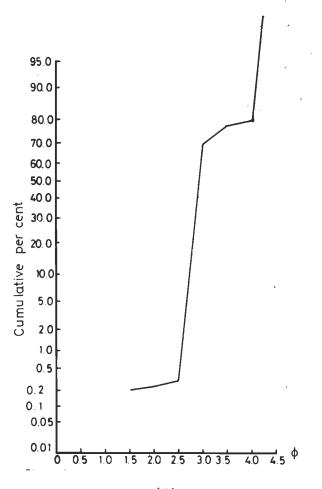
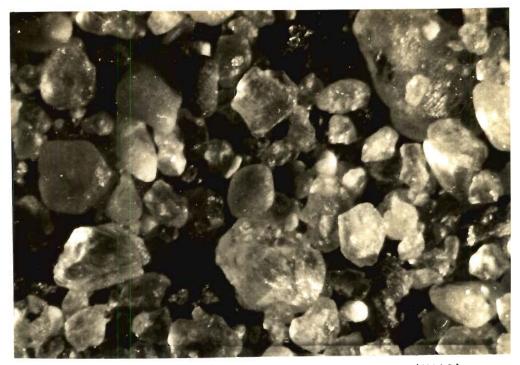
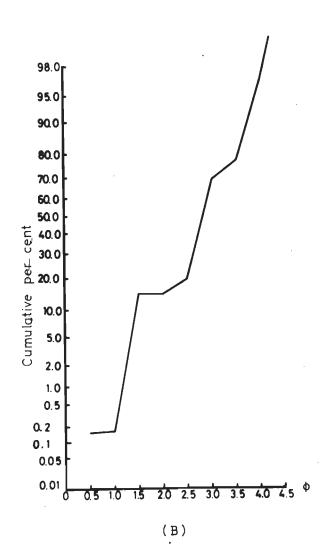


Fig.4.38_Photomicrograph (A) and cumulative frequency curve (B) of sample 2 collected from the trough of a ripple. It has a mean size of $2.78 \, \phi$ and shows poor sorting ($O = 0.71 \, \phi$).



(A)

Reflected light (X140)



The strong positive skewness of desert dunes is probably produced by the abundance of fines derived from alluvial source. Also it has been emphasized by Friedman (1967) and Folk (1971a) that skewness is a function of the depositing current. In the deposits, where fluid remains in contact with the bed, for example beach sands, the sediments tend to be symmetrical or even negatively skewed. But in those deposits where the current leaves the bed such as leeside of dunes in streams or deserts, the sediments tend to be positively skewed since they receive fines from suspension which get buried by the advancing avalanche face.

Moiola and Weiser (1968) found that inland dunes had slight negative to positive skewness (-0.3 to +0.35) whereas beach dunes were near symmetrical. Differences of desert sands from beach dune sands can be explained by the fact that the latter are derived from beach sources which are deficient in fine material, a fact consequently reflected in their grain size distribution. On the other hand, inland dunes are usually derived from alluvial sediments which have abundant fine material in the form of levee, flood plain and lake deposits.

4.2.6.4 Kurtosis

The kurtosis values range from 0 to 3.6. There are two groups of samples. One group has values from 1.7 to 2.45 i.e. of very leptokurtic nature suggesting the presence of

coarse and fine tails. The other group has values from 0.0 to 0.8 forming platy.kurtic distributions. These reflect probably bimodal distributions with two equal and widely separated modes. Usually sand piles are platykurtic and dunes are leptokurtic, though there is a fair overlap of

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In comparison to the present studies, sands of seifs of Australian Simpson desert were mesokurtic with an average kurtosis of 1.04 (Folk, 1971a). Skocek and Saadallah (1972) found Iraqian desert sands to have kurtosis from 0.58 to 1.62 with a maximum concentration of values between 0.5 to 1.1. Kurtosis values of inland dunes of Moiola and Weiser (1968) were uniformly distributed between 0.8 and 1.45 whereas their coastal dunes had much smaller range i.e. from 0.9 to 1.25.

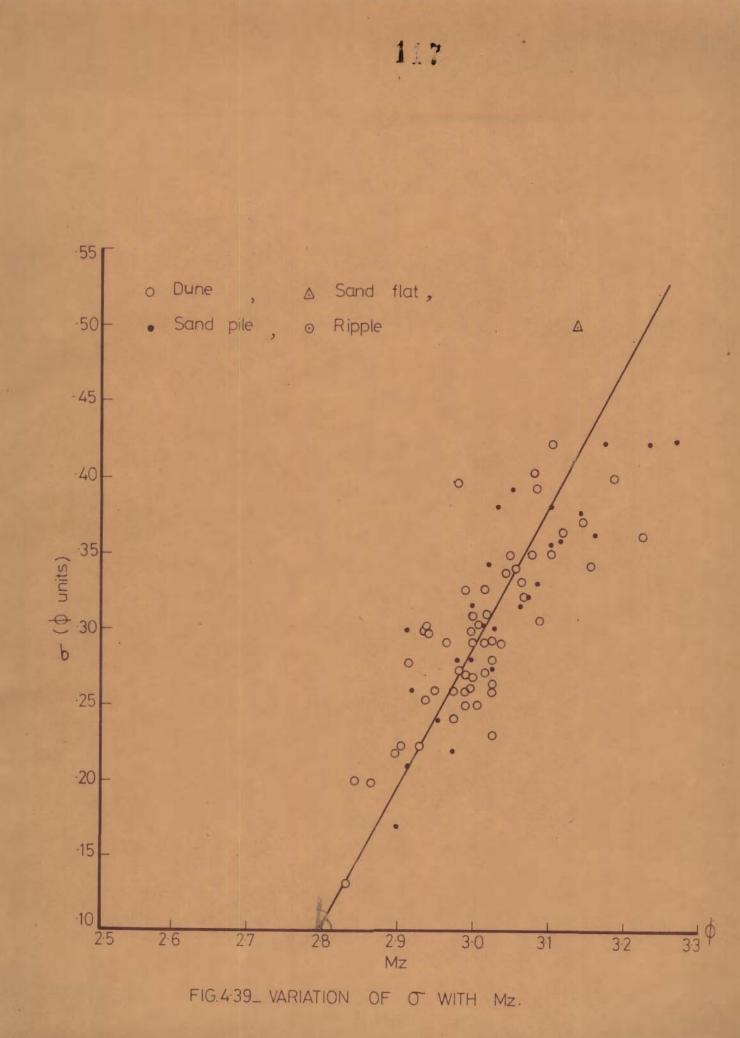
4.2.7 Parametric Interrelationships

kurtosis values of the two bedforms.

Processes leading to variation of grain size statistical parameters can be best analysed by studying their interrelationships. For this purpose, five scatter plots between the four parameters have been prepared (Figs. 4.39-4.43) and discussed below.

4.2.7.1 Mean Size Versus Sorting

The plot of mean size versus sorting (Fig.4.39) shows a strong correlation between the two parameters. With the decrease of grain size, sorting gets worse. Points lie around



a line that makes an angle of about 45° with the mean size axis suggesting that grain size distributions are mixtures of two populations in different proportions (Folk, 1971a).

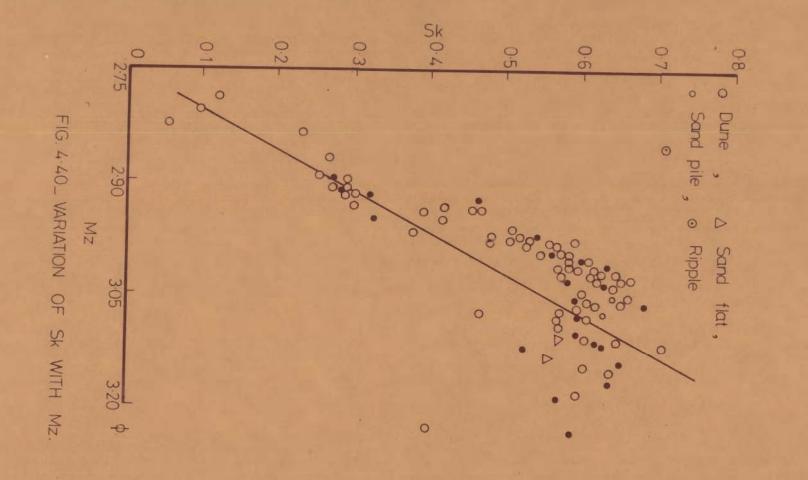
Folk (1971a) found that there is no significant relationship between the mean size and sorting in seif sands of Simpson desert. A similar sorting versus mean size trend has been found for acolian sandstones in Iraq by Philip et al.(1968) and acolian sands by Skocek and Saadallah (1972, Fig.5).

Folk and Ward (1957) found a sinusoidal trend in fluvial sediments in plots of mean size versus sorting and concluded that sands were mixtures of three populations with mean sizes in pebbles, fine sand and clay fractions. In the mean size range observed in the present investigation, Folk and Ward (1957) did find a similar relationship between mean size versus sorting.

4.2.7.2 Mean Size Versus Skewness

Covariate plot between mean size and skewness (Fig.4.40) brings out clearly a distinct overall trend in the plotted samples i.e. with a decrease in grain size the samples become more positively skewed thereby suggesting that samples are simply mixtures of two populations. With the addition of finer tail, samples become positively skewed as proposed earlier.

Folk (1971a) found that finest samples were negatively



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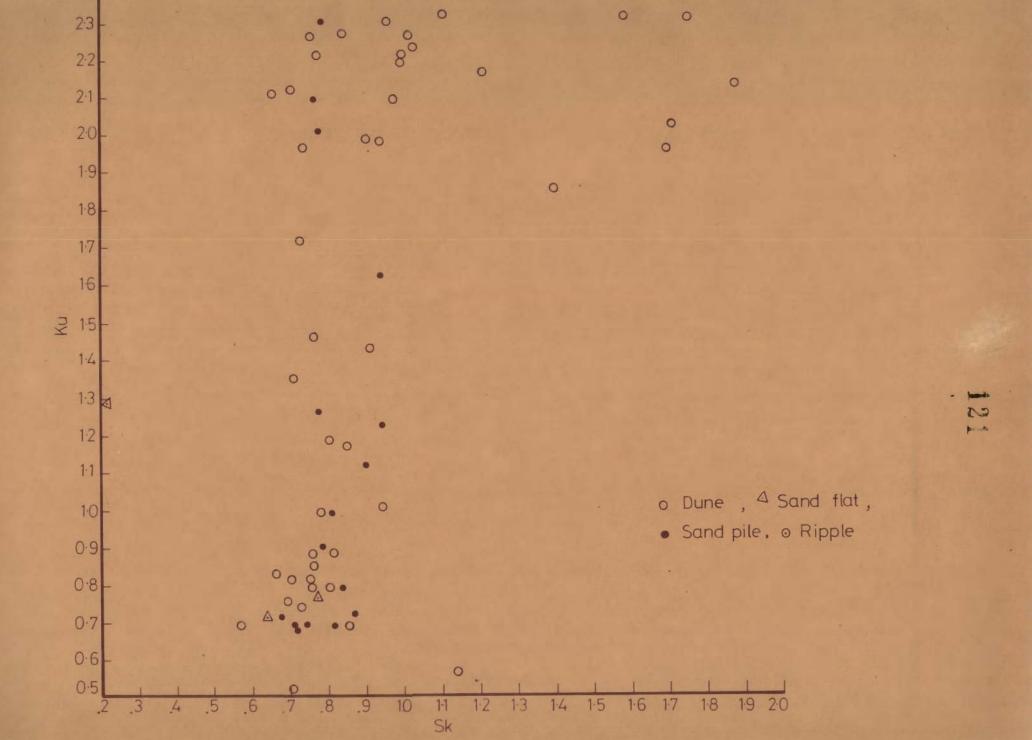
skewed $(Sk \simeq -0.15 \text{ at } Mz = 3.1 \text{ 0})$ and coarsest being most positively skewed (about +0.30 at Mz = 2.4 0). Samples with mean size of about 2.90 have skewness close to zero. Thus, there are two major differences between the two studies. General trend of increase of skewness value with increase in grain size in Folk's (op.cit.) samples is opposite to that observed in the present investigation. Also, within the observed mean size range of most of the samples (2.60 to 3.20), we have commonly positive skewness rather than negative or near symmetrical distribution as observed by Folk (1971c).

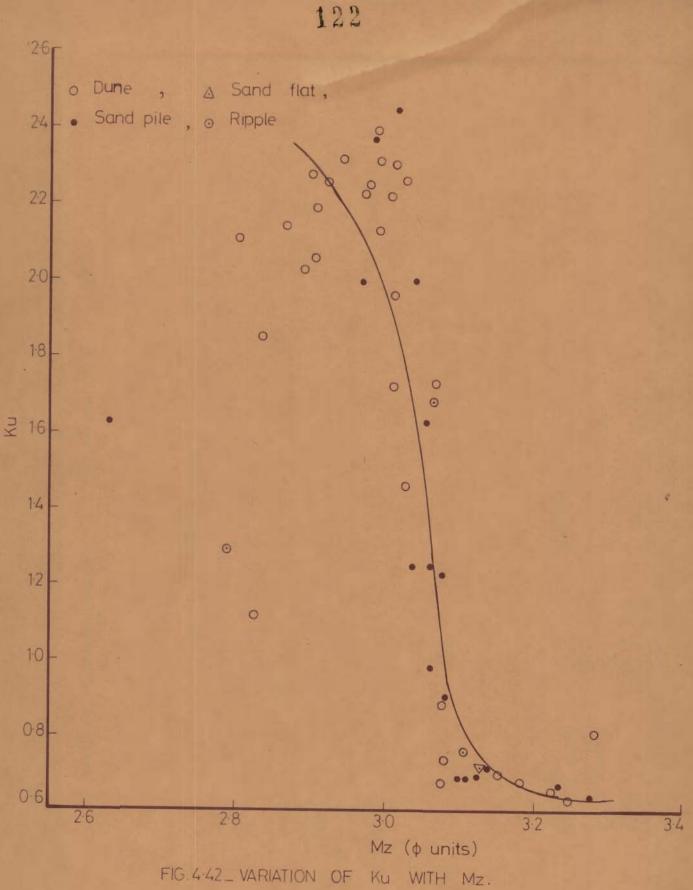
4.2.7.3 Skewness Versus Kurtosis

Evidently there is no trend in the scatter diagram of skewness versus kurtosis (Fig.4.41), but for the fact that for skewness values between 0.5 and 1.2, kurtosis values show a very wide range i.e. from 0.5 to 2.5 and for skewness values larger than 1.2, kurtosis values have a small range of 1.8 to 2.5.

4.2.7.4 Mean Size Versus Kurtosis

There is a distinct relationship between kurtosis and mean size values (Fig.4.42). Kurtosis values tend to decrease with decrease in grain size. Samples with mean sizes, between 3.00 and 3.050, are mesokurtic. Grain size distributions with mean size coarser than 3.00, tend to be more leptokurtic with increase in mean size, though there is





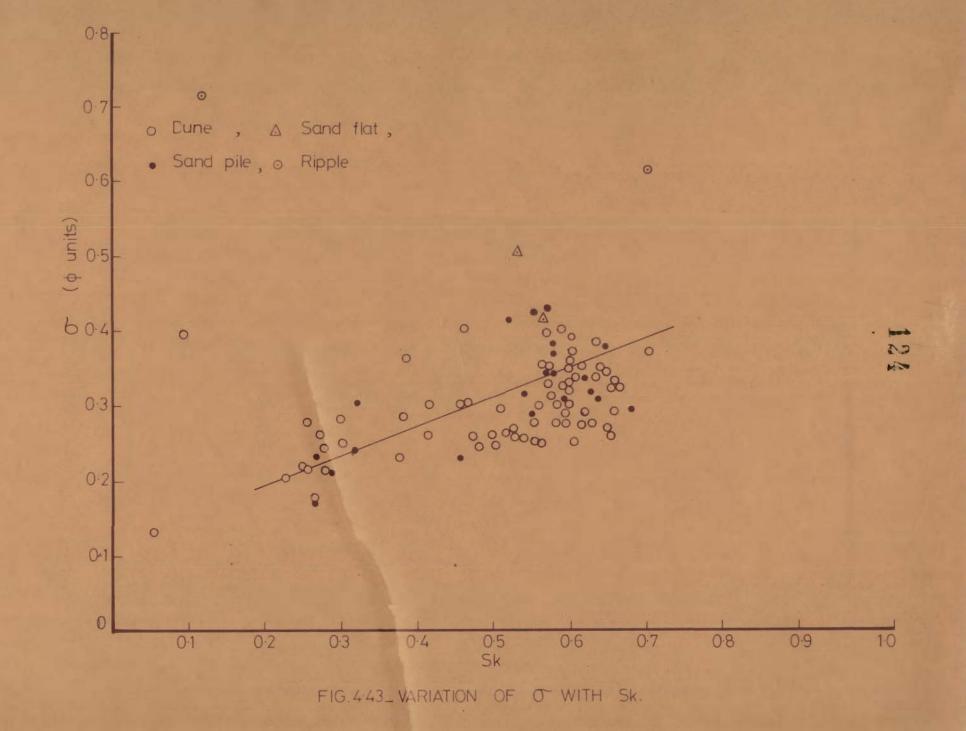
a wide scatter of points around the main trend. Samples with mean size finer than $3.05\emptyset$ tend to become distinctly more platykurtic with decrease in mean size.

4.2.7.5 Sorting Versus Skewness

A definite relationship between standard deviation and skewness in Figure 4.43 is probably a reflection of the fact that both these variables are strongly correlated with mean grain size and values of these parameters increase with decrease in mean grain size.

4.2.8 Variation of Grain Size in Different Bedforms and Sand Flats

Summary statistics i.e. mean and standard deviation of the grain size parameters for the different bedforms and sand flats are listed in Table 4.6. Bar diagrams showing distributions of grain size parameters in relation to bedforms and sand flats are shown in Figures 4.44 and 4.45. Most of the samples are from sand piles and dunes. Number of samples from sand flats and ripples are limited (only 7) for comparison purposes. Comparison of the average values of grain size parameters for different bedforms and sand flats, in conjunction with analysis of their distributions in bar diagrams (Figr.4.44,4.45), brings out some, interesting results. Ripples are the coarsest grained, worst sorted and have near symmetrical distribution. Sand piles tend to have more often finer size than dunes (Fig.4.44), though the average



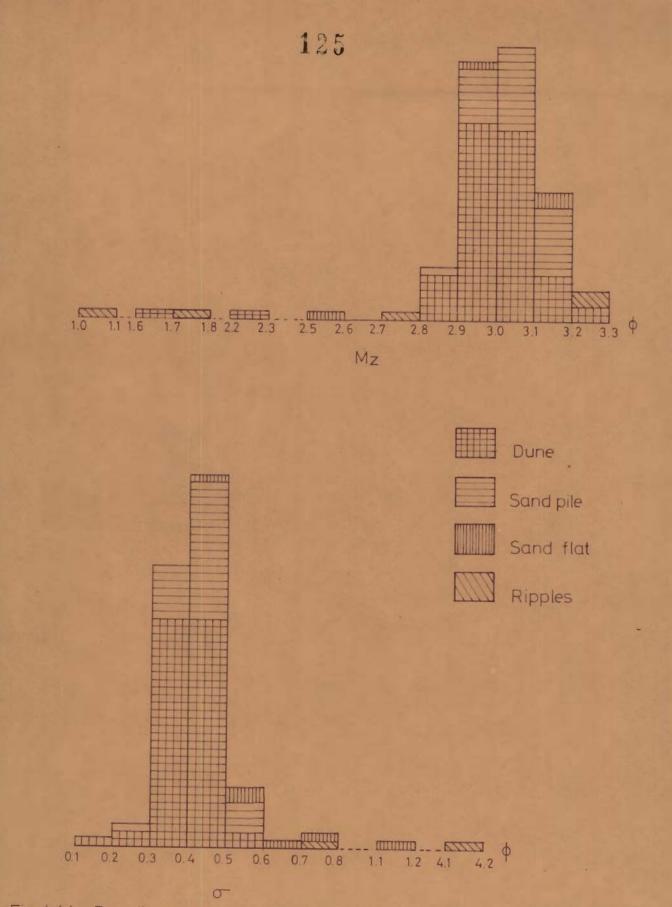


Fig. 4.44 _ Bar diagrams showing distributions of mean size Mz and standard deviation of in different bedforms and sand flats.

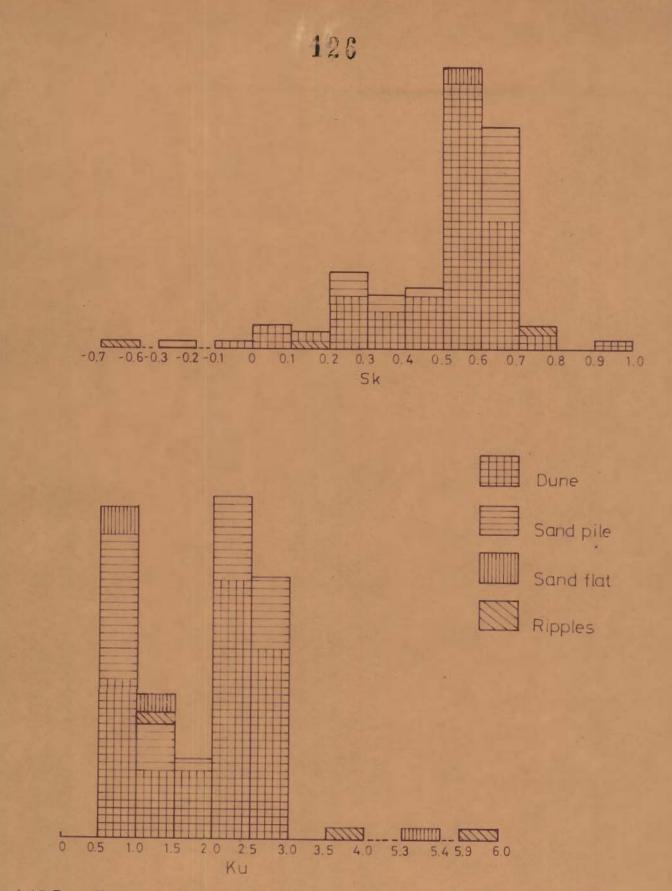


Fig.4.45.Bar diagrams showing distributions of skewness Sk and kurtosis Ku in different bedforms and sand flats. mean size of sand piles is only slightly finer than that of dunes. Also sand piles tend to have larger standard deviation and skewness values than dunes. Kurtosis values for sand piles are distinctly smaller than those for dunes, though these are leptokurtic in nature for both the bedforms.

| No | Sand flats | | Ripples | | Bedforms Sand Piles | | Dunes | |
|-----------------------------|------------|-------|---------|-------|------------------------|-------|--------|-------|
| No. of obser- vations 4 | | | | 31 | | | 66 | |
| Grain size parameter | Mean | s.d. | Mean | s.d. | Mean | s.d. | Mean | s.đ. |
| Mean size Mz | 2.9450 | 0.255 | 1.871ø | 0.874 | 3.0600 | 0.096 | 2.977ø | 0.203 |
| Standard Deviation σ | 0.292ø | 0.813 | 0.4950 | 0.400 | 0.331ø | 0.065 | 0.2550 | 0.274 |
| Skewness Sk | 0.316 | 0.734 | 0.008 | 0.761 | 0.521 | 0.187 | 0.515 | 0.174 |
| Kurtosis Ku | 2.026 | 2.209 | 3.591 | 2.315 | 1.528 | 0.815 | 1.907 | 0.735 |

Table 4.6 - Variation of grain size parameters in the various bedforms and sand flats

s.d.- Standard deviation.

4.2.9 Variation of Grain Size Parameters within Barchan Dunes

Variation of grain size within barchan dunes has been studied by collecting six or seven samples from each of four representative dunes at Sam and Dhanana. In Figures 4.46-4.49, the various grain size parameters have been plotted against the normalised heights of dunes taking the maximum heights of dunes as units. With the increase in height, there is an increase in mean grain size (Fig.4.46). Also sorting improves

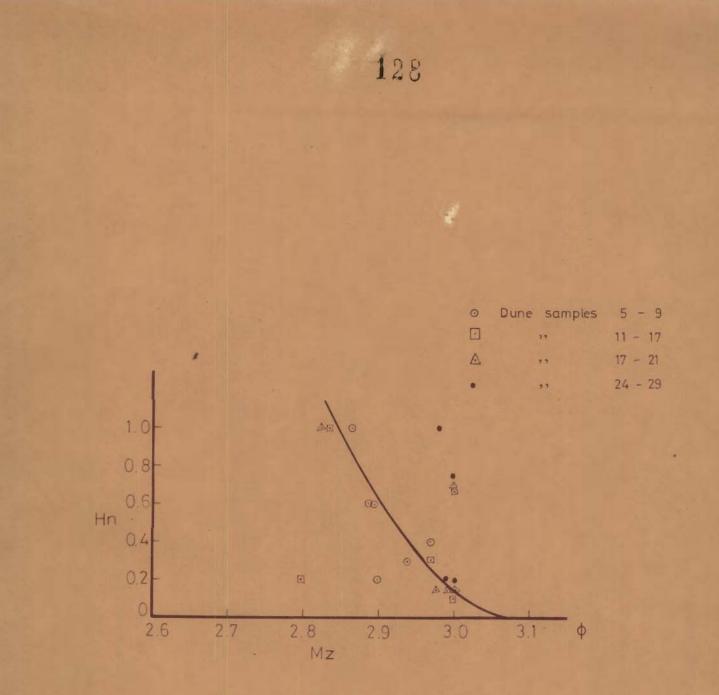


Fig. 4.46_Variation of mean size with normalised height in barchans.

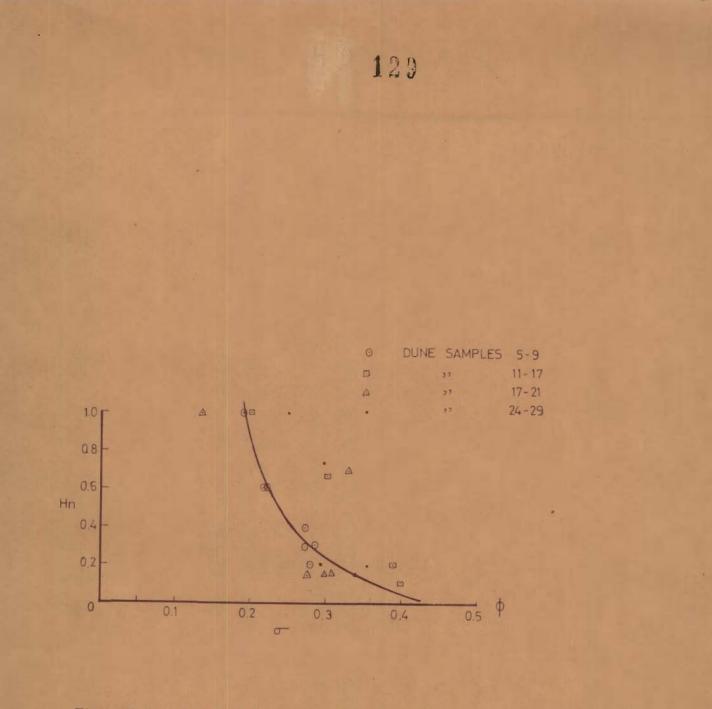


Fig.4.47_Variation of standard deviation with normalised height in barchans.

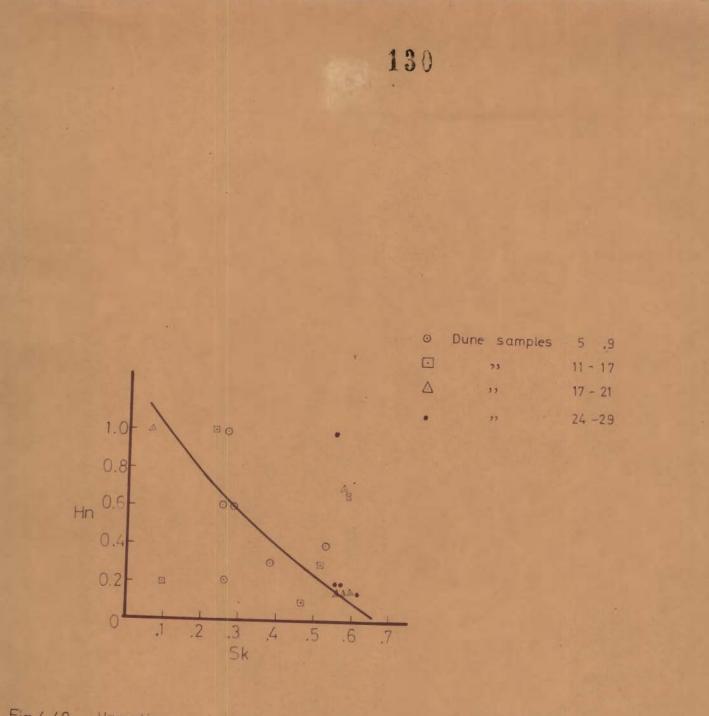


Fig.4.48__ Variation of skewness with normalised height in barchans.

\$

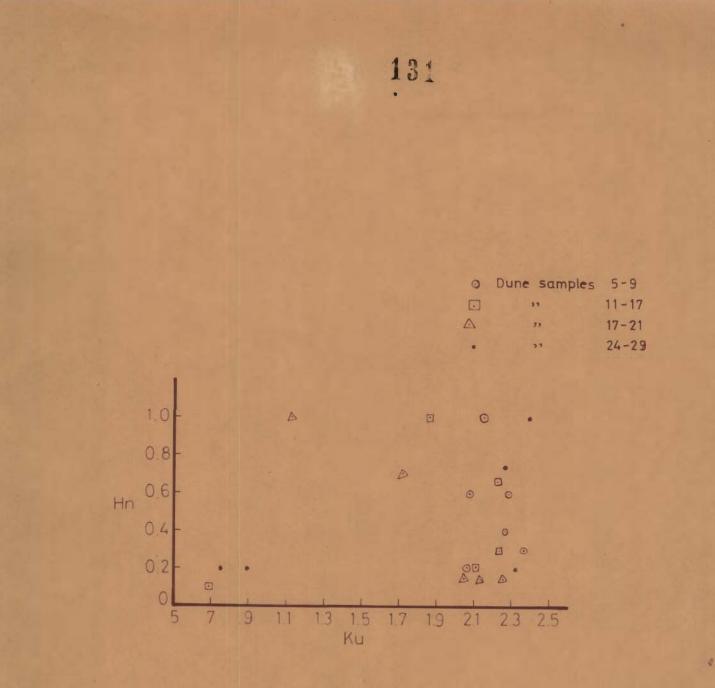


Fig.4.49 Variation of kurtosis with normalised height in barchans.

with height (Fig.4.47). Sediments are more positively skewed at the foot of the dunes and they get progressively less skewed as one moves towards the crest where they become almost symmetrical (Fig.4.48). Sands show no simple linear relationship between kurtosis and the height of dune (Fig.4.49). Also it has not been possible to detect any significant difference between samples from windward and leeward sides of dunes.

Dunes with crests coarser than the substrata have been described by Alimen (1953), Simonett (1960) and Skocek and Saadallah (1972). However, Richardson (1903, in Folk, 1971a) recorded coarsest size at the toe of leeward side of the dunes as the coarser grains rolled over the finer grains. Wait (1969, in Folk, 1971a) found no difference in mean size of dune crests and interdune flats, but crests were better sorted with positive skewness and more normal kurtosis. Mohan and Puri (1976) have reported that dunes are better sorted than interdune flat areas and also have positive skewness as compared to negatively skewed nature of the flat areas.

4.2.10 Spatial Variation of Grain Size Parameters

Taking the maximum values of grain size parameters of all the samples from barchans and sand piles, the area under investigation was contoured for the different grain size parameters. It may be emphasized that there is a fairly wide variation of grain size parameters within individual bedform and the ideal

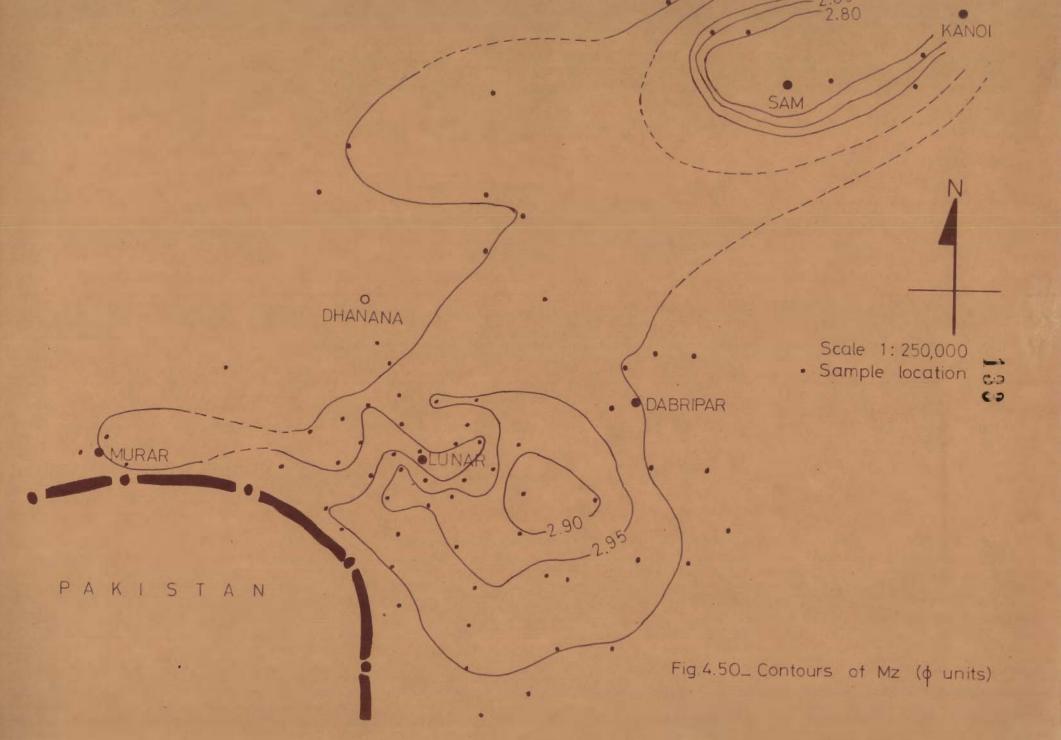
procedure for a study of spatial variation of grain size parameters would be to take samples from the same bedform and at similar location on the bedform. However, a particular bedform may not be present in all the areas of interest. To overcome this difficulty, two closely related bedforms i.e. barchans and sand piles were used for study of spatial variation of grain size parameters.

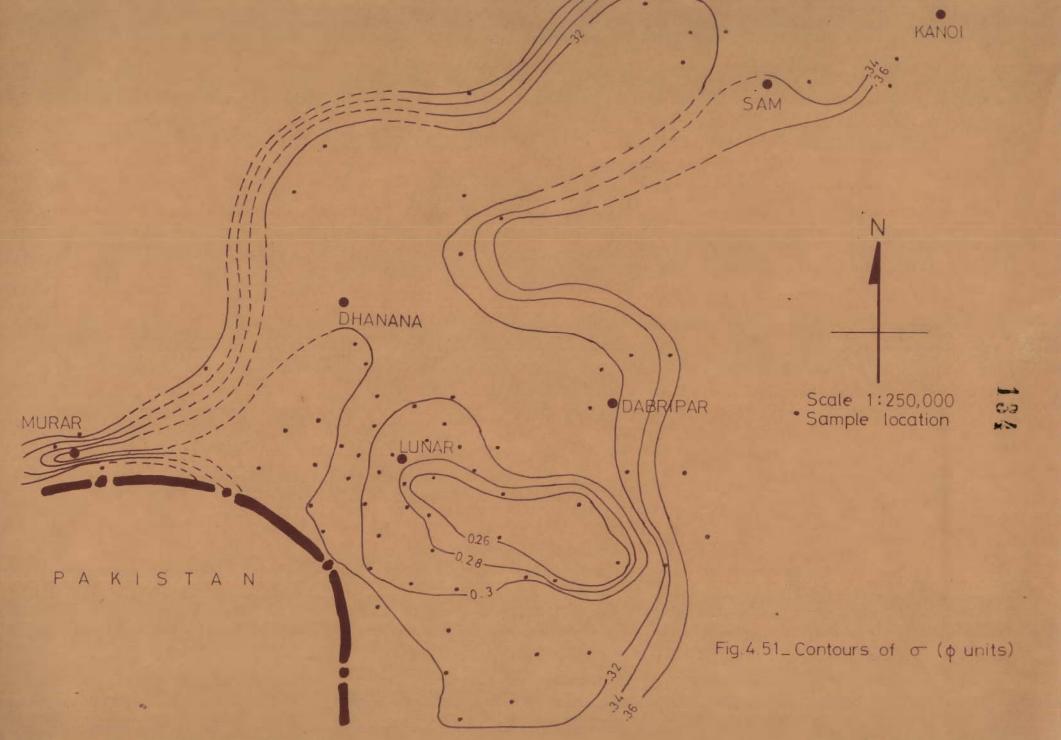
Variation in mean size shows that there are two highs one near Sam and the other near Lunar (Fig.4.50). The shape of the high near Lunar is circular, whereas, that of one near Sam is elongated in NE-SW direction, which is also the prevailing wind direction.

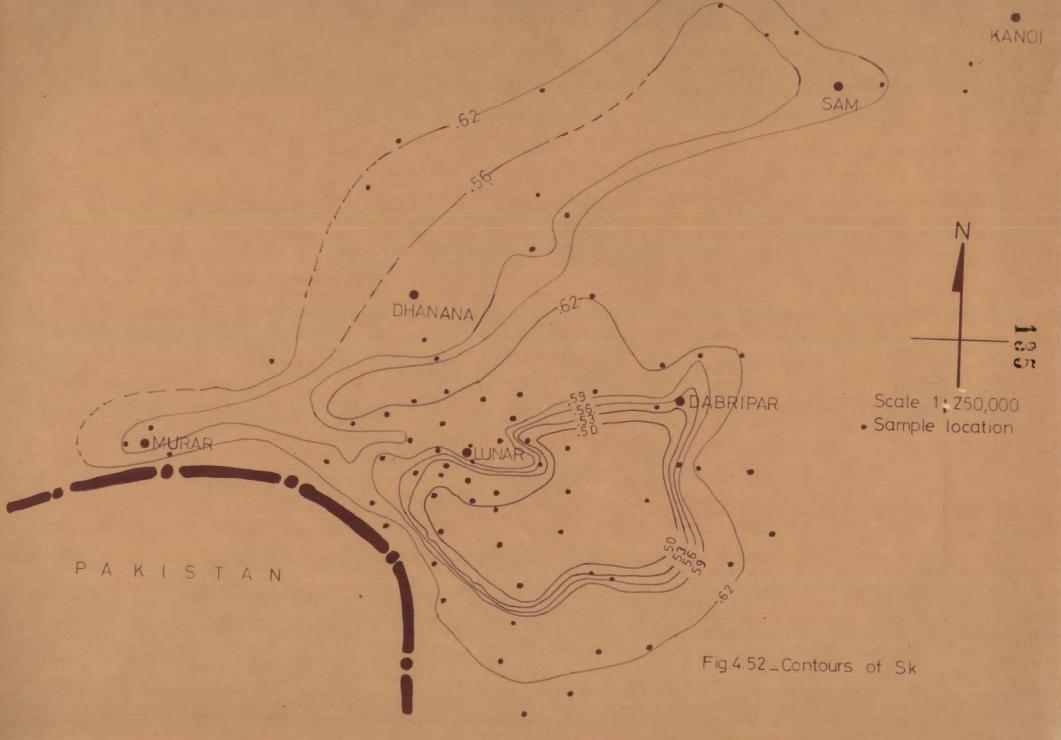
Sorting and skewness show systematic changes closely related to mean size (Figs.4.50 and 4.52). Standard deviation and skewness increase in value with decrease in grain size.

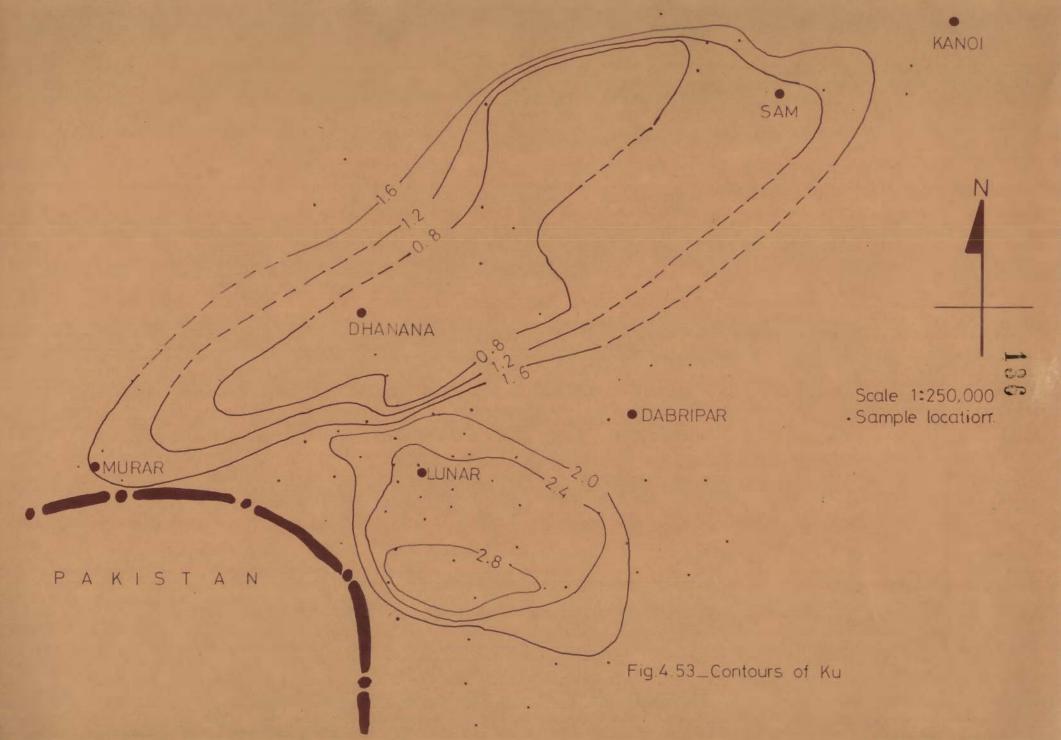
Kurtosis values decrease from 2.8 from a point near Lunar outwards to a value of 2.0, and there is a probable increase from 0.8 to 1.6 in a contour trough, elongated in the NE-SW direction in the area around Dhanana-Sam road (Fig.4.53).

No similar studies of spatial variation of grain size parameters in deserts are available for comparison, except that a limited study of areal variation of grain size parameters of cover sands of Botswana was made by Baillieul (1975) by taking a few traverses. According to him variation of









grain size parameters reflects the nature of local sources of sediments.

Systematic variations of mean size, sorting and skewness are the result of mixing, in different proportions, of saltation and suspension populations of grain sizes carried by the wind as explained in section 4.2.12. However, the presence of highs in mean size near Lunar and Sam are not clearly understood. At Sam, dunes form a large field in a flat area. The presence of the maximum size in the centre probably suggests that recycling of sediments by acolian transportation has been carried to the highest degree and these have been winnowed out of suspended sediment. In Lunar area, systematic areal variation in grain size parameters, is probably a reflection of areal grain size distribution of the older deposits which have been moulded by the wind into different bedforms.

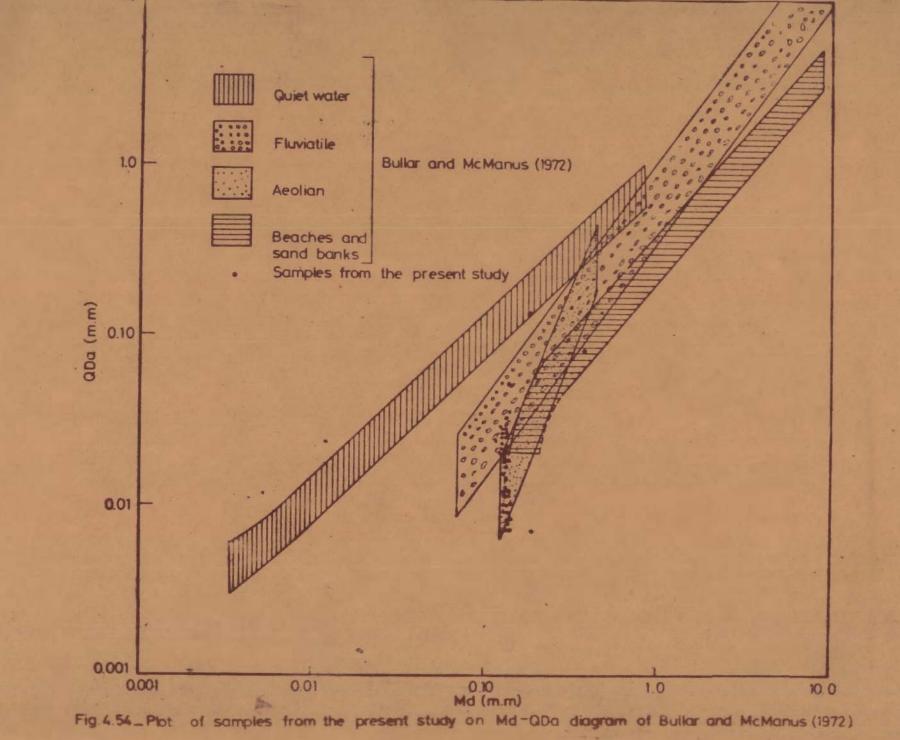
4.2.11 Evaluation of Grain Size Parameters for the Recognition of Desert Environments

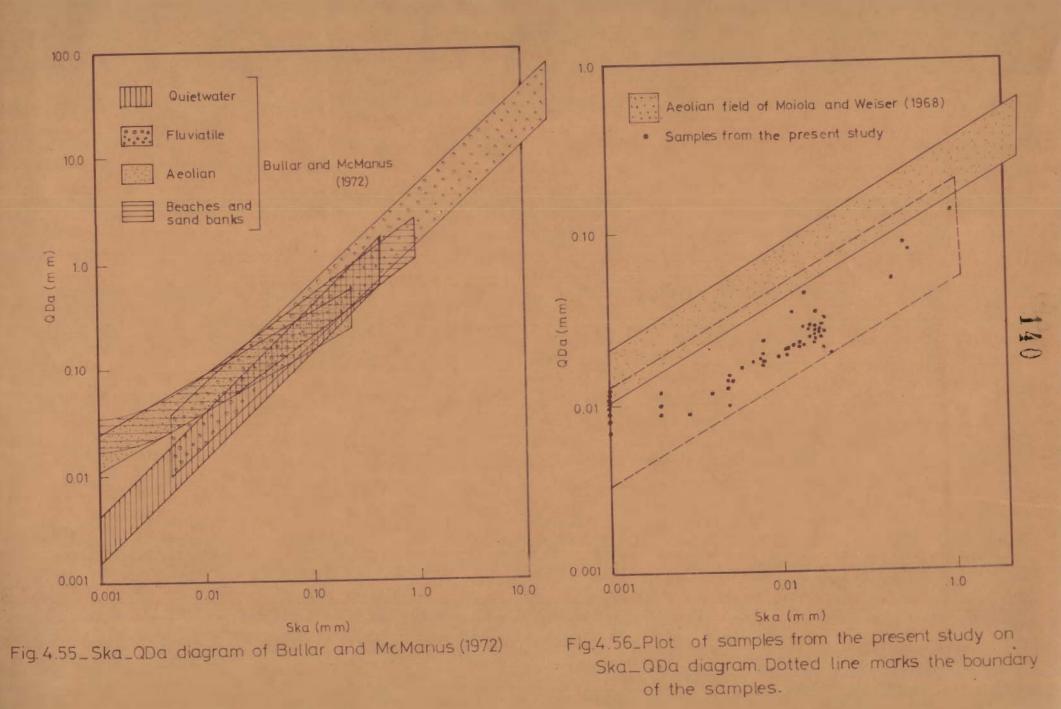
In recent years, many workers have tried to use grain size parameters for characterizing the various depositional environments (Passega, 1957, 1964; Sahu, 1964; Moiola and Weiser, 1968; Friedman, 1961, 1967; Buller and McManus, 1972). In the present study, an attempt is made to evaluate the usefulness of some of these diagrams in characterizing aeolian sediments. 4.2.11.1 Metric Based System of Buller and McManus (1972)

Metric based analysis has been suggested by Buller and McManus (1972) for distinction of aeolian, fluviatile, beach and quiet water deposits. Median-Md (mm) and Trask's quartitle skewness 'Ska' were plotted against Trask's quartile deviation 'QDa' on double log papers for the four environments (Figs.4.54-4.56). On each plot, the curves indicate a linear trend. The position and slope of the individual curves are different for different environments. Gradient of each curve was thought to reflect some environmental charactoristic relating size to sorting i.e. viscosity and current strength. In the plot of 'QDa' versus Md(mm), there is a decrease of gradient of curves in the sequence aeolian, fluviatile, beach and quiet water depostis and in the plot Ska versus Md(mm), there is a decrease of gradients of the curves in the reverse sequence.

Md, QDa and Ska in mm were determined using the cumulative frequency curves and the values are listed in Appendix VIII.

Plots of samples of the Thar desert in QDa-Md diagram form a very thin almost vertical band (Fig.4.54) indicating that median size range is very narrow in the samples under study, whereas sorting varies fairly widely. Also fairly large number of samples fall outside the aeolian field of Buller and McManus (1972). Plots of samples in Ska-QDa diagram (Fig.4.56) brings out clearly that most of the samples fall out side the aeolian field of Buller and McManus. Gradient of





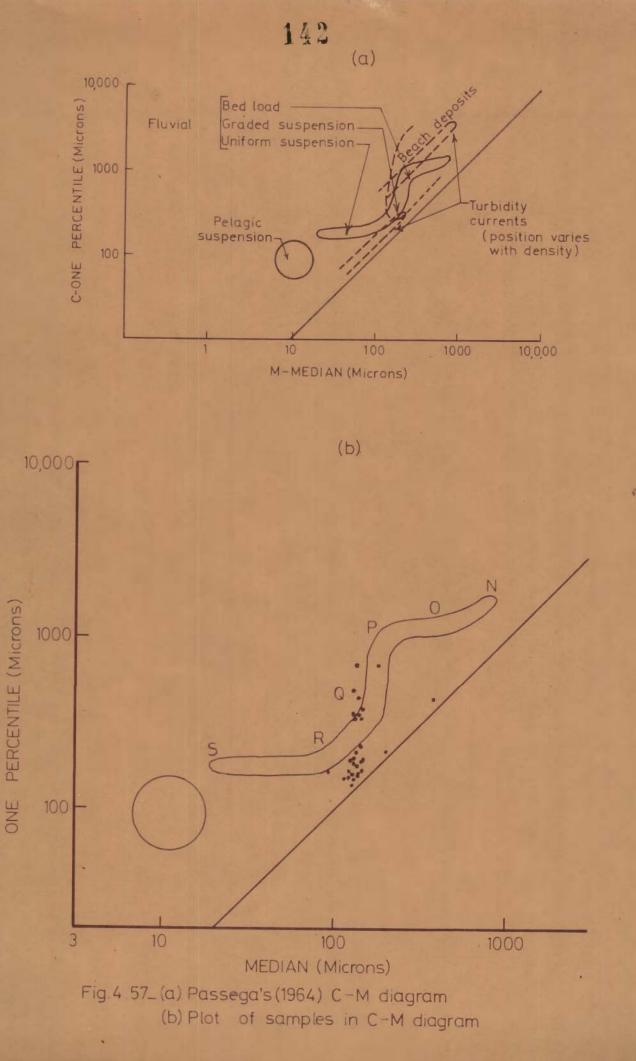
the field of samples under investigation is similar to that of Buller and McManus with the difference that we have consistently lower QDa values. Thus the type aeolian field should be widened to accommodate the present samples.

In conclusion, usefulness of the QDa-Md diagram is doubtful, but Ska-QDa diagram may prove quite helpful with minor modification in destinction of aeolian sediments.

4.2.11.2 C-M Pattern

Passega (1957, 1964) used two parameters obtained from grain size distribution curves i.e. C-coarsest one percentile and M - the median grain size. He obtained patterns for deposits of tractive currents, quet water, beaches and turbidity currents (Fig. 4.57a). These parameters were selected because the coarest fraction of a sediment is supposed to be more representative of the depositional agent provided that a full range of grain sizes was available for transportation.

It is realized that samples of the Thar desert are not strictly comparable to those studied by Passega(Op.cit) as his samples are from water borne sediments. However, the pattern of these sediments might give some insight into the process of deposition of the present sediments. Plots of samples of the Thar desert are concentrated in a vertical band with a median diameter ranging from 110 to 190 µ and C aranging from 130 to 800 µ suggesting that sand samples



consist mainly of one population with medians in a very small range and perhaps minor additions of coarse material give the observed grain size characteristics and C-M Pattern.

4.2.11.3 Mean Size Versus Standard Deviation Diagram of Friedman (1961)

Friedman (1961) delineated fields of river and inland dunes by plotting samples on mean size versus stansard deviation (Fig. 4.58). Moiola and Weiser (1968) plotted their samples on this diagram and found that these two textural parameters were not very effective in differentiating between river and inland dune sands. Plots of the samples under study fall in this diagram in a narrow area well inside the aeolian field of Friedman (1961).

4.2.II.4 <u>Skewness Versus Mean Diameter Diagrams of Friedman</u> (1961) and Moiola and Weiser (1968).

Friedman (1961) plotted skewness versus mean size and separated out areas of beach and inland dune sediments using sieves at $1/4 \ 0$ interval (Fig. 4.59). However, Moiola and Weiser (1968) had to shift the boundary between the two types of sediments slightly to accommodate their samples. The present samples are comparatively finer and more positively skewed than inland dunes of Moiola and Weiser (1968) and they fall far to one corner of the inland dune sediment field.



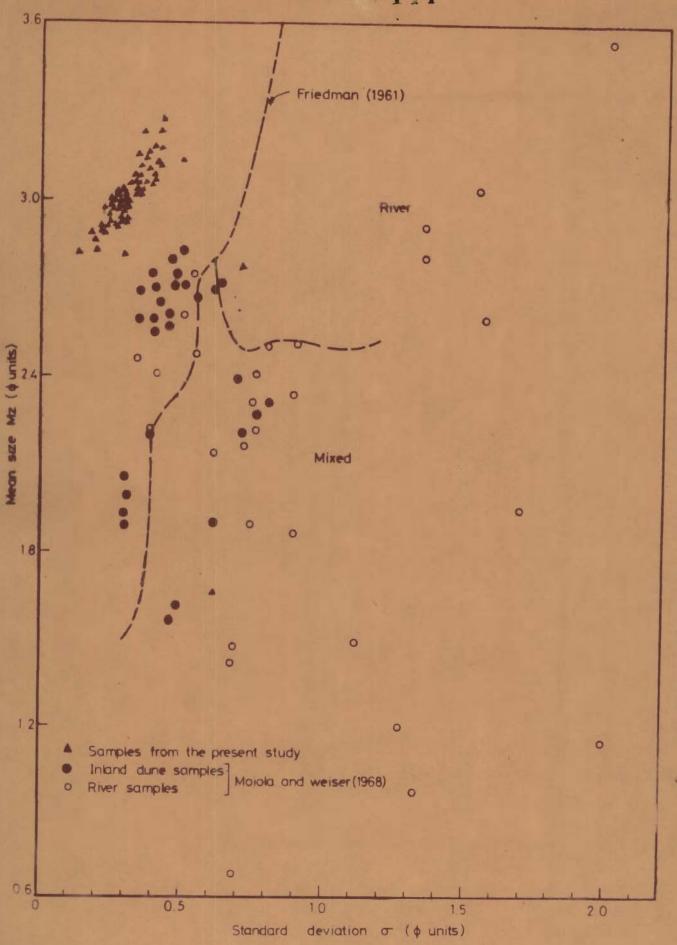
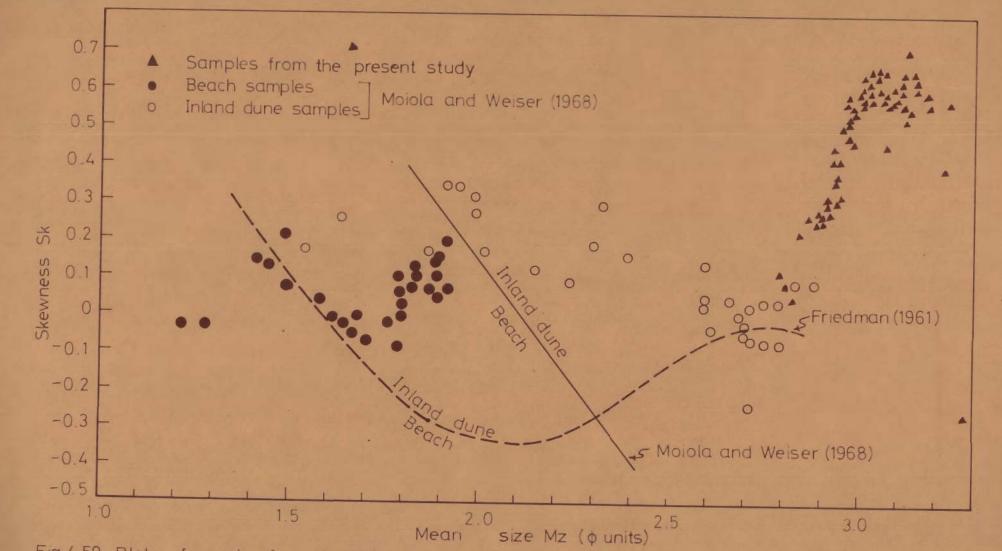


Fig.4.58_Plot of samples from the present study on mean size vs. standard deviation diagram of Friedman (1961) along with Moiola and Weiser (1968)



En

Fig.4.59_Plot of samples from the present study on skewness vs. mean size diagram with superimposed boundaries between beach and inland dune sediments after Friedman(1961) and Moiola and Weiser(1968)

Also, the present samples lie well inside the inland dune sediment field when these are compared with coastal dunes on skewness-mean size plot (Fig. 4.60) of Moiola and Weiser (1968).

4.2.11.5
$$\sqrt{\sigma^2}$$
 versus $\frac{s(Ku)}{s(Mz)}$ $s(\overline{\sigma}_2)$ plot of Sahu (1964)

Sahu (1964) carried out discriminant analysis of grain size data from different environments. From his study, it became apparant that the standard deviation of the discriminant functions were progressively increasing in the order: aeolian, beach and shallow marine sediments, which suggested that standard deviations of sample statistics might prove helpful in this regard and best results were obtained by plotting $\sqrt{\sigma^2}$ against $s_{(Ku)} \cdot /s_{(MZ)} \cdot s_{(\sigma^2)}$ on log -log paper (Fig. 4.61). The general direction of decreasing energy and fluidity for the different environments are also shown in the figure. The lines of demarcation between the processes and environments of deposition have been drawn visually.

The plot of samples under study comes in the right hand corner in the area of low energy (Fig. 4.61). But exclusion of a single sample of ripples with poor sorting shifts the plot to the lower part of the left hand side well inside the aeolian field. Thus, this diagram is very sensitive to slight changes in standard deviation of

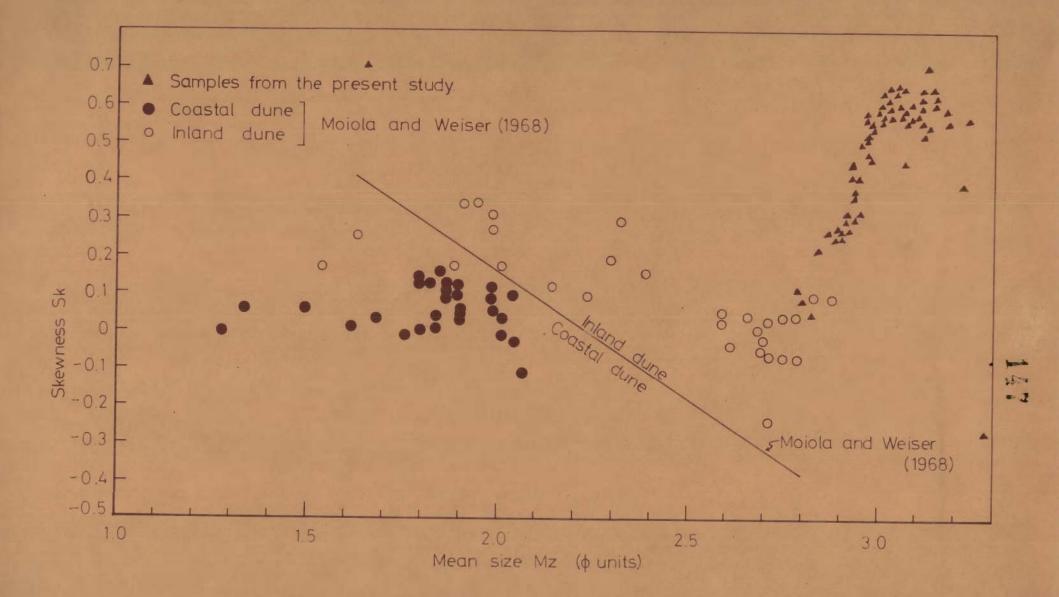


Fig.4.60_ Plot of samples from the present study on mean size vs. skewness diagram with superimposed boundary between coastal and inland dunes after Moiola and Weiser, 1968.

 \mathbf{e}_{i}

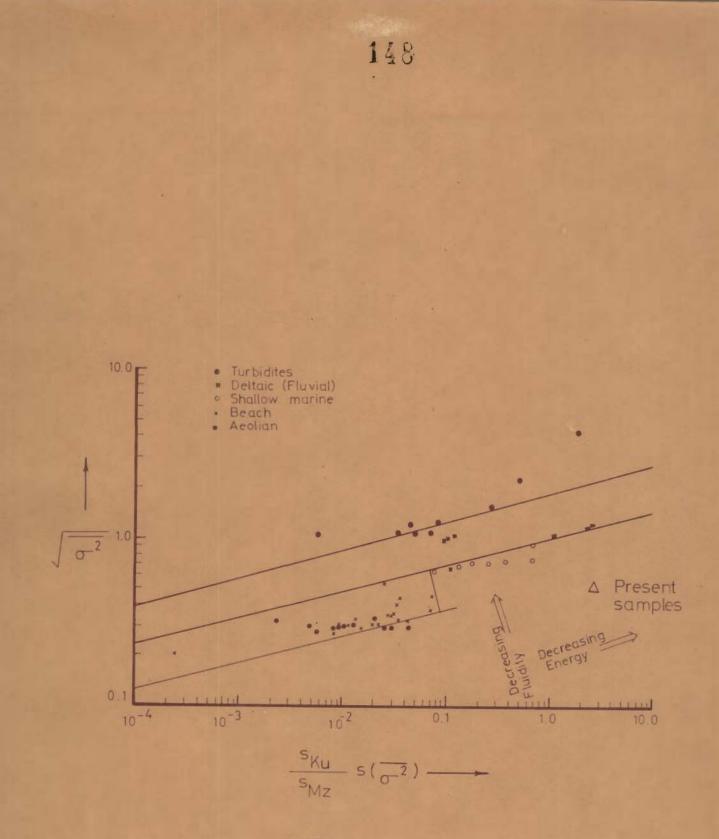


Fig. 4.61_Log log plot of $\sqrt{\sigma^2}$ Vs $\frac{s_{ku}s(\sigma^2)}{s_{Mz}}$ showing the differentiation between the environments of deposition after Sahu (1964) with the plot of present samples

sorting. Inclusion of larger number of samples from sand flats and repples might impair its usefulness for distinguishing aeolian sediments.

4.2.12 Grain Size Populations in Aeolian Sediments

In the present study, an attempt has been made to recognize basic genetic populations on the basis of cumulative curves according to the method suggested by Spencer (1963). In dunes and sand piles, commonly three populations A, B and C can be distinguished. Population A forms usually less than 1% of the samples . It is coarser than 2.5 \emptyset and is poorly sorted. Population B forms the major portion of the sands, commonly constituting 60% to 90% of the samples and lying mainly between 2.5 \emptyset and 3.25 \emptyset . Its sorting is excellent. Population C forms 10% to 40% of the samples and is finer than 3.25 \emptyset . Its sorting is excellent to good. Distributions of amounts of A and C populations in dunes and sand piles are shown in the form of histograms in Figure 4.62a. Histograms bring out the fact that amounts of population A are approximately log-normally distributed, whereas percentages of population C are approximately normally distributed.

In the case of sand flats, population A constitutes 2 to 10% of samples and its mixing with population B is extremely poor. Population B forms 30-60% of the samples and its mixing with population C is good. Except that population A may contain

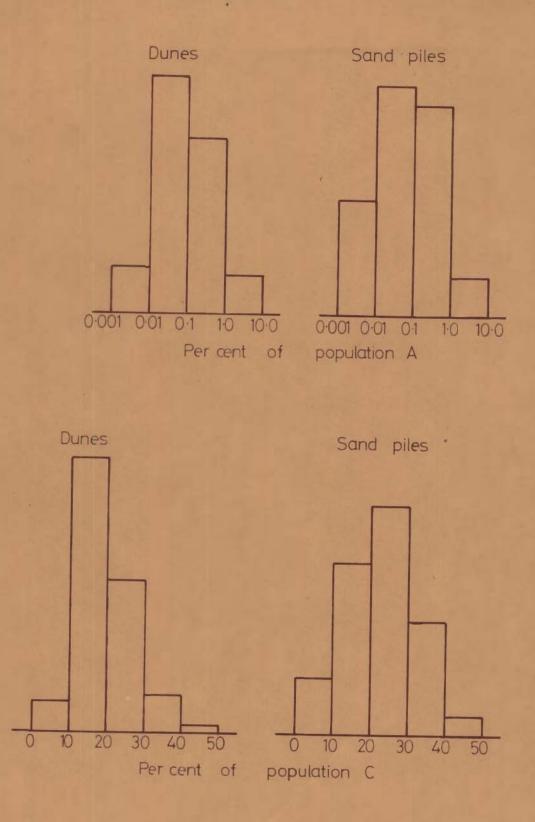


Fig. 4.62 (a)_Histograms showing distributions of amounts of populations A and C in dunes and sand piles.

particles of quite coarse size, the size limits of the different populations are similar to those of dunes and sand piles.Sand flats differ from dunes and sand piles essentially in possessing less amounts of population B and correspondingly higher amounts of populations A and C.

Ripples have population A in the range $1.0-1.5 \, \text{\emptyset}$ and distinction between populations B and C is difficult.

Bagnold (1937, 1941) and Sharp (1963) recognized three basic genetic types of populations i.e. (a) surface creep, (b) saltation population and (c) suspension populations in aeolian sediments. Populations A,B and C of the present study can obviously be taken as surface creep, saltation and suspension populations, though their maximum and minimum limits have a smaller range than hitherto reported.

Folk (1971a) dissected the frequency curves of grain size distributions of samples from Simpson desert, Australia He found that dune sediments consisted mainly of saltation population with mean size range of 1.5 \emptyset to 4.0 \emptyset . Also the sediments had different quanta or sub-populations with a standard deviation of 0.25-0.50 \emptyset . Each quantum is carried by a separate puff of wind and deposited in a particular microlocality as a laminae or a patch of grains.

Using an analysis similar to that of (Folk, 1971 a) for sand piles and dunes, it can be seen that these sediments consist mainly of two populations in different proportions i.e. and saltation population with a mean size of .2.75 p and standard deviation of about 0.2 p and another suspension population with a mean size of $3.75~\phi$ and a standard deviation of about 0.25 p . When these sediments consist mainly of saltation population with minor additions from suspension, sediment is well sorted with nearly symmetrical distribution and leptokurtic. With larger additions of suspension population to saltation population so that the two populations become subequal, composite frequency curve for the sample becomes poorly sorted, positively skewed and platykurtic (Fig. 4.62 b). This explains the observed interrelationship of the grain size parameters, their variation within dunes and their spatial variation.

Essential bimodal nature of the sand piles and dunes is obvious from the above discussion. Skocek and Saadallah (1971) summarized the various suggested causes of bimodality as follows:

> (a) Repeated reworking of a unimodal sand and thus transportation by saltation and suspension may produce bimodality of the aeolian sediments. This process is called 'rectification' by Wood (1970).

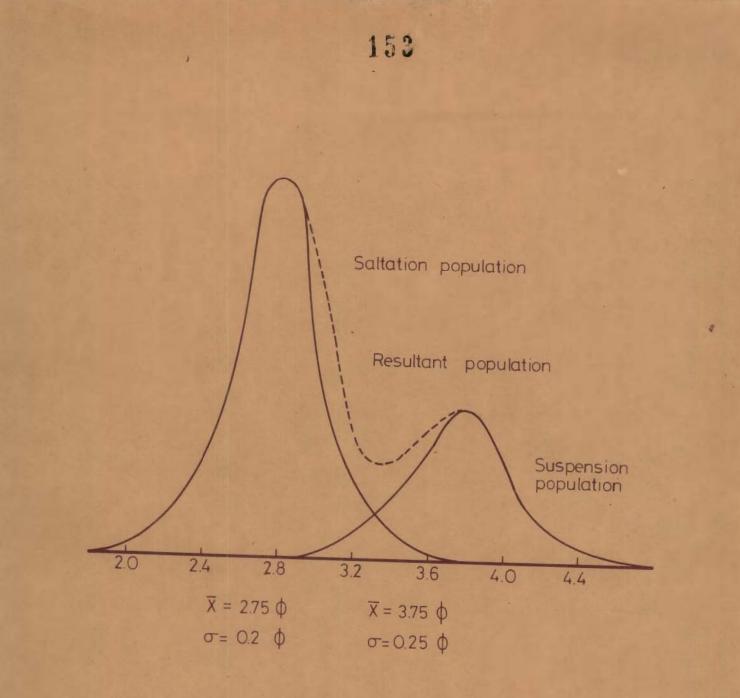


Fig.4.62(b)_Diagramatic representation to explain the observed grain size characteristics of samples studied by mixing of two distinct populations with \overline{X} =2.75 ϕ , σ =0.2 ϕ and \overline{X} =3.75 ϕ , σ =0.25 ϕ respectively.

- (b) Lack of grains in the range 3.0 \emptyset to 3.5 \emptyset in the source sediments could produce bimodality of the sediments under study.
- (c) Decomposition of unstable grains due to weathering may destroy certain grain size fractions of the source material.
- (d) Deposition of different 'quanta' of sediment sizes in various distinct layers with changing velocity of wind (Stokes, 1964; McKee and Tibbitts, 1964; Folk, 1971 a) may also explain bimodality of aeolian sands.
- (e) A large amount of fine material during slackening of dust storm may infiltrate down the sand.

Skocek and Saadallah (1971) favoured the infiltration hypothesis as mentioned above. In the present area also, such an explanation seems to be plausible. Fine materials, in the form of dust storms, could be transported from the flood plains of the Indus River in the upwind direction. There are plenty of fine materials along levees, flood basin and abandoned channels of the Indus rivers. Also fine sediment could be derived locally from the parent materials which were essentially fluvial sediments with plenty of fines and deposited by tributaries of the Indus, as mentioned elesewhere. Differences in grain size distributions of sand piles and dunes can be explained by the fact that piles are essentially stationary bedforms and fines, deposited by slackening dust storms, infiltrate down and with time their amount increases. However, barchan dunes travel under the influence of wind which transports sand.grains along the stoss side on to the crest and across with occasional avalanching of the sand along the slip face. This process is repeated continuously, whereby, fines may be picked up by the strong wind and removed from the dunes leaving dune sediments better sorted than sand piles.

4.3 STUDY OF ROUNDNESS

4.3.1 Procedure

Wadell (1932) first described a quatitative procedure for determination of roundness of particles and defined the 'degree of curvature' as the ratio of average radius of curvature of the different corners or edges to the radius of curvature of the maximum inscribed sphere or to the nominal radius of the fragment.

Using Wadell's scale of roundness, Russel and Taylor (1937) set up five roundness classes with irregular intervalc. Pettijohn (1949) redfined the class limits in such a manner that the middle points of classes form a geometric pattern. Folk (1955) defined six roundness classes such that the ratio of upper class limit to the lower limit of each class is 0.7 and called his scale as P(rho) scale.

It is tedius and cumbersome to determine the radius of curvature of corners and radius of the largest inscribed circle of a fragment and calculate the roundness value. In the present study, roundness values of individual grains were obtained by comparison with Folk's (1955) roundness images that are convenient to use because of the logarithmic nature of the scale. All the $1/2 \not 0$ size fractions of eleven samples were examined for their roundness using grain-mount slides and by studying one hundred clear quartz grains from each slide.

4.3.2 Operator Experiment

An operator experiment was performed to determine two factors (i) operator consistency and (ii) operator error resulting from variation from person to person. Four slides were selected randomly from the whole lot. These slides were analysed by two operators by the above described method. The experiment was repeated after two days by the same operators. The results are shown in Table 4.7.

Table 4.7 - Values of Xp for different slides and operators

| Slide No. | Operato | or No.1 | Operator | No.2 |
|-----------|---------|---------|----------|---------|
| | First | Second | First | Second |
| | attempt | attempt | attempt | attempt |
| 90/45 | 2.91 | 2.81 | 2.73 | 2.73 |
| 55/ F | 2.04 | 2.14 | 1.94 | 2.30 |
| 55/45 | 2.54 | 2.48 | 2.61 | 2.76 |
| 10/230 | 2.36 | 2.32 | 2.31 | 2.57 |

A Two Way Analysis of Variance model with replication (Miller and Kahn, 1962, p. 171) has been used to analyse the data. The calculations are done assuming that slides and operators are random samples from larger populations of thin sections and operators respectively. Results of ANOVA are given in Table 4.8.

Table 4.8 - Operator experiment data subjected to Analysis of Variance.

| Source of Variation | Degrees of freedom | Sun of squares | Mean squares | Variance Ratio F |
|-----------------------------|-----------------------|----------------|-----------------|---------------------|
| Variation between operators | l | 0.0076 | 0.0076 | 1.90 NS |
| Variation between slides | 3 | 1.0459 | 0.3486 | 87.15 ^X |
| Interaction | 4 | 0.1422 | 0.0355 | |
| Replication | 7 | 0.0280 | 0.0040 | |
| Total | 15 | 1.2237 | | |

NS - Not significant at $\alpha = 0.05$

X - Significant at $\alpha = 0.05$

Analysis of Variance (Table 4.8) brings out the following important features:

- (i) Replication error is very small (mean square = 0.004).
- (ii) Operator error due to personal bias of operators is not significant statistically.

3

(iii) Differences between mean roundness of slides are significant.

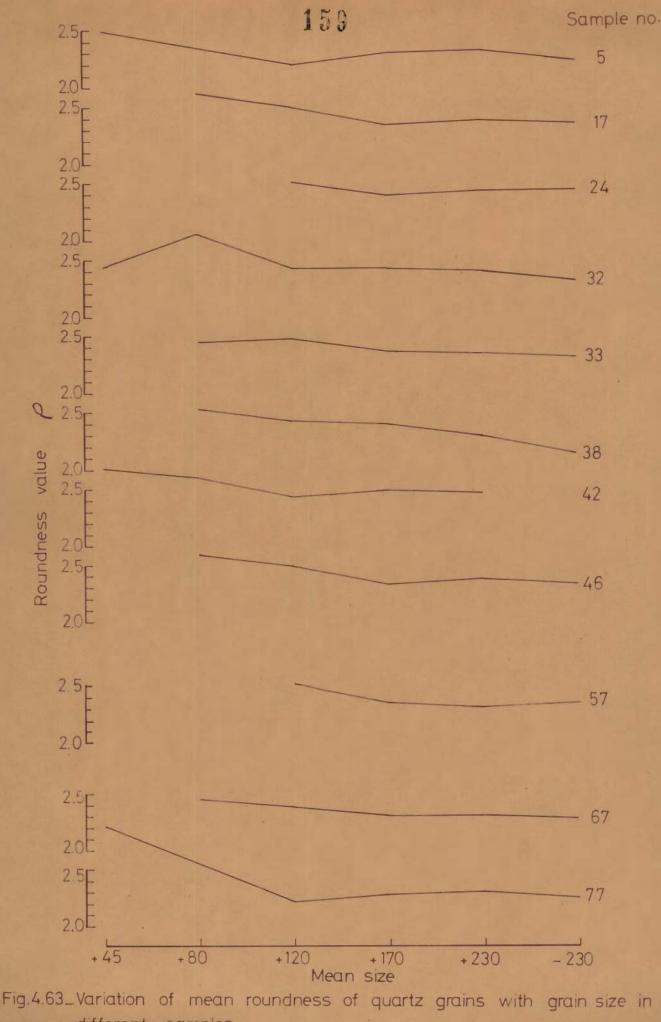
It is observed that differences between roundness values of different slides are small, but these can be detected by the present method.

Thus, it seems that the present method of determining roundness is quite satisfactory.

4.3.3. Results of Roundness Study

Mean and standard deviation of roundness for different slides are listed in Table 4.9. Mean roundness for different slides has a very limited range of 2.02 to 2.91P suggesting thereby, that different sized quartz grains are mainly subangular in nature. Standard deviation of roundness of the different slides also has a limited range of 0.30 to 0.67P indicating that all the grains in a certain size fraction are rounded approximately to the same degree.

Variation of roundness with grain size is shown in Figure 4.63. It seems that there is extremely small, but distinct decrease in roundness value with decrease in grain size. Also Figure 4.63 brings out the fact that quartz grains smaller than 120 mesh (0.125 mm) have roughly the same roundness value, whereas, particles larger than 120 mesh show higher roundness values, thereby suggesting that wind is an effective rounding agent



different samples.

a had been added and

for particles carried in saltation and traction.

Table 4.9 - Mean and standard deviation of roundness values of quartz grains of the various fractions of different samples

| Sample No. 17 | | 7 | 24 | | 3 | 2 |
|--|--------------------------------------|--------------------------------------|------------------------------|------------------------------|--|--|
| Size Frac- tions | | | π _ρ | Sp | xρ | sp |
| +45 Mesh +80 Mesh +120 Mesh +170 Mesh +230 Mesh -230 Mesh | 2.62 2.50 2.36 2.39 2.36 | 0.43 0.35 0.46 0.45 0.45 | 2.51 2.39 2.42 2.43 | 0.41 0.48 0.50 0.37 | 2.43 2.72 2.42 2.41 2.39 2.30 | 0.42 0.55 0.47 0.37 0.42 0.46 |

| Sample No. | 33 | | 38 | | 42 | | |
|--|--------------------------------------|--|--------------------------------------|--------------------------------------|--------------------------------------|--------------------------------------|--|
| +45 Mesh +80 Mesh +120 Mesh +170 Mesh +230 Mesh -230 Mesh | 2.44 2.47 2.37 2.34 2.31 | | 2.52 2.42 2.38 2.29 2.13 | 0.34 0.30 0.48 0.48 0.58 | 2.68 2.59 2.42 2.48 2.45 | 0.52 0.51 0.41 0.44 0.33 | |

| Sample No. 46 | | 6 | 52 | 5' | 57 | | |
|---------------|------|------|------|------|------|------|--|
| +45 Mesh | 2.54 | 0.41 | | | | | |
| +80 Mesh | 2.53 | 0.52 | 2.57 | 0.50 | | | |
| +120 Mesh | 2.40 | 0.43 | 2.28 | 0.52 | 2.52 | 0.45 | |
| +170 Mesh | 2.24 | 0.49 | 2.22 | 0.48 | 2.33 | 0.51 | |
| +230 Mesh | 2.04 | 0.67 | 2.10 | 0.51 | 2.30 | 0.47 | |
| -230 Mesh | 2.02 | 0.59 | 1.79 | 0.56 | 2.33 | 0.45 | |

| 1 | £ | 1 |
|---|---|---|
| 1 | U | À |

| lesh | | In the second seco | Non-second second second | | | |
|------|------|--|---|--|--|---|
| | | | 2.91 | 0.54 | 0.50 | |
| lesh | 2.47 | 0.45 | C . JT | 0.94 | 2.50 | 0.51 |
| lesh | | | 2 20 | 0.54 | | 0.50 |
| lesh | | | | | | 0.44 |
| | | | | | 2.56 | 0.41 |
| | | | | 0.38 | 2.36 | 0.53 |
| esn | 2.29 | 0.46 | 2.27 | 0.42 | 2.43 | 0.51 |
| | esh | esh 2.40 esh 2.32 esh 2.32 | esh 2.40 0.45 esh 2.32 0.49 esh 2.32 0.42 | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | 2.47 0.45 2.47 esh 2.40 0.45 2.20 0.54 2.51 esh 2.32 0.49 2.30 0.42 2.56 esh 2.32 0.42 2.32 0.38 2.36 esh 2.29 0.46 2.27 0.45 |

4.4 STUDY OF SPHERICITY OF QUARTZ GRAINS

4.4.1 Introduction

Russel and Taylor (1937) observed that both experinental and petrographic studies of natural sands suggested that sphericity of quartz sand grains was not significantly nodified by abrasion, but was inherited from the parent rock. Krynine (1940) found that clastic quartz of metamorphic origin tended to be more elongated than that of igneous rocks. Pettijohn (1957, p. 66, 119) also emphasized that the end shape of a sand grain depends upon its original shape. Thus there could be some quantitative distinction between quartz grains of different origins.

Sphericity (ψ) of quartz grains has been commonly studied by measuring axial ratio i.e. short axis/long axis after Bokman (1952) who claimed that there existed significant differences in axial ratios of quartz grains from schistose and granitic sources. Numerous observations of axial ratios of quartz grains in thin sections show that the average axial ratio of quartz grains ranges only from 0.61 to 0.73 (Griffiths, 1967, p.123). Bokman (1957) too endorsed it subsequently.

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Mukherjea (1975) has restudied data of Bokman (1952) and claims that a major inflection point exists at elongation quotient (inverse of axial ratio) at 1.2 and a minor one around 2.0. He found that the various transformations do not help in normalisation of data. Also he suggests a triangular diagram for possible identification of schistose and plutonic sources.

Sahu and Patro (1970) indicated that $\log(\psi/1 - \psi)$ transformation normalized the sphericity distributions. Sahu (1973) attempted to relate sphericity distributions with environments.

In the present study, sphericity of quartz grains has been studied with a view to determine their possible ultimate source and the effect of aeolian action on the mean sphericity and type of distribution.

4.4.2 Procedure of Study

Five sand samples studied for roundness from widely separated localities were selected. Slide mounts of all the $1/2 \ 0$ size fractions were examined for axial ratios of

quartz grains. The maximum number of grains available in the slide or grains observed in four fields of view (:100 grains) were studied.

Distributions of sphericity values of quartz grains are depicted in the form of cumulative frequency curves on arithmatic-probability paper in Figures 4.64 - 4.68. Mean and standard deviation for sphericity of each slide are calculated and are listed in Table 4.10.

4.4.3 Distribution of Sphericity Values

Nature of distribution of sphericity values has been examined by studying the shape of cumulative frequency curves in Figures 4.64 - 4.68. These curves can be grouped into polymodal, normal, posicitively skewed and negatively skewed classes. All the curves except that for slide 5/230 lend themselves to this type of visual examination. The curve for slide 5/230 is positively skewed in the lower part and negatively skewed in the upper part and as such has been grouped in polymodal class. This analysis gives the following results for different curves: normal - 11, polymodal - 6, positively skewed - 4 and negatively skewed - 4. Thus it seems that there is no need for any transformation of the sphericity data. Deviations from normality probably reflect the degree of abrasion, distance from the source and mixing of sediments from different sources.

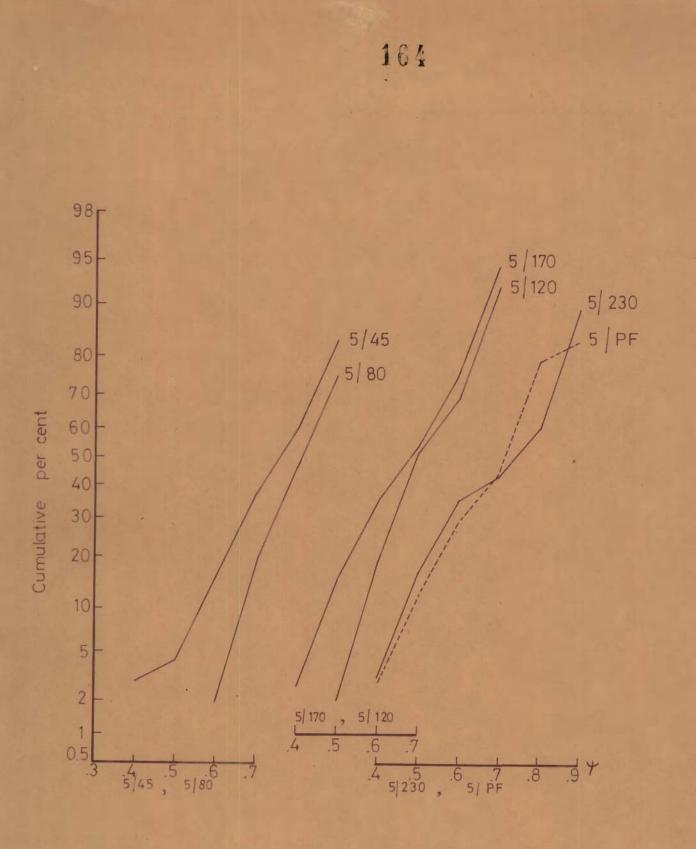


Fig. 4.64_Cumulative per cent frequency curves for sphericity values of quartz grains of different fractions of sample 5.

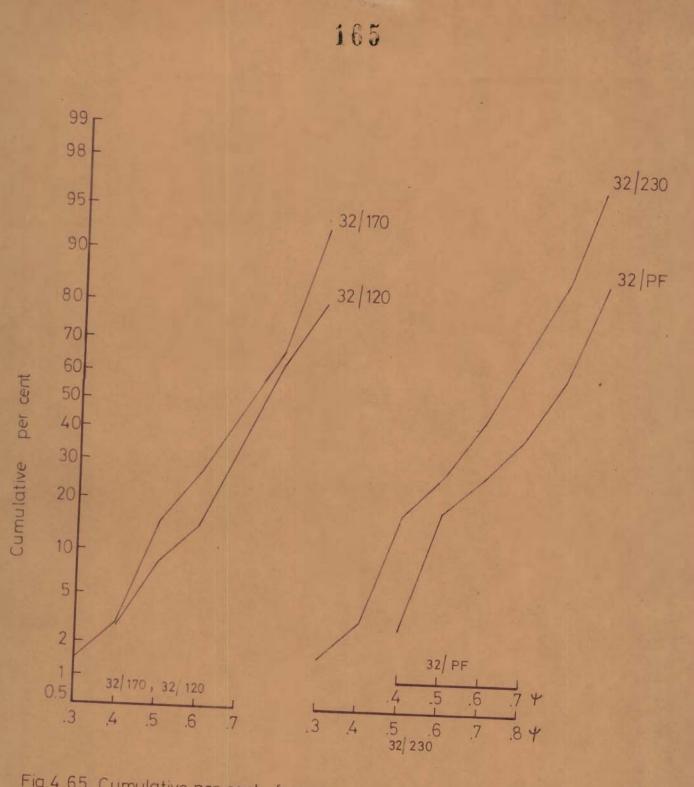
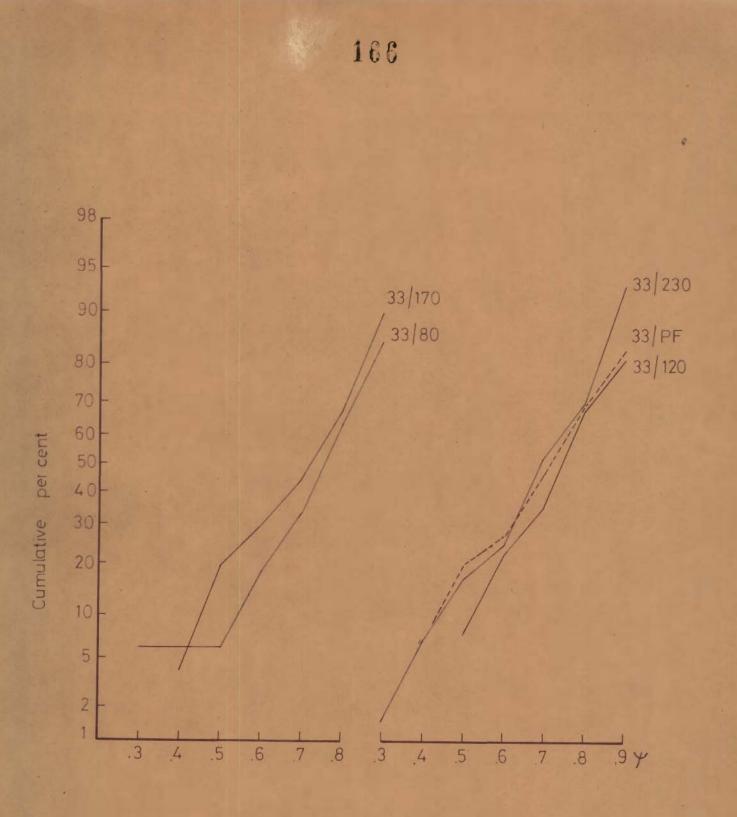
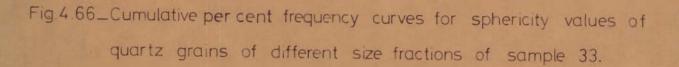


Fig.4.65_Cumulative per cent frequency curves for sphericity values of quartz grains of different size fractions of sample 32.





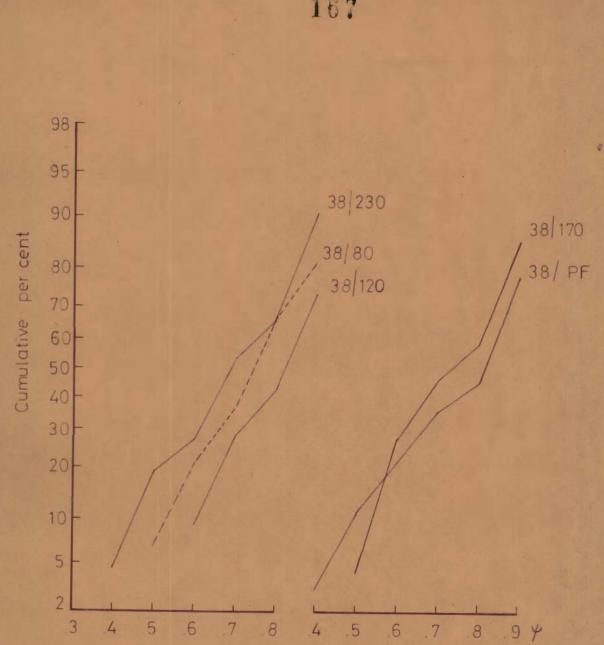


Fig. 4.67_Cumulative per cent frequency curves for sphericity values of quartz grains of different size fractions of sample 38,

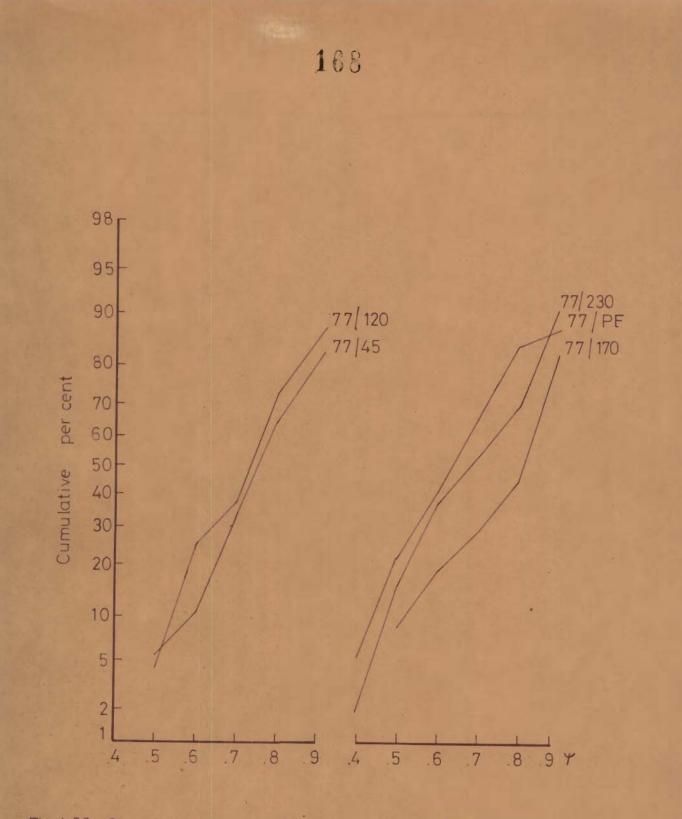


Fig.4.68 Cumulative per cent frequency curves for sphericity values of quartz grains of different size fractions of sample 77.

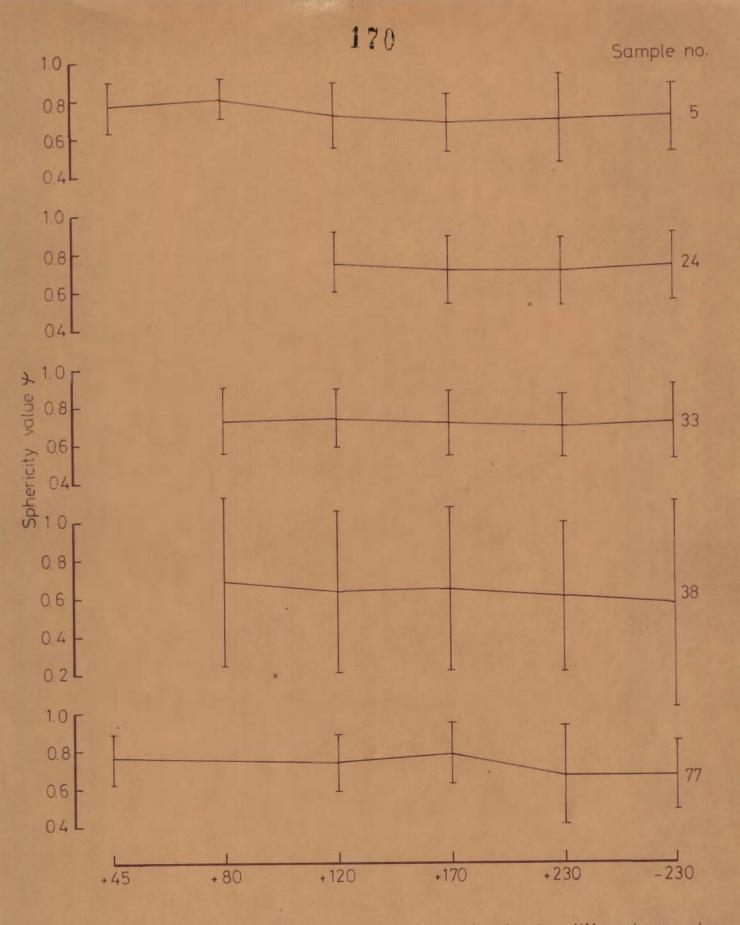
4.4.4 Mean and Standard Deviation of Sphericity Values

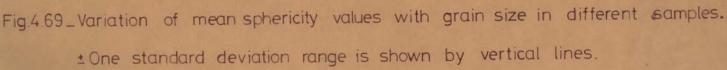
Mean value of sphericity for the different slides ranges from 0.56 to 0.81 t However, for most of slides it lies between 0.6 and 0.78 t (Table 4.10). Also, there seens to be little evidence of change of mean sphericity with grain size (Fig. 4.69). All fractions of sample no. 38 show consistently low sphericity values.

Standard deviation of sphericity values for the four samples with numbers 5,24,33 and 77 ranges from 0.11 to 0.20 \Downarrow but for the sample number 38 from Rangarh area, it varies from 0.39 to 0.54 \Downarrow and these are much higher than those reported from other areas (Griffiths, 1967, p.123). In the vicinity of Rangarh, there are exposures of Jurassic and Eocene sandstones and limestones. It seens probable that quartz grains of all size fractions under consideration with lower sphericity value are contributed from these rocks resulting in slightly lower nean and high standard deviation for sphericity values.

Release of low sphericity quartz grains from the Jurassic and Eocene sediments suggests that perhaps these sediments are also first cycle ones which did not suffer much transport before deposition.

Synthesis of the present observations and those of others (Griffiths, 1967, p.123) suggests that slight





| Mesh | · · · · · · · · · · · · · · · · · · · | Sample | and stands to a second stand stands of the second standstandstandstandstandstandstandstand | Se | mple No.22 | | | Sample No. | 33 |
|------|---------------------------------------|---------|--|-------------------|------------|------------------------------|-------|------------|------------------------------|
| size | Mean | s.d. | type of distri- bution | Mean | s.d. | type of distri- bution | Mean | s.d. | type of distri- bution |
| +45 | 0.769 | 0.135 | N | | | | | | |
| +80 | 0.814 | 0.103 | N | | | | 0.730 | 0.170 | N |
| +120 | 0.719 | 0.172 | SP | 0.755 | 0.158 | N | 0.737 | 0.149 | N |
| +170 | 0.680 | 0.153 | N | 0.714 | 0.173 | SN | 0.710 | 0.172 | N |
| +230 | 0.702 | 0.226 | Р | 0.706 | 0.177 | SN | 0.694 | 0.162 | P |
| -230 | 0.708 | 0.176 | Р | 0.727 | 0.177 | SN | 0.713 | 0.196 | P |
| | | | | | | | | | |
| | | Sample | No 38 | So | male Me 77 | | | | |
| | | vampro. | 110.00 | Da | mple No.77 | | | | |
| +45 | | | | 0.759 | 0.135 | N | | | |
| +80 | 0.689 | 0.444 | P | | | | 5 | | |
| +120 | 0.636 | 0.422 | Ŋ | 0.735 | 0.145 | P | | | |
| +170 | 0.639 | 0.428 | SP | 0.785 | 0.160 | SN | | | |
| +230 | 0.602 | 0.352 | N | 0.666 | 0.253 | SP | | | |
| -230 | 0.562 | 0.538 | SP | 0.666 | 0.180 | N | | | |
| · | | | **** | | | | | | |
| | | | N- Nor P- Pol | rmal. Lymodal. | | | | | |
| | | | SN- Neg | gatively sk | ewed. | | | | |

Table 4.10- Mean, standard deviation and type of distribution of sphericity values

SP- Positively skewed.

abrasion gives nean sphericity values of 0.6 to 0.8 ψ , so that away from the source, axial ratios can hardly be of any significance regarding their provenance. However, if the sediments have not travelled far from a metamorphic source, the provenance may be reflected in slightly lower sphericity and higher variance than as commonly observed.

CHAPTER - 5

PETROGRAPHIC STUDIES

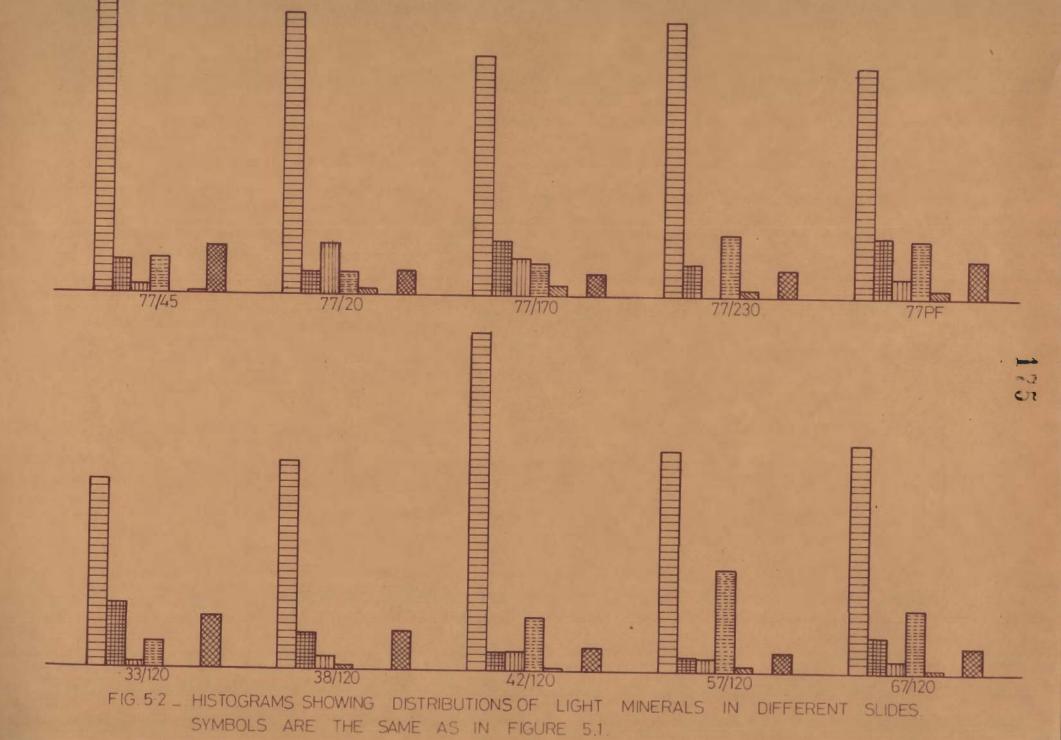
5.1 INTRODUCTION

A prolininary study of the petrography of the aeolian sands has been made to determine variation in light and heavy minerals with grain size, regional variation in petrographic composition and to find out provenance of these sands.

5.2 LIGHT MINERALS

5.2.1 Method of Study

Light minerals have been studied under a polarizing microscope by mounting grains on slides with Canada balsam. Maximum number of grains available or about 170 grains are counted. All the half phi size fractions of three samples with number 5,24 and 77 have been analysed for light mineral composition. Modal composition data for different fractions of these samples are utilized to recalculate modal composition of the whole samples. In addition, +120 mesh fractions of five other samples have been analysed for light mineral composition. Modal analysis data are listed in Table 5.1 and histograms depicting distributions of the different modes of the various slides are shown in Figures 5.1 - 5.2.



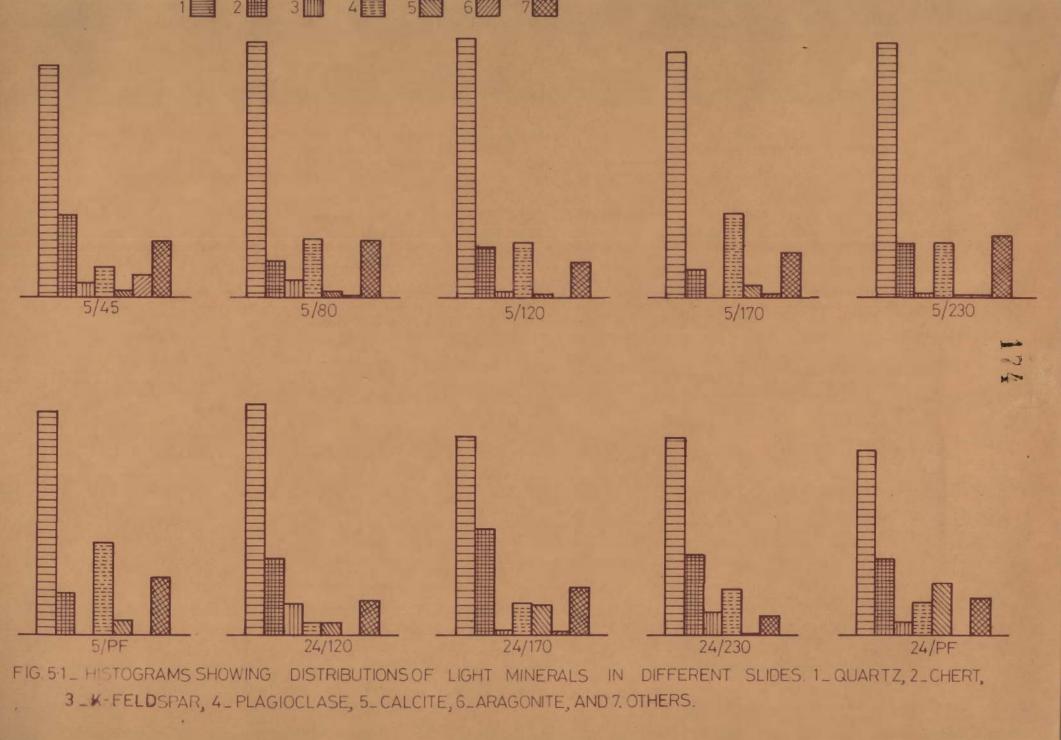
Mainly six modes i.e. quartz, chert, K-feldspar, Plagioclase, calcite and aragonite are recognized. Heavy minerals and opaques are grouped in 'others' category.

5.2.2 Description of Light Mineral Constituents

A brief description of light mineral modes and their significance is given below.

5.2.2.1 Quartz

The percentage of quartz varies from 45 to 71 for different slides, though its amount ranges from 51.4 to 55.9%. for complete sand samples. Its shape varies considerably from angular to rounded. Many grains are pitted and exhibit grounded surfaces. Striations on grain surfaces are not uncommon. Inclusions of tourmaline crystals are observed in a few grains. Tourmaline inclusions are sharp, well defined prismatic needles randomly distributed in the grain. Some grains have tiny inclusions of iron exide, which are distributed randomyly or arranged in straight lines. Quartz grains show often straight or uneven fractures. Many grains are stained by iron exide which often penetrates the fractures of the grains. Quartz grains are distinguished from feldspar by low relief and fresh appearance.



The use of undulosity in detrital monocrystalline quartz for provenance interpretation declined significantly since Blatt and Christie (1963) suggested that broad overlap in character of undulosity of plutonic and metamorphic quartz makes determination of undulosity of quartz of little value in source identification. Also these workers observed that flat stage microscopic measurements of undulosity lack validity because they bear no simple relation to the true values which are measurable on a universal stage. However, Blatt, Middleton and Murray (1972, p. 272 - 274) observed that number of crystal units in sand sized grains of polycrystalline quartz varies depending on the source rock of quartz.

More recently Basu et al. (1975) suggested that the distinction among quartz grains from different sources remains valid even when a flat stage microscope is used for determination of undulosity. Also determination of undulosity of monocrystalline quartz, percentage of polycrystalline quartz and number of crystal units per grain leads to a striking discrimination of source rocks such as plutonic, and low, medium and high rank metamorphic rocks.

Following Basu et al. (1975), four types of detrital quartz were recognized i.e.,

(i) quartz with single crystal unit, having ≤5° undulosity, called as monocrystalline, non-undulatory quartz,

- (ii) quartz with a single crystal unit, having >5°
 undulosity named monocrystalline undulatory
 quartz,
- (iii) polycrystalline quartz with 2-3 crystal units per grain and
- (iv) polycrystalline quartz with more than 3 crystal units per grain.

Percentages of different types of quartz are also listed in Table 5.1. Different slides and the whole sand samples are represented in the diagram of Basu et al. (1975) (Fig. 5.3). All slides and samples fall in the low to high rank metamorphic provenance zones of the diagram.

5.2.2.2 Chert

Chert grains constitute 3 to 25% of different slides and 8.0 to 11.7% of whole sand samples. These grains show turbid appearance with low relief. Some grains show a slight fibrous nature and exhibit anomalous optical properties. These also **s**how surficial fractures.

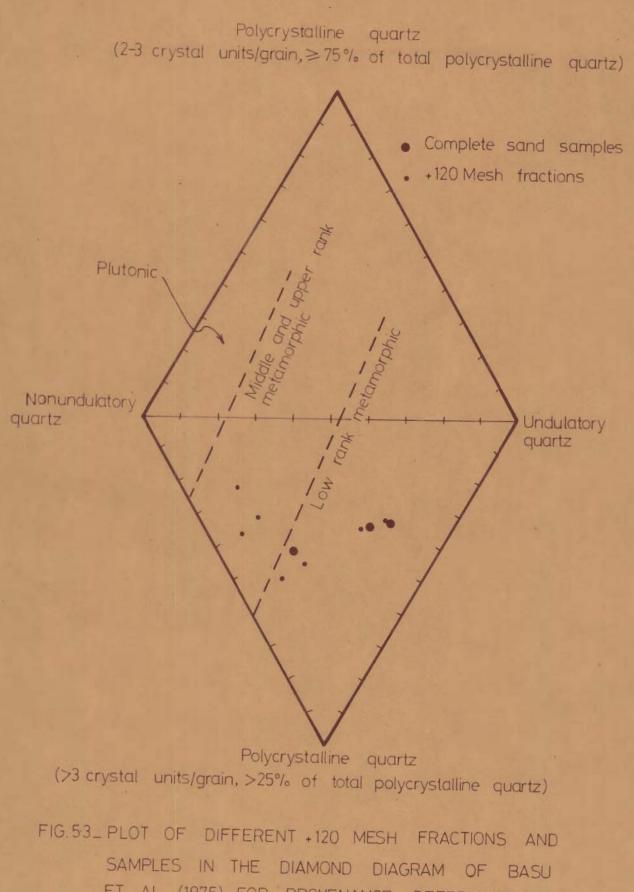
5.2.2.3 K-feldspars

The K-feldspars constitute upto 12.5% of detrital grains of different slides, but form 8 to 11.7% of whole sand samples. Many grains show twinning according to

Table 5.1- Modal analysis of different slides and samples

| nle No | Non un- dulose quartz | Undulose quartz | Polycrys quar 2-3 gra- ins | tz | Chert | K-feld- spar | Plagio- clase | Calcite | Aragonite | Others |
|--|---|---|--|--|---|---|--|---|-----------|--|
| 5/45 5/80 5/120 5/170 5/230 5/PF 24/120 24/170 24/230 24/PF 77/45 77/120 77/170 77/170 77/230 77/PF 33/120 38/120 38/120 57/120 57/120 57/120 | 18.84 20.49 12.29 8.39 5.56 10.99 14.41 8.43 6.19 10.54 30.11 23.33 28.37 25.85 33.77 32.69 25.92 45.52 26.60 23.13 11.16 12.98 25.79 | 11.54 16.40 30.73 28.29 27.79 28.39 24.02 22.76 27.40 21.08 5.26 14.73 15.89 14.96 5.28 5.45 8.55 10.12 9.26 8.41 30.11 24.98 13.01 | $\begin{array}{c} 8.33\\ 7.17\\ 4.92\\ 4.19\\ 16.67\\ 0.92\\ 6.73\\ 6.74\\ 7.96\\ 4.87\\ 6.95\\ 11.05\\ 10.21\\ 17.65\\ 10.55\\ 5.45\\ 10.55\\ 5.45\\ 6.41\\ 5.06\\ 9.26\\ 13.67\\ 6.36\\ 13.67\\ 6.89\\ 10.99\\ 10.99\end{array}$ | 15.73 17.42 14.75 16.76 6.67 10.07 12.48 8.43 7.96 8.11 22.00 19.64 5.68 9.52 5.28 15.26 10.68 10.11 13.87 15.77 13.82 11.62 15.55 | $18.84 \\ 8.54 \\ 12.05 \\ 6.63 \\ 12.30 \\ 9.65 \\ 18.51 \\ 24.52 \\ 20.42 \\ 21.39 \\ 7.70 \\ 5.62 \\ 14.12 \\ 7.82 \\ 14.18 \\ 17.71 \\ 9.66 \\ 4.97 \\ 2.25 \\ 9.76 \\ 11.67 \\ 19.08 \\ 7.98 \\ \end{array}$ | 3.14 3.98 1.45 1.07 7.93 1.16 6.18 3.05 1.92 12.50 9.41 - 5.03 1.71 3.86 3.11 3.93 3.66 1.30 7.32 10.57 | $\begin{array}{c} 6.80\\ 14.23\\ 13.50\\ 19.38\\ 12.30\\ 20.90\\ 3.17\\ 7.53\\ 11.76\\ 7.94\\ 8.66\\ 5.62\\ 7.85\\ 15.05\\ 13.74\\ 7.43\\ 19.81\\ 14.29\\ 27.53\\ 17.07\\ 13.80\\ 4.58\\ 7.52 \end{array}$ | 1.05 1.14 0.96 3.06 0.54 3.21 3.17 6.95 4.95 12.83 1.25 2.61 1.81 1.82 0.48 0.62 1.69 0.61 1.06 3.64 1.48 | 0.48 | 15.20 10.05 9.34 12.28 16.57 15.87 9.57 12.50 6.54 10.18 12.92 6.25 5.84 7.30 10.36 14.29 10.63 6.21 5.62 7.93 10.53 5.29 7.04 |

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ET AL. (1975) FOR PROVENANCE DETERMINATION.

carlsbad law or cross-hatched twinning typical of microcline. The feldspar grains are angular to rounded in shape. On the whole, they show higher degree of roundness than quartz grains. Often feldspar grains are weathered along cleavage or twin planes which are altered to clay minerals imparting them cloudiness — a fact which helps in their diagnesis. Feldspars show all degrees of alteration from completely unaltered to almost fully altered nature. Inclusions of quartz and iron exide are seen in a few grains.

5.2.2.4 Plagioclase Feldspars

The percentage of plagioclase feldspars shows a fair degree of variation i.e. 3 to 28% for different slides. Compositionally they are albite to oligoclase in nature. These are recognised by their well marked cleavage and albite law twin lamellae. They also show higher roundness as compared to quartz grains. A few very angular grains are also observed. These feldspars show highere degree of weathering than K-feldspars. Most of the grains show rigoures of weathering and some are rendered almost opaque due to alteration to clay minerals. Alteration of feldspars is often along the twin lamellae, cleavage or fractures. A few unweathered grains are observed from -230 mesh fractions, occasionally containing inclusions of iron exide.

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5.2.2.5 Calcite

Calcite forms upto 7% grains of different slides. It occurs as well rounded grains showing pitted appearance often resulting in general grounding of the grain surface which masks its typical sheen. A few grains show clear sparry calcitic nature. Coloured spectrum bands are seen even under polarized light with characteristic sheen in some grains.

5.2.2.6 Aragonite

A few aragonite chips with woody appearance are seen. These show parallel striations. Ornamentations on some of these fragments suggest the possibility of their being chips of some shells.

5.2.3 Variation of Modal Composition with Grain Size

An examination of Table 5.1 reveals significant trends in variation of amount of different modes with grain size. The percentages of quartz and K-feldspar tend to decrease with decrease in grain size, whereas plagioclase feldspars and chacite tend to occur in higher proportions in smaller sizes. The amount of chert varies irregularly with grain size.

5.2.4 Areal Variation of Constituent Modes

The samples selected for petrographic study are from widely separated localities. These samples can thus be analyzed to see the homogeneity of composition of sands in the area under investigation. For this purpose +120 mesh fractions of all the samples have been compared using χ^2 (chi) test. Five modal classes i.e. quartz, chert, K-foldspar and plagioclase and 'others' are recognized for this purpose. The mean of all the samples is taken as the expected value for each of the modal classes. The statistic χ^2 is then calculated as

$$\mathbf{x}^{2} = \sum_{i=1}^{n} \frac{\left(O_{i} - E_{i} \right)^{2}}{E_{i}^{2}}$$

where 0_i and E_i are observed and expected frequencies of a particular modal class i, and n is the total number of modal classes. For details of x^2 -test, Dixon and Massey (1957, p.221) may be referred.

X values for different samples (Table 5.2) indicate that four samples differ from the average modal composition significantly and the other four samples seen to cone from a population with the average modal composition at 95% confidence level. Also an examination of the contribution of the various modes to total \mathbf{X}^2 for individual samples (Table 5.2) shows that the minimum variation is shown by quartz amount and the maximum variation is shown by plagioclase amount.

A valuable property of \mathbf{x}^2 is that the sum of n sample values is itself distinguished as chi square with n

Table 5.2- Comparison of light mineral constituents in +120 mesh fractions to determine whether they are all from the same population.

| Slide No. Light Mineral Constituents | | | | | | | | | |
|--|--|---|---|--|---|--|--|--|--|
| Slide No. | Quartz | Chert | K-felds- | nstituent Plagio- | Others | | | | |
| - | | | par | clase | otners | | | | |
| (a) <u>Observ</u> | ed Freque | ncies | | · · · · · · · · · · · · · · · · · · · | alignes - y - months restored and the - y - ry - y - ay - y - y - y - y - y | | | | |
| 5/120 | 62.69 | 12.05 | 1.45 | 13.50 | 10.3 | | | | |
| 24/120 | 57.64 | 18.51 | 7.53 | 3.17 | 12.74 | | | | |
| 33/120 | 58.85 | 17.71 | 1.71 | 7.43 | 14.29 | | | | |
| 38/120 | 55.56 | 9.66 | 3.86 | 19.81 | 11.11 | | | | |
| 42/120 | 70.81 | 4.97 | 3.11 | 14.29 | 6.83 | | | | |
| 57/120 | 58.99 | 2.25 | 3.53 | 27.53 | 7.31 | | | | |
| 67/120 | 60.98 | 9.76 | 3.66 | 17.07 | 8.54 | | | | |
| 77/120 | 68.75 | 5.62 | 12.50 | 5.62 | 7.50 | | | | |
| Total | 494.17 | 80.53 | 38.15 | 108.42 | . 78.62 | | | | |
| Mean/ Expected | 61.77 | 10.07 | 4.77 | 13.55 | 9.83 | | | | |
| (b) Contrib | (b) Contributions to Criterion $(0_i - E_i)^2 / E_i = x^2$ | | | | | | | | |
| | | | Maximum | | 0 | | | | |
| E /200 | 0.07 | | | The second s | Total X ² | | | | |
| 5/120 | 0.01 | 0.39 | 2.31 | 0.00 | 0 | | | | |
| 24/120 | 0.28 | 0.39 7.07 | 2.31 2.09 | 0.00 | Total X ² | | | | |
| 24/120 33/120 | 0.28 0.05 | | | | Total X ² 0.02 2.73NS | | | | |
| 24/120 33/120 38/120 | 0.28 | 7.07 | 2.09 | 7.95 | Total X ² 0.02 2.73NS 0.86 18.25x | | | | |
| 24/120 33/120 38/120 42/120 | 0.28 0.05 | 7.07 | 2.09 1.96 | 7.95 2.76 | Total X ² 0.02 2.73NS 0.86 18.25x 2.02 12.59x | | | | |
| 24/120 33/120 38/120 42/120 57/120 | 0.28 0.05 0.10 | 7.07 5.80 0.02 | 2.09 1.96 0.17 | 7.95 2.76 2.89 | Total X ² 0.02 2.73NS 0.86 18.25x 2.02 12.59x 0.17 3.35x | | | | |
| 24/120 33/120 38/120 42/120 57/120 67/120 | 0.28 0.05 0.10 0.15 | 7.07 5.80 0.02 2.58 | 2.09 1.96 0.17 0.58 | 7.95 2.76 2.89 0.04 | Total X ² 0.02 2.73NS 0.86 18.25x 2.02 12.59x 0.17 3.35x 0.92 4.27NS 0.64 21.80x | | | | |
| 24/120 33/120 38/120 42/120 57/120 | 0.28 0.05 0.10 0.15 0.50 | 7.07 5.80 0.02 2.58 6.07 | 2.09 1.96 0.17 0.58 0.15 | 7.95 2.76 2.89 0.04 14.44 | Total X ² 0.02 2.73NS 0.86 18.25x 2.02 12.59x 0.17 3.35x 0.92 4.27NS | | | | |
| 24/120 33/120 38/120 42/120 57/120 67/120 | 0.28 0.05 0.10 0.15 0.50 0.01 | 7.07 5.80 0.02 2.58 6.07 0.01 | 2.09 1.96 0.17 0.58 0.15 0.26 | 7.95 2.76 2.89 0.04 14.44 0.91 | Total X ² 0.02 2.73NS 0.86 18.25x 2.02 12.59x 0.17 3.35x 0.92 4.27NS 0.64 21.80x 0.17 1.36NS 0.55 19.80x | | | | |
| 24/120 33/120 38/120 42/120 57/120 67/120 | 0.28 0.05 0.10 0.15 0.50 0.01 0.11 NS- Not | 7.07 5.80 0.02 2.58 6.07 0.01 1.97 signifi | 2.09 1.96 0.17 0.58 0.15 0.26 12.53 | 7.95 2.76 2.89 0.04 14.44 0.91 4.64 | Total X ² 0.02 2.73NS 0.86 18.25x 2.02 12.59x 0.17 3.35x 0.92 4.27NS 0.64 21.80x 0.17 1.36NS | | | | |
| 24/120 33/120 38/120 42/120 57/120 67/120 | 0.28 0.05 0.10 0.15 0.50 0.01 0.11 NS- Not x- Sign | 7.07 5.80 0.02 2.58 6.07 0.01 1.97 signifi | 2.09 1.96 0.17 0.58 0.15 0.26 12.53 cant at α | 7.95 2.76 2.89 0.04 14.44 0.91 4.64 | Total X ² 0.02 2.73NS 0.86 18.25x 2.02 12.59x 0.17 3.35x 0.92 4.27NS 0.64 21.80x 0.17 1.36NS 0.55 19.80x | | | | |
| 24/120 33/120 38/120 42/120 57/120 67/120 | 0.28 0.05 0.10 0.15 0.50 0.01 0.11 NS- Not x- Sign | 7.07 5.80 0.02 2.58 6.07 0.01 1.97 signifi | 2.09 1.96 0.17 0.58 0.15 0.26 12.53 cant at α | 7.95 2.76 2.89 0.04 14.44 0.91 4.64 | Total X ² 0.02 2.73NS 0.86 18.25x 2.02 12.59x 0.17 3.35x 0.92 4.27NS 0.64 21.80x 0.17 1.36NS 0.55 19.80x | | | | |

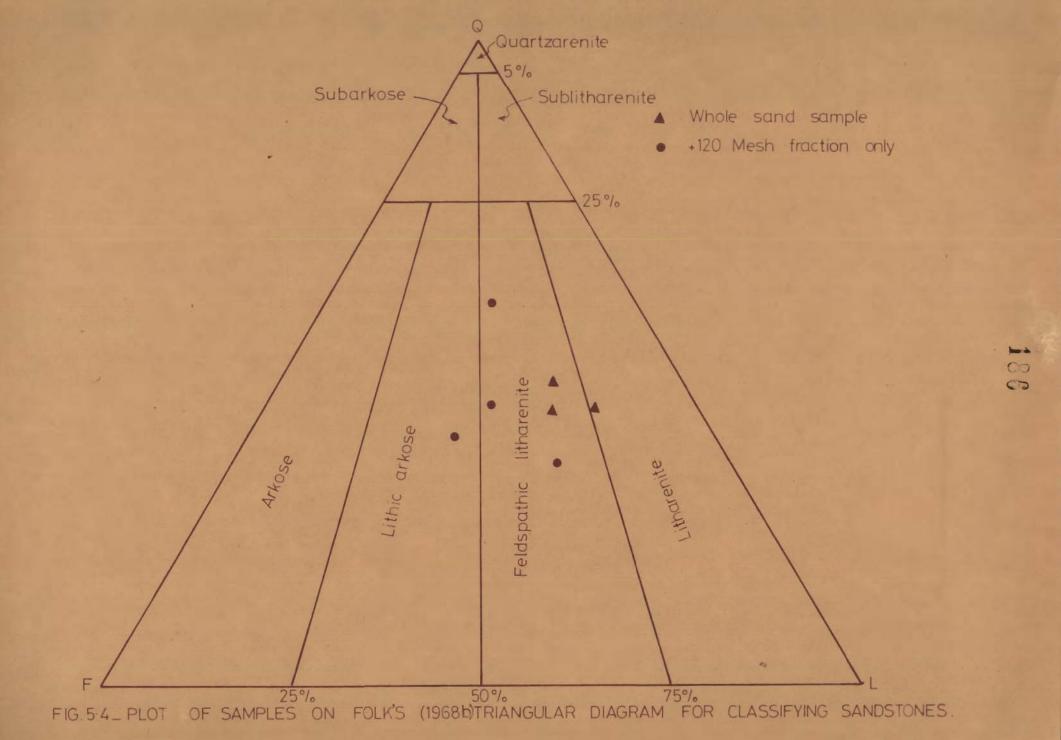
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degrees of freedom (Snedecor, 1956, p.213). Thus \mathbf{X}^2 values of different samples can be added and tested for 'homogeneity'. Cumulative \mathbf{X}^2 for all the samples is also significant at 5% significance level, suggesting that the samples belong to a 'heterogeneous' population.

Large scale transport of sand by wind over long distances should tend to result in a certain amount of uniformity of mineral composition of the sediments especially in the saltation loads. However, highly significant differences in the composition of saltation load of sediments (+120 mesh fraction) from different localities suggest that the wind is reworking the local sediments and cumulative sediment transport by wind is very small. Of course, it is realized that slight changes in composition of sediments could be introduced due to abrasion effects of wind. Incidentally, it should be interesting to determine the distances over which wind is able to bring about uniformity of sediment transport.

5.2.5 Classification of Sands

Folk's (1968b, in Blatt et al. 1972, p.311) triangle for classifying sandstones (Fig. 5.4) on the basis of detrital modes with slight modification is used here for categorizing the sands under study. The three end-members Q, F and L representing the three ends of the triangle



are Q-monocrystalline quartz, F-feldspars and L-rock fragments, chert and polycrystalline quartz. Following Dickinson (1970), chert and polycrystalline quartz are included with rock fragments instead of combining with Q as suggested by Folk (1968b)so as to emphasize the aspects of provenance. According to this classification most of the whole sand samples and +120 mesh fractions fall in feldspathic-litharenite class suggesting the importance of plutonic and metamorphic rocks with preponderance of the latter as provenance of these sands.

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5.3 HEAVY MINERALS

5.3.1 Method of Study

Since sands are coated with ferruginous naterial, the desired grain size fraction of the sands are first boiled with dilute hydrochloric acid. Then heavy mineral fraction is separated using bromoform in a separating funnel. The heavy minerals are mounted on slides with Canada balsam and about 200 grains are counted to determine the relative abundance of different minerals by studying all the minerals in four or five fields of view.

Four fractions i.e. +120, +170, +230 mesh and pan fractions of two samples with numbers 24 and 77 and +230 mesh fractions of other six with numbers 32, 33, 38, 42, 46 and 57, are studied in the manner described above. The data are given in Table 5.3 and are represented in the form of histograms in Figures 5.5 - 5.6.

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5.3.2 Description of Heavy Minerals

Hornblende, zircon, staurolite, kyanite, sphene, sillinanite and andalusite are the major nonopaque heavy minerals. Monazite is observed only in sample 24. A brief description of these minerals is attempted below.

5.3.2.1 Hornblende

Hornblende is the nost abundant heavy mineral and its percentage varies from 22.8 to 43.7. Most of the grains are subrounded but some elongated fragments are also noticed. Many grains show development of schiller structure. Some grains are pitted and have fractures.

The body colour of hornblende is green, but some samples contain a few brown hornblende grains. Also green hornblende grains show uneven colour distribution, deepest in the centre becoming paler towards the peripheries. Green hornblende is strongly pleochroic, from bottle green to pale yellow colour. Brown hornblende is also strongly pleochroic and the colour varies from golden yellow to brown.

Extinction angles, when neasured with crystal boundaries (cleavage being indistinct) for green hornblende range from 5° to 15° . Brown hornblende shows higher extinction angles of 20° to 22° .

| Sample No. | Hornbl- ende | Kyanite | Stauro- lite | Sillin- anite and and- alusite | Zircon | Tour- nal- ine | Rutile | Sphene | Monazite | Opaques | |
|---------------|-----------------|---------|-----------------|---|--------|----------------------|--------|--------|----------|---------|---------|
| 24/120 | 30.8 | 0.5 | - | - | 22.1 | K28 | 8.1 | 2.2 | 4.3 | 31.9 | |
| 24/170 | 22.8 | 3.5 | - | - | 23.7 | | 14.1 | 3.0 | 6.1 | 21.7 | |
| 24/230 | 36.7 | 1.7 | 3.3 | - | 13.9 | | 11.1 | 2.8 | 6.1 | 24.4 | |
| 24/PF | 50.6 | 2.4 | 1.8 | 0.6 | 16.5 | *** | 2.9 | 3.5 | 2.9 | 18.8 | |
| 77/120 | 26.7 | 1.6 | 11.2 | - | 9.6 | 0.5 | 6.4 | 7.0 | - | 36.9 | |
| 77/170 | 27.4 | 1.6 | 15.6 | | 18.3 | - | 9.1 | 2.7 | - | 25.3 | hare be |
| 77/230 | 37.6 | 2.1 | 3.1 | 1.5 | 10.8 | 1.0 | 4.1 | 10.8 | | 28.9 | 00 |
| 77/PF | 42.9 | 1.1 | 14.3 | 0.6 | 14.9 | | 5.1 | 7.4 | - | 13.7 | 60 |
| 32/230 | 42.3 | 1.2 | 9.5 | 1.2 | 13.7 | - | 5.4 | 4.8 | - | 22.0 | |
| 33/230 | 34.7 | 2.3 | 2.3 | 9.2 | 10.4 | - | 4.0 | 16.8 | | 19.7 | |
| 38/230 | 26.4 | 1.9 | 1.9 | 6.9 | 12.6 | 1.3 | 5.0 | 15.1 | - | 30.2 | |
| 42/230 | 41.3 | 4.2 | 8.4 | 1.2 | 12.0 | - | 4.8 | 8.4 | - | 19.8 | |
| 46/230 | 34.8 | 1.7 | 1.1 | 6.1 | 9.9 | 0.6 | 6.1 | 13.3 | - | 26.5 | |
| 57/230 | 43.7 | 3.2 | 10.3 | 2.2 | 11.3 | - | 9.2 | 4.9 | - | 15.1 | |
| | | | | | | | | | | | |

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Table 5.3 - Percentages of different minerals in heavy mineral fractions

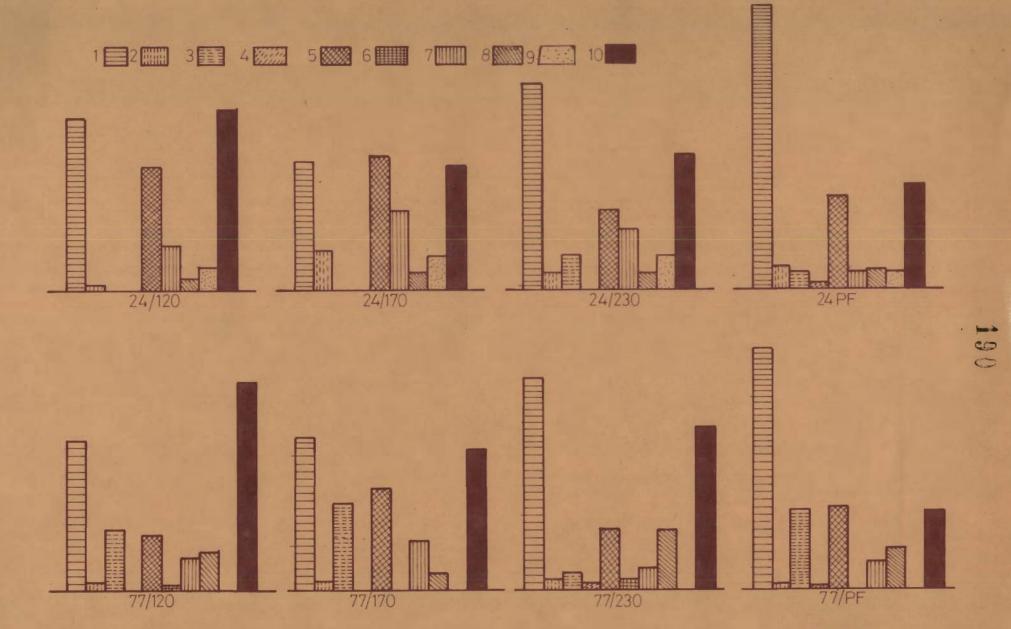


FIG. 5.5_ HISTOGRAMS SHOWING DISTRIBUTIONS OF HEAVY MINERALS IN DIFFERENT SIZE FRACTIONS OF SAMPLES 24 AND 77. 1_HORNBLENDE,2_KYANITE, 3.STAUROLITE,4_SILLIMANITE & ANDALUSITE, 5_ZIRCON, 6_TOURMALINE,7_RUTILE, 8_SPHENE,9_MONAZITE, AND 10_OPAQUES.

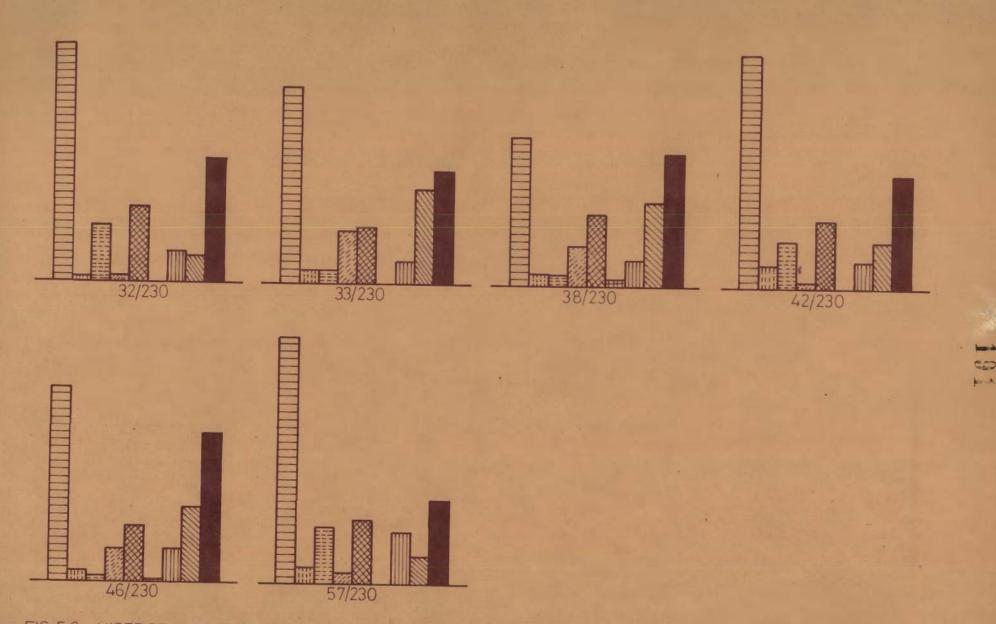


FIG 5:6_ HISTRGRAMS SHOWING DISTRIBUTIONS OF HEAVY MINERALS IN SAMPLES FROM DIFFERENT LOCATIONS. SYMBOLS ARE THE SAME AS IN FIGURE 5:5.

Many grains show alteration to iron oxides especially along cleavage planes or fractures. Some grains show sharp edges probably due to splitting. Inclusions of iron oxides and apatite are not uncommon.

5.3.2.2 Kyanite

Kyanite grains show uneven surface due to flaking. It has a very high refractive index. Extinction angle is low and varies from 5° to 8° . One grain shows inclusions of rutile. Grains show partings which are at right angles to the grain elongation.

5.3.2.3 Staurolite

Amount of staurolite varies from 1.1 to 15.6%. Staurolite shows considerable variation in form and habit. Most of the grains are short and stumpy and others exhibit irregular platy forms with distinct cleavage and fractures. It has pleochroic colours from pale yellow to golden yellow.

5.3.2.4 Sphene

A few grains of sphene are always present in all the slides. It occurs as irregular or slightly rounded grains, whereas a few euhedral, diamond shaped grains are also noticed in some slides showing brown to brownish yellow colour with very high index of refraction under cross nicols. It never shows complete extinction

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due to high dispersion. Some grains are marked by a network of fractures which criss-cross the grain.

5.3.2.5 Rutile

Rutile occurs as either euhedral, slightly rounded or even anhedral prismatic grains with characteristic foxy red or reddish brown colour. It shows strong pleochroisn from weak brown to reddish brown colour. Grains are often fractured. In case of many prismatic grains, parallel striations which run more or less obliquely to the prism boundary are observed.

5.3.2.6 Other Minerals

Grains of .nonopaque minerals such as actinolite, sillimanite, and alusite and tournaline are also noticed. These occur in very subordinate amounts. Also a fairly large amount of opaque minerals are recorded.

Similar heavy mineral assemblage has been reported from the aeolian sands of Barner district by Rao (1962).

5.3.3 Areal Variation of Heavy Mineral Frequencies

Heavy mineral frequencies of +230 mesh fractions of different samples are compared with the values for the mean of all these samples, using χ^2 test as described earlier. Seven classes i.e. hornblende, staurolite, kyanite, sillimanite, zircon, rutile, sphene and 'others' are recognized for this purpose. Calculations are shown in Table 5.4.

The analysis brings out the fact that the maximum variation is shown by staurolite, sphene and rutle frequencies. Five samples are not different from the average value whereas other three are considerably different from the average value at 5% significance level suggesting that there is probably higher uniformity in heavy mineral frequencies of samples than light mineral frequencies. These samples belong to a "heterogeneous" population as indicated by sum of χ^2 for all the slides. Only sample 33 shows strong deviations from average values for both light and heavy minerals. Other slides showing significant difference from the average heavy mineral frequencies are 24/230 and 57/230, but these samples show similar light mineral composition as the average of +120 mesh fractions of all the samples are this stage.

5.4 PROVENANCE OF THE AEOLIAN SANDS

The presence of heavy minerals like spherical and elongated hornblendes and zircons and staurolite, sillimanite, kyanite, andalusite and mongzite suggest a dominant low to high rank metamorphic rocks and a minor plutonic rock source for these sands. Light mineral composition and relative abundance of different types of quartz give a similar provenance. Table 5.4- Comparison of heavy mineral frequencies in +230 mesh fractions to determine whether they are all from the same population

| · | | | | | | | | |
|--|-----------------|-----------------|---|--------|--------|--|---|----------|
| Slide No. | Hornb- 1ende | Staur- olite | Kyanite + Sillin- anite + Andalusite | Zircon | Rutile | Sphene | Others | * * ** |
| (a) <u>Obse</u> | rved Fr | cquenci | les | | | an a | 1999 - 1999 - 1999 - 1999 - 1999 - 1999 - 1999 - 1999 - 1999 - 1999 - 1999 - 1999 - 1999 - 1999 - 1999 - 1999 - | а. — тур |
| 24/230 | 36.7 | 3.3 | 1.7 | 13.9 | 11.1 | 2.8 | 30.5 | |
| 32/230 | 42.3 | 5.5 | 2.4 | 13.7 | 5.4 | 4.8 | 22.0 | |
| 33/230 | 34.7 | 2.3 | 11.5 | 10.4 | 4.0 | 16.8 | 19.7 | |
| 38/230 | 26.4 | 1.9 | 8.8 | 12.6 | 5.0 | 15.1 | 31.3 | |
| 42/230 | 41.3 | 8.4 | 5.4 | 12.0 | 4.8 | 8.4 | 19.8 | |
| 46/230 | 34.8 | 1.1 | 7.8 | 9.9 | | 13.3 | 27.1 | |
| 57/230 | 43.7 | 10.3 | 5.4 | 11.3 | 9.2 | 4.9 | 15.1 | |
| 77/230 | 37.6 | 3.1 | 3.6 | 10.8 | | 10.8 | 29.5 | |
| Total | 297.5 | 39.9 | 46.6 | 94.6 | | | 195.6 | |
| Mean | 37.2 | 5.0 | 5.8 | 11.8 | 6.2 | 9.6 | 24.5 | |
| (b) Contributions to Criterion $(0_i - E_i)^2 / E_i = x^2$ | | | | | | | | |
| | | | | i 'i'' | i · | | 0 | |
| | | | | | | | | χ^2 |
| 24/230 | 0.01 | 0.58 | 2.90 | 0.37 | 3.87 | 4.82 | 1:47 14. | .02x |
| 32/230 | 0.70 | 4.05 | 1.55 | 0.31 | 0.10 | 2.40 | | SONS |
| 33/230 | 0.17 | 1.46 | 5.60 | 0.17 | 0.78 | 5.40 | 0.54 14. | |
| 38/230 | 3.14 | 1.92 | 1.55 | 0.05 | 0.23 | 3.15 | 1.89 11. | |
| 42/230 | 0.45 | 2.31 | 0.03 | 0.00 | 0.32 | 0.15 | | 16NS |
| 46/230 | 0.15 | 3.04 | 0.69 | 0.31 | 0.00 | | | SOME |
| 57/230 | 1.14 | 5.62 | 0.03 | 0.02 | 1.45 | | 3.61 14. | |
| 77/230 | 0.00 | 0.72 | 0.83 | 0.08 | 0.71 | | | 68NS |
| | | | | | | | | |

78.19

x Significant at $\alpha = 0.05$ NS Not significant $\alpha = 0.05$ \mathbf{X}^2 6, 0.95 = 12.59 \mathbf{X}^2 8, 0.95 = 15.51 The presence of chert, however; points to some contribution from sedimentary rocks also.

Comparison of light minerals of +120 mesh fractions and heavy minerals of +230 mesh fractions of samples from different areas using X^2 test suggest that samples have significantly different composition from each other and they belong to a 'heterogeneous' population. Thus it seems that probably the older deposits with areally varying composition are being reworked by the wind and as such are not transported over long distances. Acgarding the desert expansion, it may be said here that it occurs either due to alteration of climatic conditions, massive transport of sediments engulfing the bordering fertile lands or due to reworking of older deposits under the influence of excessive deforestation and land use. Since there is no approciable change in the climatic conditions of the Thar desort and its bordering regions, nor there is large scale sediment transport, there should not be any cause of alarm of desert expansion particularly so when the conservation of forests and proper land use methods are adopted.

Gupta (1958) considers that sands of the Thar desert are probably derived from the beaches of pre-existing seas in the area. Wadia (1966, p.53) also finds that these sands are indistinguishable from sands of the seashore and remarks that these have been derived mostly from the Rann of Kutch and partly from the basin of the lower Indus. Ghosh's (1964) investigations reveal that most of the desert sands have

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roundness similar to that of the sands of old flood plains having more rounded quartz grains than the piedmont apron sediments. He maintains that the origin of the sands of the western Rajasthan is mainly due to reworking by aeolian cycle of earlier alluvial deposits.

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Usually the shoreline sediments are poor in fines, whereas the flood plains of rivers contain plenty of them along levees, in the flood basin and in ox-bow lakes. The presence of high percentage of fines in the Thar desert sediments as mentioned in section 4.2.12 and significant changes in their composition from place to place suggest their derivation from earlier alluvial deposits after reworking by the wind. In fact, sediments of most of the large deserts in the world have been considered to be derived from the loose alluvial deposits of the Pleistocene times (Madigan, 1946; Holm, 1960; Alimen, 1965; Smith, 1965).

CHAPTER-6

ENGINEERING PROPERTIES

6.1 INTRODUCTION

The use of soil as an engineering material and its behaviour towards various civil engineering structures forms an interesting field of study which demands a detailed investigation of its various engineering properties such as shear strength, permeability, compaction and mortar making property.

The area of the Thar desert under study is a virgin area and has much potential for future development, particularly from defence and traction points of view due to its strategic location near the international border. Therefore, the importance of such geotechnical investigations is selfevident. Also, there is a need to classify the desert soils according to their engineering properties.

These studies may be of use in the following civil engineering construction works:

(i) Foundation design of various structures like buildings, bridges, tunnels, canals etc,

(ii) Flexible or rigid pavenent design and the suitability of the soil as construction material for building highways, airports, railways, earthfills or cuts etcand

(iii) The design of subterranian and earth retaining

structures such as underground buildings, drainage structures, pipe lines, anchored bulk-head, coffer dans etc.

6.2 LABORATORY INVESTIGATIONS

The sands of the area have been subjected to laboratory investigations to determine the following engineering properties:

- (i) Mortar Compressive Strength,
- (ii) Compaction,
- (iii) Shear Strength and
- (iv) Permeability.

6.2.1 Mortar Conpressive Strength

The compressive strength of sand cement mortar is one of the most important properties to determine the suitability of sand for use as one of the constituents in the structural concrete - both reinforced and plain. Six representative sand samples from Sam (sample 20), Dhanana (samples25 and 32), Murar (sample 34), Ramgarh (sample 38) and Lunar (sample 77) are used to determine the mortar compressive strength using ordinary ACC Portland Cement with the properties given in Table 6.1.

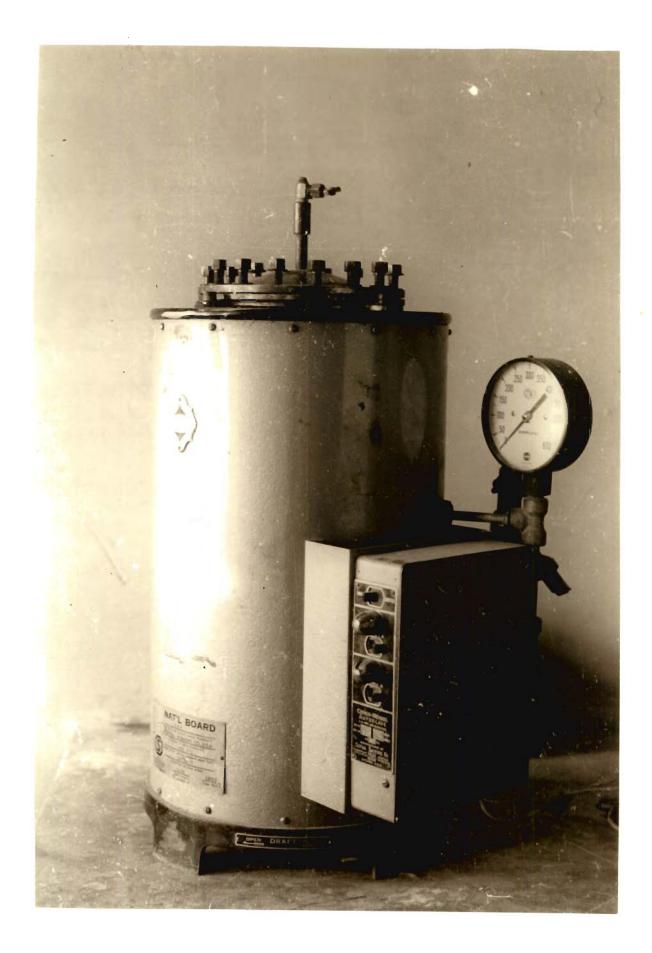
The cenent sand cubes were prepared by mixing the two in the proportions of 1:3. The water cenent ratio has been kept as 0.4. Five cubes of 2.54 cm size were prepared from each sand sample. The cube moulds are filled with mortar in two layers and each layer was compacted thoroughly by hand.

| Normal consistency-water in per cent of cement by weight. | • | 26% | Values specified by Indian Standard (Anon., 1967) |
|---|-----------|------|---|
| Setting time in mts | Initial | . 90 | ≮ 30 |
| Compressive strength in | Final | 300 | ≯ 600 |
| sand mortar (with single | at 3 days | 200 | ≮115 |
| sized sand) | at 7 days | 300 | ≮ ¹⁷⁵ |

Table 6.1- Properties of ACC Portland Cement

These noulds were then kept in the constant temperature and humidity chamber for 24 hours. The temperature of the chamber was controlled at (27 ± 2) ^oC and relative humidity at (50 ± 5) %. The curing of concrete products can be accelerated easily by placing them in a chamber at elevated temperatures. It is, however, essential that the atmosphere should be damp to prevent drying of the product. Therefore, stean heating is a convenient way of curing. High pressure stean curing has an additional advantage of giving very high strength in a considerably short time.

The cubes were denoulded and kept in the autoclave (Fig.6.1) for high pressure stean curing. The autoclave temperature was raised to boiling point. After keeping it boiling for a few minutes to allow for the escape of air, the escape value is closed and the pressure allowed to rise to Fig. 6.1_ Autoclave for high pressure steam curing.

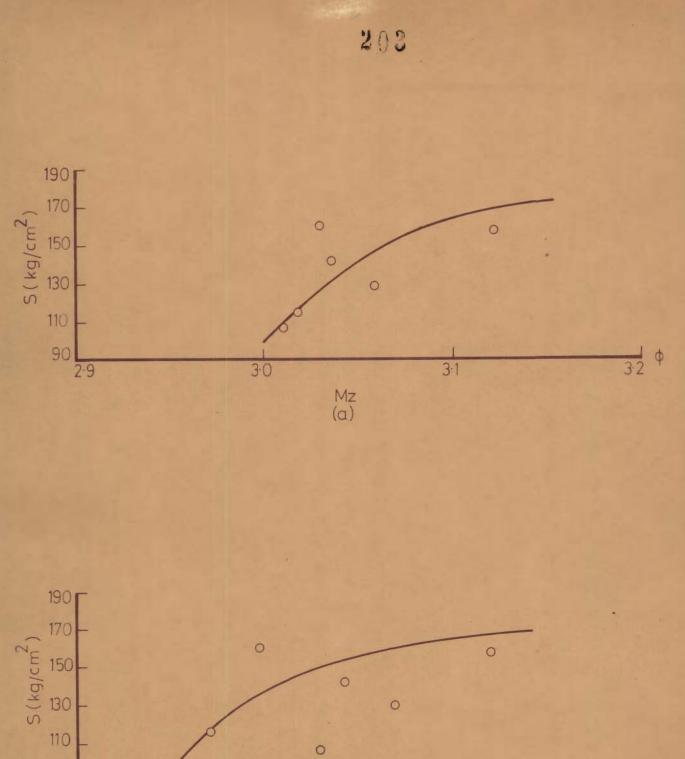


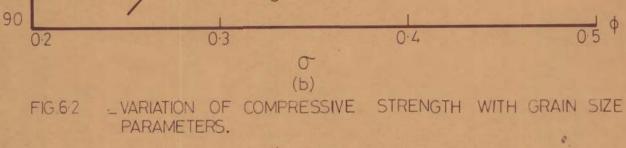
8.44 kg/cm² (120 psi gauge) which was maintained for 12 hours. This curing time gives strength corresponding to one year's strength of normal curing at standard conditions of temperature and humidity. After this the contents were cooled slowly in four hours and were taken out of the autoclave. These cubes were then tested in the Universal Testing Machine of 5 tonne capacity. The compressive strength data so obtained has been correlated with grain size parameters Mz, σ , Sk and Ku as shown in Figure 6.2.

The compressive strength increases from 99 to 174 kg/cm² as Mz increases from 3.00 to 3.150 (Fig.6.2a). This may be due to increase in the surface area of the particles. Similarly the variation in the sorting coefficient σ also has significant effect on the compressive strength. As is evident from the curve (Fig.6.2b), compressive strength increases from 99 to 168 kg/cm² with the increase of σ from 0.25 to 0.440.

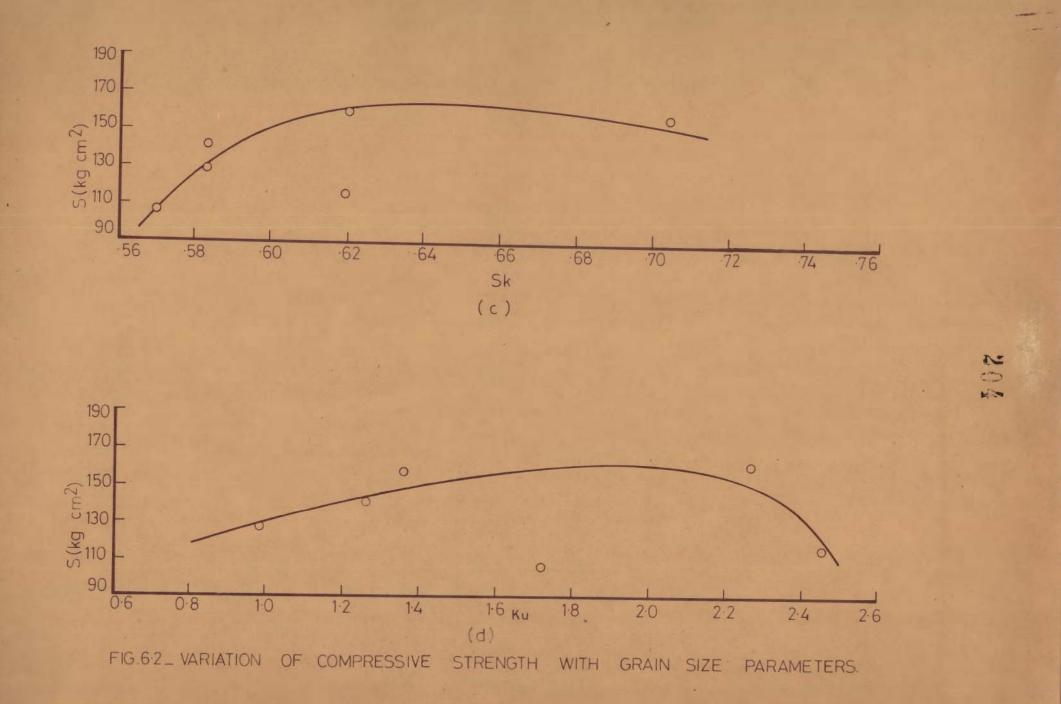
The effect of variation in skewness on compressive strength is somewhat different than that of Mz and σ . It can be noted from Figure 6.2c that as skewness increases from 0.57 to 0.64 the compressive strength also increases from 106 to 166 kg/cm². With further increase in the skewness from 0.64 to 0.71 the compressive strength decreases gradually from 166 to 150 kg/cm². Kurtosis too has sinilar effect on the compressive strength as seen in Figure 6.2d. The compressive strength increases from 118

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q



to 160 kg/cm^2 with the increase of kurtosis from 0.8 to 2.0. Thereafter, any increase in Ku causes a decrease in the compressive strength. As evident from the curve there is a fall in compressive strength from 160 to 110 kg/cm² with an increase in Ku from 2.0 to 2.5.

With a view to compare these results with the findings of other investigators, the nortar strength literature has been surveyed. Unfortunately, it appears that no worker has correlated nortar strength with grain size parameters employed in this study. Therefore, no comparison could be made.

6.2.2 Compaction

The compaction of soil can be defined as the process of packing soil particles closely together by mechanical treatment thereby increasing the dry density of soil. In the present investigation the standard Proctor test has been used to study the compaction which is measured quantitatively in terms of dry density to which a soil sample can be compacted. The dry density γ_d for the compacted soil is calculated from the following equation,

$$\gamma_d = \frac{W}{V(1+w)} \qquad \dots \qquad (6.1)$$

where W is the weight of wet compacted specinen, w the water content and V the volume of the mould.

The test is repeated on soil samples with increasing water contents (12%, 15%, 18% and 21%) and corresponding

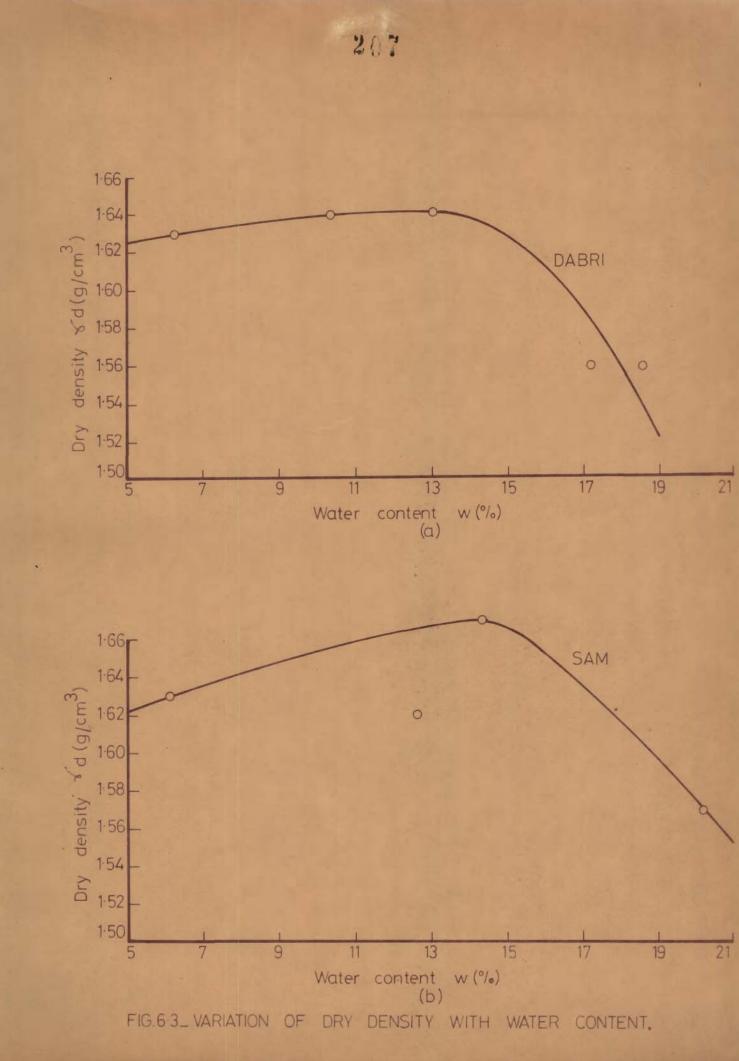
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dry densities γ_d obtained. A compaction curve is plotted between the water content as abscissa and dry density as ordinate.

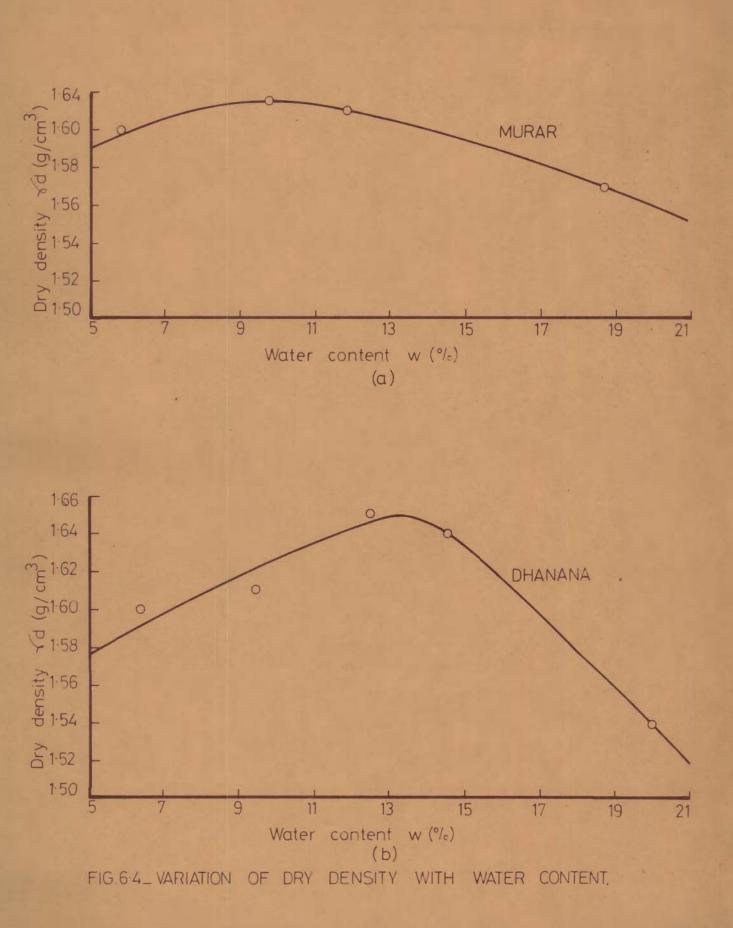
The standard Proctor test has been carried out on representative samples collected from six localities of the area namely, Dabri (sample A), San (sample B), Murar (sample C), Dhanana (sample D), Lunar (sample E) and Rangarh (sample F). The compaction curves for the above samples are discussed below. (i) Dabri - Near Dabri (Fig.6.3a), the maximum dry density obtained is 1.64 gm/cm³ at an optimum water content of 13.1%. The dry density at 6.3% water content is 1.63 gm/cm³ while at 15% the dry density decreases to a low value of 1.52 gm/cm³. (ii) Sam - In the Sam area (Fig.6.3b), the dry density increases from 1.63 gm/cm³ at 6% water content to maximum dry density of 1.67 gm/cm³ at the optimum water content of 14.4%. With further increase in water content the dry density rapidly declines to a value of 1.57 gm/cm³ at water content of 20.25%.

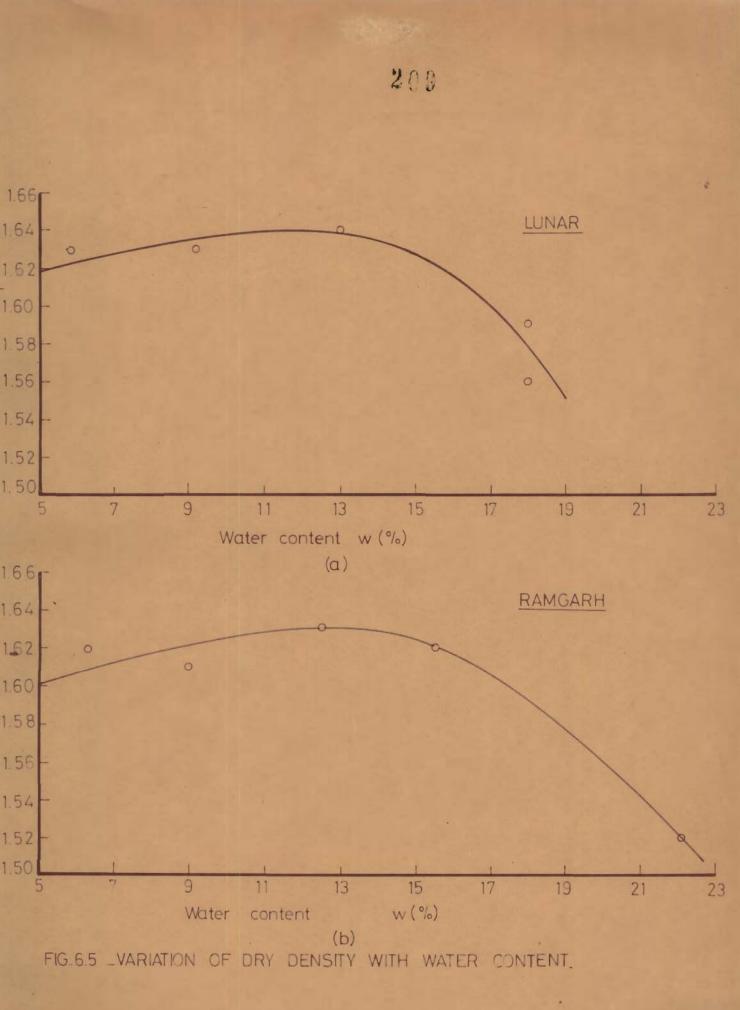
(iii) Murar - At Murar (Fig.6.4a), the maximum dry density obtained is 1.61 gm/cm³ at 9.8% water content, which is comparatively lower than those of above mentioned areas. The dry density is 1.59 gm/cm³ at 5% water content and it decreases to 1.55 gm/cm³ at 21% water content.

(iv) Dhanana - At Dhanana (Fig.6.4b), the dry density varies from 1.58 gm/cm^3 at 5% water content to a peak value of









1.65 gn/cm³ at 12% water content. It declines to 1.52 gn/cm³ at 21% water content.

(v) Lunar - At Lunar (Fig.6.5a), the dry density is 1.62 gm/cm^3 at 5% water content and attains a maximum value of 1.64 gm/cm^3 at 12% water content. It decreases to 1.55 gm/cm^3 at 15% of water content.

(vi) Ramgarh - Figure 6.5b is a curve representing variation of dry density near Ramgarh area. Here the dry density is 1.60 gm/cm^3 at 5% water content and attains a maximum value of 1.63 gm/cm^3 at 13% water content which falls to a low value of 1.52 gm/cm^3 at 22% of water content.

Table 6.2 summarises the values of maximum dry density $(\gamma_{d \text{ max}})$, the optimum moisture content (OMC) and the relevant grain size parameters. The variation of $\gamma_{d \text{ max}}$ has been correlated with the grain size variations of the samples from the six localities in Figure 6.6. It may be noted from Figure 6.6a that as Mz decreases from 2.89 to 3.1 \emptyset the value of $\gamma_{d \text{ max}}$. continuously decreases. Therefore, it is clearly indicated that larger the grain size the smaller the $\gamma_{d \text{ max}}$. Similarly, Figure 6.6b shows the variation in $\gamma_{d \text{ max}}$ with standard deviation σ of grain size. It may be observed that as σ value increases from 0.24 to 0.36 \emptyset the value of $\gamma_{d \text{ max}}$. decreases from 1.67 to 1.61 gm/cm³. This clearly indicates that poorer the sorting, lesser is the $\gamma_{d \text{ max}}$.

The range of $\gamma_{d\ max}$ and OMC values of the sand samples

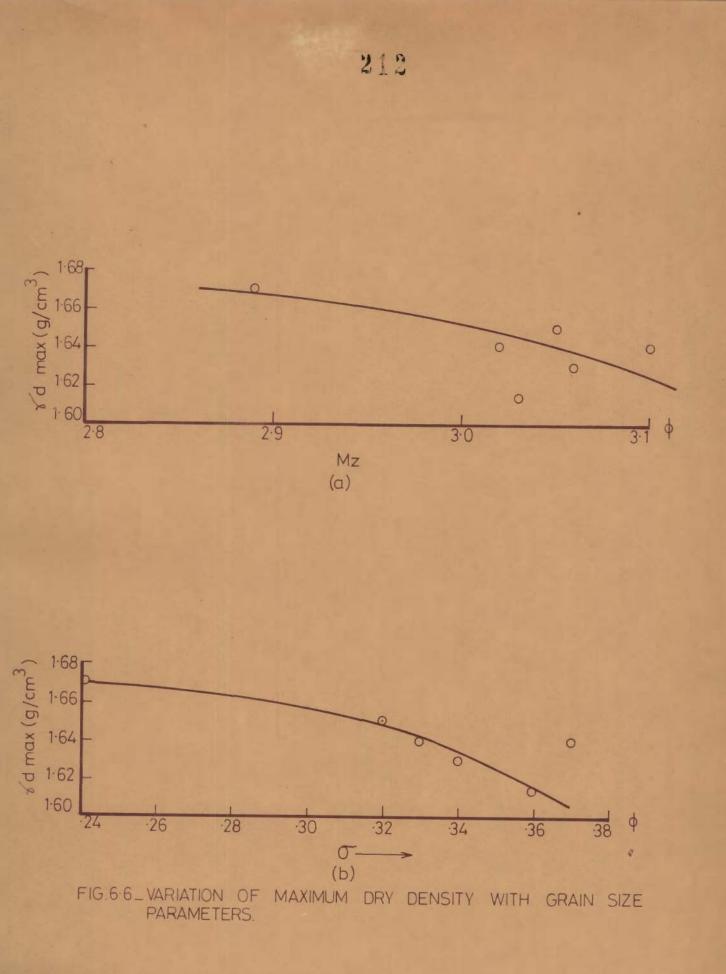
| Sample No. | Location | Grain Size Parameter | | Compa | ction | Permeability K |
|---------------|--|----------------------|-------|---------------------------------|---------|-----------------------|
| 110. | and the second | Mz (Ø) | σ (Ø) | Yd max (gm/cm ²) | OMC (%) | (cm/sec) |
| A | Dabri | 3.10 | 0.37 | l.64 | 13.1 | 0.33x10 ⁻³ |
| В | Sam | 2.89 | 0.24 | 1.67 | 14.4 | 0.86x10 ⁻³ |
| C | Murar | 3.03 | 0.36 | 1.61 | 12.0 | 0.31x10 ⁻³ |
| D | Dhanana | 3.05 | 0.32 | 1.65 | 12.0 | 0.55x10 ⁻³ |
| Ĩß | Lunar | 3.02 | 0.33 | 1.64 | 13.0 | 0.92x10-3 |
| \mathbf{F}' | Kangarh | 2.06 | 0.34 | 1.63 | 12.5 | 0.76x10 ⁻³ |

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Table 6.2 - Bulk sample data

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investigated fall almost in SW and SP groups of soil according to Unified Soil Classification System (Anon., 1962). To the awareness of the author, no investigation has been reported which correlates γ_d max. and OMC with grain size parameters employed in this study.

6.2.3 Shear Strength

The shear strength of the soil is its maximum resistance to shearing stresses. It is taken to be equal to the shear stress at failure on the failure surface. It consists of (i) internal friction, or the resistance due to interlocking of particles and friction between individual particles at their contact points, (ii) cohesion, or the resistance due to interparticle forces which tend to hold the particles together in a soil mass.

The shear strength τ of soil can be represented by Coulomb's equation:

 $\tau = C + \sigma_n \tan \phi_1 \qquad \dots \qquad (6.2)$

where σ_n is the normal stress on the failure plane, C the cohesion and ϕ_i the angle of internal friction.

The shear strength of the desert soil under consideration was determined by direct shear test in which the plane of shear failure is predetermined.

A graph is plotted between the normal stress σ_n as abscissa and shear strength τ as oridnate. The inclination to the horizontal of the strength envelope so obtained is the

angle of shearing resistance and the intercept on the ordinate is taken as cohesion.

Sand samples from Sam (samples 6 and 21), Dhanana (sample 31) and Lunar (sample 78) have been tested for shear strength. The results of these tests, in the form of $\tau vs.\sigma_n$ plots, are shown in Figures 6.7 and 6.8. The shear strength plot for sample 21 from Sam (Fig.6.7) shows that it has zero cohesion thereby indicating that clay content is almost absent. The equation of the plot comes out as $\tau = 0.606 \sigma_n$.

The sample 78 from Lunar (Fig.6.7) exhibits a cohesion of 0.145 kg/cm² thereby, indicating the presence of fines (-75 μ) in the sand sample. The equation of the τ vs. σ_n graph for Lunar sample comes out as $\tau = 0.110 + 0.450 \sigma_n$.

The sample 31 from Dhanana (Fig.6.8) again exhibits almost cohesionless nature of the sand. The equation of the graph is found as $\tau = 0.706 \sigma_{n}$.

The curve of the sample 6 from Sam (Fig.6.8) has the following relation:

 $\tau = 0.055 + 0.706 \sigma_n$.

The tan \not{p}_i values for the sand samples agree well with the range of values for SP and SW soil groups of Unified Soil Classification System (Anon., 1962).

6.2.4 Permeability

Permeability is defined as the property of a porous

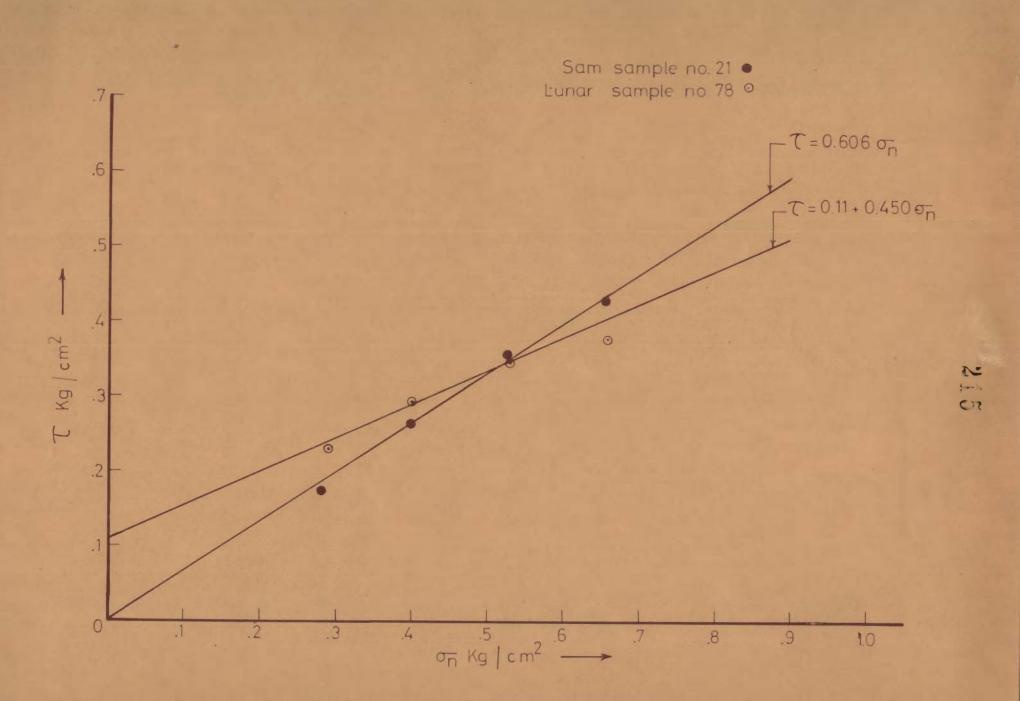


FIG.6.7_VARIATION OF SHEAR STRESS WITH NORMAL STRESS

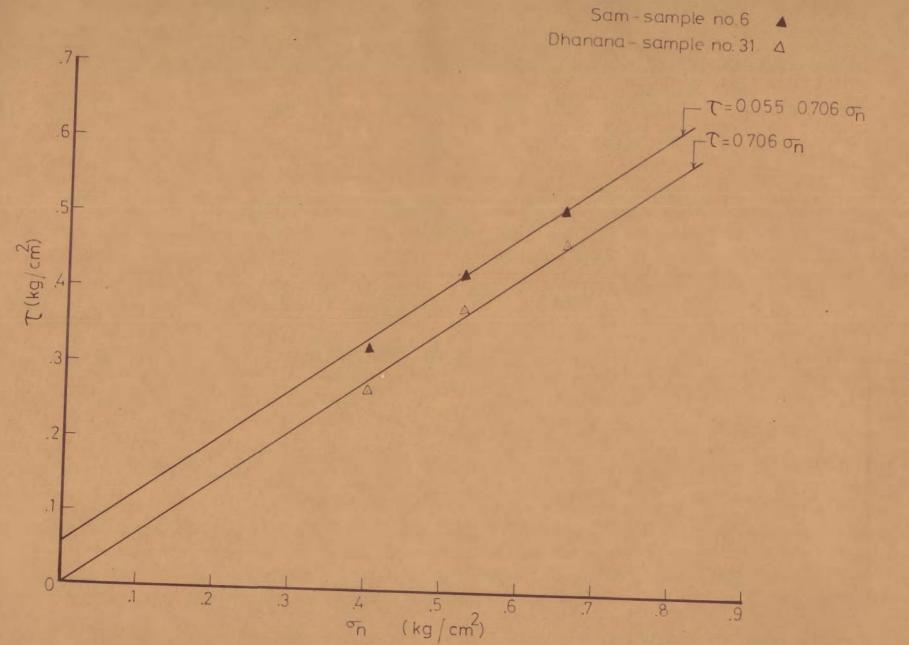


FIG.6.8 _ VARIATION OF SHEAR STRESS WITH NORMAL STRESS.

material which permits the seepage of water (or other fluids) through its interconnecting voids. A material having continuous voids is called permeable.

The study of seepage of water through soil is important for many engineering problems, for example, determination of rate of settlement, calculation of seepage through the body of earth dams and stability of slope, calculation of uplift pressure under the hydraulic structures and their safety against piping, ground water flow towards wells and drainage of soils etc.

The coefficient of permeability can be determined by constant head and falling head permeability tests in the laboratory, and by pumping-out and pumping-in tests in the field. For the permeability investigations of the sand samples of the present area falling head permeability test has been performed. In this test the water is allowed to flow through the soil sample and the time 't' taken for the water level to fall from a height h_1 to h_2 is noted.

If A is the cross-sectional area of the soil sample, 'a' the cross-sectional area of the stand pipe and L the length of the soil sample, then the permeability of the soil sample is given by the expression.

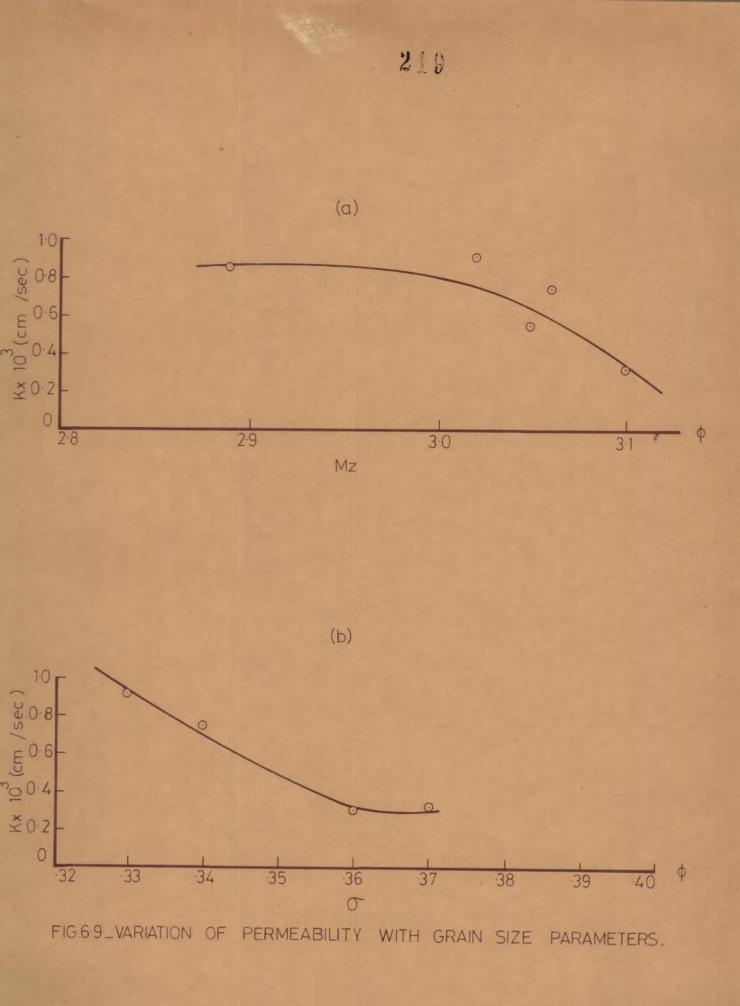
$$K = 2.303 \frac{a.L}{A.t} \log_{10}(\frac{h_1}{h_2})$$
 ... (6.3)

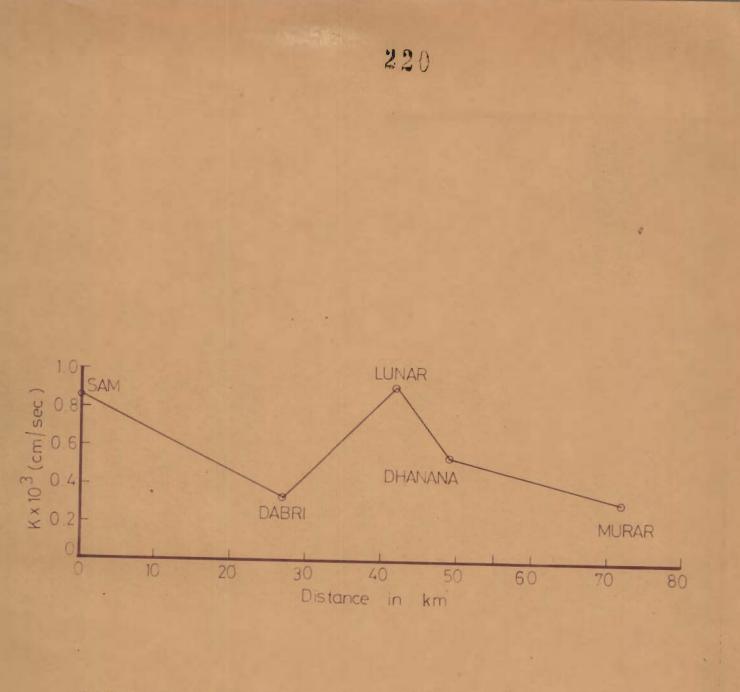
For the permeability determination , representative sand samples were collected from five localities of the area

namely, Dabri (sample A), Sam (sample B), Murar (sample C), Dhanana (sample D) and Lunar (sample E). Table 6.2 also includes the permeability results of these samples. The variation of permeability has been correlated with grain size parameters like Mz and sorting coefficient σ . It has been found (Fig.6.9a) that permeability decreases from a value of 0.86×10^{-3} to 0.33×10^{-3} cm/sec as Mz increases from 2.89 to 3.1Ø. Fhus, it is evident that larger grain size supports larger interstitial spaces resulting in higher permeability. From Figure 6.9b it is clearly seen that decrease in its value from 0.9×10^{-3} to 0.33×10^{-3} cm/sec with an increase of σ from 0.33 to 0.37Ø.

The above trends of decreasing permeability with increasing Mz and σ agree with the findings of Krumbein and Monk (1943) and Masch and Denny (1966). The values of permeability obtained correspond to the values of the soil group SP of the Unified Soil Classification (Anon., 1962).

A permeability traverse has also been prepared from the permeability test data as shown in Figure 6.10. As one proceeds from Sam to Dabri, the permeability decreases from 0.86×10^{-3} to 0.33×10^{-3} cm/sec while it again increases from Dabri to Iunar from 0.33×10^{-3} to 0.92×10^{-3} cm/sec. From Iunar to Dhanana, there is a continuous decrease in permeability from 0.92×10^{-3} to 0.55×10^{-3} cm/sec. Further, towards Murar the permeability decreases gradually from 0.55×10^{-3} to 0.31×10^{-3} cm/sec.





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FIG 6.10_VARIATION OF PERMEABILITY, WITH DISTANCE

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CHAPTER-7

SUMMARY AND CONCLUSIONS

7.1 SUMMARY

The Thar desert has remained neglected geologically perhaps due to the inhospitable terrain and the extreme climatic conditions. But lately the desert has come to prominence due to its strategic location and future potential for development, particularly with the advance of work on the Rajasthan canal. Considering this, together with the author's interest in the deserts, a type area, falling in latitudes $26^{\circ}30^{\circ}$ to $26^{\circ}52^{\circ}$ and longitudes $70^{\circ}0^{\circ}$ to $70^{\circ}33^{\circ}$, in district Jaisalmer has been selected for investigations. The present study embodies famy exhaustive and systematic sedimentological and geotechnical investigations of the sands of the area.

Climatically, the Thar desert can be referred to as a hot desert characterised by an annual rainfall of 25 cm or less and a mean diurnal range of temperature of 13.5° C or more. The relative humidity ranges between 50 to 60% in the morning hours and 25 to 35% in the afternoon hours whereas, summer relative humidity for the corresponding hours ranges between 35 to 60% and 10 to 30% respectively.

Regarding physiography, in a general way, the various features have largely been controlled by climate typical of a wind governed terrain. The sand cover may be a few meters thick, thin or absent altogether to bare the rocky surface. There appears to be a tendency of the sand cover to thicken in the west and southwest of the area where it is occupied by longitudinal dunes separated by more or less flat and comparatively firm interdune areas. The marginal fringe of the desert where the thickness of the sand is less, barchan dunes predominate.

A review of the literature indicates that mainly climatic conditions are responsible for the initiation, growth and maintenance of the world deserts. Arid conditions of the Thar desert are attributed to the location of the Himalayan, the Kirthar and the Suleiman mountain ranges including Tibetan plateau which induce low pressures over western India and central part of Pakistan. Atmospheric dust, recent tectonic movements resulting in change of river courses and global climatic changes also might be additional causes of aridity of the region.

Regarding the age of the Thar desert, it is suggested that it came into existence about 10,000 years back, when mainly longitudinal dunes and sand piles were formed. These were stabilised during the relatively humid and warm period of 10,000 to 3,000 years B.P. The area has been subjected to wind action again since 3,000 years B.P. with the advent of arid conditions to form active barchans, transverse dunes and some sand piles. Thus the present scenario of the area is a product of the superposition of the present wind regime over the fossil longitudinal dunes and sand piles. Three distinct types of bedforms are recognised in the area, namely, ripples, dunes and sand piles. Ripples are mostly asymmetrical, developed transverse to the dominant wind direction. Usually they are straight and parallel but at many places they show wavy strikes. Well developed branching of ripple is observed. When they branch, it is the crest line that bifurcates. Arcuate ripples tend to straighten out until they become more or less transverse to the dominant wind direction. Crests are composed of comparatively coarser grains than the troughs. Rarely, ripples of different wavelengths occur in juxtaposition, if the modality of the sand alters. Ripples are well developed on finer sands than on coarse ones.

Plots between the different ripple parameters show that ripple amplitude is proportional to the wavelength. The ripple index (λ/H) varies from 5 to 40 with a mean value of 20.1. Ripple index is minimum for a critical range of amplitude (0.45 to 0.55 cm) and it starts increasing with either increase or decrease of amplitude. Also, ripple index increases with the wavelength.

Three varieties of dunes, namely, barchans, transverse dunes and seifs are found in the area. Two families comprisi--ng active and stabilized barchans are noticed. Two morphologically distinct active barchans have been recognised. One, having a perfect crescentic shape and the other, which is reported for the first time, resembles a hat-shape. Both of these types have similar leeslopes but they differ in their windward slopes since the latter has a narrow trench which opens on both the flanks some distance down the crest line.

Mechanism of formation of barchans has been visualized to occur in three stages such as initiation or nucleation stage, youth stage and the old stage.

The occurrence of narrow (0.5 to 1 m wide) high angle band at the toe of the lee slope and the narrow trench on the windward slope of hat-shape barchan is attributed to lee.eddies and the newly reported windward eddies respectively.

Transverse dunes which are normal to the dominant wind direction, seem to originate by the lateral conjugation of two or more barchans, though their independent origin is not ruled out.

Longitudinal dunes are long, parallel, linear structures which are the dominant feature in the desert interior where sufficient sand supply is available. Their mean length is 8.8 km when measured between extreme ends. Many of them have 'Y' shaped bifurcations facing the wind direction. Their origin is attributed to the complex helicoidal wind circulations.

Sand piles may be thought as low stabilized longitudinal dunes which may be difficult to recognize in the field as linear structures. Orientation of different bedforms indicates N 25°E to N 30°E direction of net sediment transport. Both the stabilised and active dunes give similar sediment transport directions suggesting that the same wind regime has been prevailing since the formation of stabilised dune system. The 15°N divergence of net sediment transport direction from the resultant wind direction is attributed to the 'Ekman spiral' effect.

More than one hundred samples have been collected from the various bedforms and sand flats situated in different parts of the area. Samples are analysed using ASTM sieves at half phi intervals. Two instruments - sample splitter and transfer funnel-were designed and fabricated for quick analysis of samples. Sieve data are analyzed using IBM-1620 computer. Normal curves are fitted between the two adjacent points. Grain size parameters according to different workers are calculated.

A comparison of grain size parameters according to different workers shows that formulae of Krumbein and Pettijohn (1538) for skewness and kurtosis give very different results from those of others and these formulae should not be used for these sediments. But other formulae for the different grain size parameters give similar results. For detailed discussion, formulae of HcCammon (1962) for mean and standard deviation and those of Folk and Ward (1957) for skewness and kurtosis are taken into consideration. The average mean size for all the samples is 2.57 ϕ (0.13 mm) with a S-range (\pm one standard deviation) of 2.78 to 3.26 ϕ . Thus the Thar desert sediments lie on the finer side of dune sands reported earlier. The average standard deviation of all the samples is 0.37 ϕ with a S-range of 0.00 to 0.76 ϕ . A comparison of photomicrographs and cumulative frequency curves of typical samples brings out clearly that sorting in the present samples is a function of the ratio of mainly two populations.

Most of the samples studied are positively skewed with an average skewness of +0.50 and a 5-range of 0.28 to 0.78. Samples can be roughly divided into two groups with different kurtosis values. One group is very leptokurtic with kurtosis values between 1.7 and 2.45. The other group has platykurtic character with kurtosis values lying mainly between 0.0 and 0.8.

Study of interrelationship of the different grain size parameters brings out some interesting features. There is a significant relationship between the mean size and standard deviation and points fall around a line making an angle of about 45° with each of the axes. Standard deviation increases with decrease in mean size. Sediments become more positively skewed with decrease in mean size. These observations lead to a significant relationship between sorting and skewness. Kurtosis values tend to decrease with decrease in mean size but they seem to be independent of skewness. Comparison of the average size parameters between the various bedforms indicates that ripples are quic coarse grained, poorly sorted and nearly symmetrical in nature. Sand piles and dunes are distinguished by small but distinct differences in grain size parameters. The former are fine grained, poorly sorted and more positively skewed than the latter. Further, sand piles commonly tend to fall in platykurtic group whereas dunes, in general, tend to have leptokurtic nature.

Plots of normalized heights versus grain size parameters indicate that there is an increase in grain size, improvement in sorting and change from near symmetrical nature to higher positive skewness from the foot to the crest of the dune. No significant differences between samples from windward and leeward sides of barchans are observed.

Using values of grain size parameters from sand piles and dunes, contours are drawn to study their spatial variability. There is a mean grain size 'high' in an area southeast of Lunar. The same general area forms a 'low' for skewness and standard deviation values and a 'high' for kurtosis values. A'high' for mean grain size and similar related changes in other parameters are seen near Sam. The variation in grain size parameters in the Lunar area is thought to reflect areal grain size distribution of an older deposit which has been reworked by the wind. Changes in grain size parameters near Sam are probably a result of repeated

reworking of sand flats around Sam and piling of sediments into large mounds covered with dunes.

Evaluation of the various diagrams by different workers for discrimination of desert deposits from other types of deposits brings out that QDa-Md diagram of Buller and McManus (1972) is not particularly useful, whereas desert sediment field, delineated on Ska-QDa diagram of these workers should be widened to include samples of the Thar desert. Mean size versus standard deviation diagram of Friedman (1961) for distinction between desert and fluvial sediments and skewness versus mean size diagrams of Friedman (1961) and Moiola and Weiser (1968) for discriminating between beach, coastal dunes and inland dunes seem to be useful. Sahu's (1964) plot of $\sqrt{\sigma^2}$ vs. $\frac{s_{NZ}}{s_{NZ}} \cdot s_{(\sigma^2)}$ is very sensitive to the presence of extreme values of standard deviation and should be used with care for recognition of desert sediments.

The shape of cumulative curves, photomicrographs of the typical samples from the area and interrelationships of the grain size parameters suggest that sediments of the Thar desert consist mainly of two populations of grains mixed in different proportions, namely, a saltation population and a suspension population. The saltation population has a mean size of about 2.750 and a standard deviation of 0.200 and the suspension population has a mean size of about 3.750 and a standard deviation of about 0.250. The saltation

population constitutes 60-90% and the suspension population forms 10-40% of the samples. A minor amount of a traction population with grains coarser than 2.50 may constitute less than 1% of the samples. When the sediments consist chiefly of the saltation population with minor additions of the suspension population, they are well sorted, nearly symmetrical and leptokurtic. With larger additions of the suspension population, the composite samples become more poorly sorted, positively skewed and platykurtic. This also explains the variation of grain size parameters spatially and within barchans.

Strong winds transport saltation population in large amount and heap them in the form of various bedforms. Slackening winds deposit suspension population which percolates down with time. Consequently, the stabilized sands contain higher proportions of suspension population.

Roundness of desert sediments has been studied by determining roundness of one hundred quartz grains from each $1/2 \ 0$ fraction of five samples from different areas. Roundness is determined by comparison with photographic chart on P(rho) scale of Folk (1955). Operator experiment has been run to find the accuracy and consistency of the method. Different grain size fractions have a roundness of 1.79 to 2.91P. Quartz grains of the saltation population (larger than 0.125 mm) show small increase in roundness with increase in grain size, but quartz grains of the suspension population (smaller than 0.125 mm) are comparatively less rounded than the saltation population grains and have similar roundness irrespective of grain size.

Sphericity of the acclian sediments is studied by mounting grains from each of $1/2 \ 0$ fractions of samples in Canada balsamon glass slides and by measuring axial ratios of more than looquartz grains from each slide. About half of the slides show normal distribution of sphercity values and other slides are roughly equally distributed in positively skewed, negatively skewed and polymodal groups indicating that there is no need for transformation of sphericity values for their normalization as suggested by earlier workers. Mean sphericity for different slides lies between 0.56 and 0.81. One of the samples shows exceptionally low mean sphericity and high standard deviation values, reflecting probably an ultimate metamorphic source. Sphericity values are independent of grain size.

The aeolian sands have been studied for their light as well heavy mineral contents. Light minerals are studied by mounting grains of all the 1/2 Ø fractions of three samples and +120 mesh fractions of other five samples in Canada balsam on glass slides. Dominant light minerals are quartz, K-feldspar, plagioclase, chert, calcite and aragonite. The whole sand samples fall in feldspathic litharenitic sand class of Folk's (1968b) classification of sandstones indicating their mineralogically immature nature. Heavy minerals are separated using gravity separation method mainly from +230 mesh fractions of samples, in which these are abundant. Major non-opaque heavy minerals met with are hornblende, zircon, staurolite, kyanite, sillimanite and andalusite. Comparison of light minerals of +120 mesh fractions and heavy minerals of +230 mesh fractions using \mathbf{x}^2 test suggests that the samples differ from one another significantly and they belong to a 'heterogeneous' population.

The presence of spherical and elongated zircon and hornblende, staurolite, kyanite, sillimanite, and andalusite and relative abundance of the different types of quartz indicates mainly low to high rank metamorphic provenance with a minor contribution from plutonic source. Some contribution from sedimentary source is indicated by chert. Spatial inhomogeneities in light and heavy mineral composition of sands suggest that probably older deposits are being reworked by the wind and sediments are not transported over long distances. Thus no significant expansion of the desert is contemplated due to transportation of sand.

Considering the strategic location of the area and the future development potential it holds, engineering properties of the sands of the area have been studied. These include mortar making properties, compaction, shear strength and permeability.

Mortar strength test of the autoclaved cement sand cubes

reveals that strength increases with increase of Mz and σ . Further, the strength increases with increase in Sk and Ku and after critical values of Sk and Ku there is appreciable fall in strength.

Compaction test indicates that the maximum dry density decreases with increase in Mz and σ .

The determination of shear strength indicates that the soil is almost noncohesive.

The correlation of permeability with grain size parameters indicates that K decreases with increase in Mz and σ .

On the basis of these tests it can be concluded that the sands of the area belong to SW and SP soil groups of the Unified Soil Classification System (Anon., 1962).

7.2 CONCLUSIONS

Following are the salient conclusions:

- i. The Thar desert probably came into existence 10,000 years B.P. The present scenario is the product of superposition of the prevailing wind regime over the fossil longitudinal dunes and sand piles.
- ii. Three types of bedforms, namely, ripples, duncs (barchans, transverse and longitudinal) and

sand piles are recognised in the area of study.

- iii. Ripples invariably ornament the skins of dunes and sand piles. Barchans show a preferential tendency to develop in the marginal areas whereas longitudinal dunes, in general, are restricted to the desert interior.
- iv. Ripples of different wavelengths and amplitudes may occur in juxtaposition due to change in the modality of sands. Ripple index varies from 5 to 40 with a mean value of 20.1.
- v. Hat-shape barchan dunes are reported for the first time. A narrow trench scooped on its windward slope is attributed to the existence of a windward eddy.
- vi. Three stage mechanism for the formation of barchans is suggested.
- vii. Transverse dunes may originate due to lateral conjugation of two or more barchans.
- viii. The net sediment transport direction, as indicated by different dunes, deviates 15°N from the resultant wind direction. This is attributed to 'Ekman spiral' effect.
 - ix. The wind regime has remained essentially unchanged since the fossil bedforms formed around 10,000 years B.P.

- x. The Thar desert sediments lie on the finer side of the dune sands reported earlier.
- xi. Sorting appears to be a function of intermixing of mainly two populations in different proportions.
- xii. Most of the sand samples are positively skewed.
- xiii. Sand samples fall in either very leptokurtic or platykurtic groups.
 - xiv. Correlations of grain size parameters indicate that σ and Sk increase with increase in Mz whereas Ku decreases with increase in Mz.
- xv. Ripples are coarse grained, poorly sorted and have symmetrical grain size distribution, whereas sand piles and dunes, in general, have platykurtic and leptokurtic natures respectively.
- xvi. Mz, σ and Sk decrease as one moves from the foot to the crest of the barchans.
- xvii. Spatial variation as indicated in the contour maps of the various grain size parameters is thought to reflect areal variability of the grain size distribution of the original deposits being reworked or the degree of reworking by wind.
- xviii. The Thar desert sediments consist chiefly of two populations, namely, a saltation population (60-90% with Mz = 2.75 Ø and $\sigma = 0.20$ Ø) and a

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suspension population (10-40% with Mz = 3.75 ϕ and $\sigma = 0.25 \phi$). Interrelationships of the various grain size parameters and their spatial variation may be explained in terms of intermixing of these two populations in different proportions.

- xix. Roundness of quartz grains ranges from 1.79 to 2.91p. Saltation population is more rounded and the roundness increases with increase of grain size whereas suspension population is less rounded and roundness is independent of grain size.
 - xx. Sphericity of the quartz grains varies from 0.56 to 0.81 and is independent of grain size.
- xxi. The present sands fall in the feldspathic litharinitic class of Folk's (1968b) triangular diagram indicating their mineralogical immaturity. Variations of light and heavy minerals suggest that samples belong to a 'heterogneous' population. This further indicates that sands are not being transported over long distances and no significant expansion of the desert is taking place by transportation of sand.
- xxii. The mineralogical assemblage suggests low to high rank metamorphic provenance with minor contributions from the plutonic and sedimentary sources.
- xxiii. There is a significant effect of variation in

the grain size parameters on the mortar strength of cement sand cubes.

- xxiv. The maximum dry density and permeability decrease with increase in Mz and o.
 - xxv. The sand is almost noncohesive and falls in SW and SP soil groups of the Unified Soil Classification System.

7.3 SUGGESTIONS FOR FURTHER STUDY

- i. Dynamics of dune formation and rate of their migration in relation to the prevailing wind regime may be investigated in the field. It may provide clues for controlling their migration.
- ii. Ages of the stabilized dunes may be determined accurately by analyzing their pollon contents and by carbon dating method.
- iii. Internal structures of the various bedforms may be studied by trenching.
 - iv. Exhaustive study of the variation of grain size distribution within the various bedforms needs to be undertaken.
 - v. Regional variation of the thickness of sand cover, its permeability and detection of the buried channels, faults etc. in relation to the occurrence of groundwater should be carried out.

vi. Geotechnical investigations of the descrt sands reported in the dissertation need to be supplemented with further studies.

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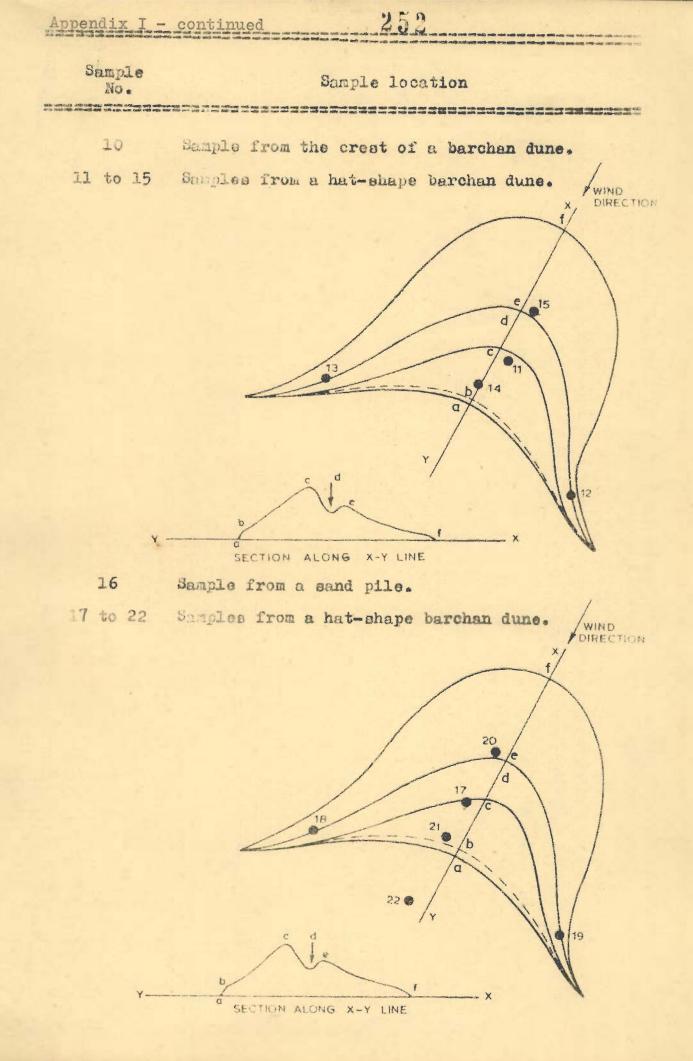
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251 APPENDIX I

DESCRIPTION OF SAMULE LOCATIONS (Refer Figure 1.3)

| Sample No. | Sample location |
|---------------|---|
| 1 | Sample from the crest of a ripple. |
| 2 | Sample from the trough of the above ripple. |
| | |
| 3 to 9 | Samples from a barchan dune. |
| | WIND DIRECTION |
| | Y Y SECTION ALONG X-Y LINE X |



| | 253 |
|----------------|--|
| Appendix I - | continued |
| Sample No. | Sample location |
| 23 24 to 29 | Sample from a sand flat (from the ripple crest) Samplesfrom a hat-shape barchan dune. |
| | WIND DIRECTION |

SECTION ALONG X-Y LINE

1

6

a

Sample from a sand pile.

Ŧ

- X

| +} | E | 1 |
|----|---|---|
| he | 0 | 4 |

| Sample No. | Sample location |
|--|--|
| a same data takan kutu kutu kutu kutu kutu kutu kutu kut | |
| 31 | Sample from the windward side of a barchan dune. |
| 32 | Sample from the windward side of a barchan dunc. |
| 33 | Sample from the southeastern flank of a longitudinal dune. |
| 34 to 36 | Samples from different sand piles. |
| 37 to 40 | Samples from different sand piles near Ramgarh (27 ⁰ 23': 70 ⁰ 30'). Locations not |
| | shown in Figure 1.3. |
| 41 and 42 | Samples from a sand pile near Ludharwa (26 ⁰ 25'0'' : 70 ⁰ 48'30''). |
| 43 | Sample from leeward side of a barchan dune. |
| 44 | Sample from windward side of the above barchan. |
| 45 | Sample from a sand pile. |
| 46 | Sample from windward side of a barchan dune. |
| 47 | Sample from leeward side of the above barchan. |
| 48 | Sample from windward side of a barchan dune. |
| 49 | Sample from leeward side of the above barchan. |
| 50 | Sample from leeward side of a barchan dune. |

| Sample No. | Sample location |
|---------------|---|
| 51 | Sample from windward side of the above barchan. |
| 52 to 54 | Samplesfrom different sand piles. |
| 55 | Sample from a sand flat. |
| 56 | Sample from a sand pile. |
| 57 | Sample from leeward side of a barchan dune. |
| 58 | Sample from windward side of the above barchan. |
| 59 | Sample from a sand pile. |
| 60 | Sample from a sand pile. |
| 61 | Sample from a sand flat. |
| 62 to 65 | Samples from different sand piles. |
| 66 | Sample from windward side of a barchan dune. |
| 67 | Sample from windward side of a barchan dune. |
| 68 | Sample from leeward side of a barchan dune. |
| 69 | Sample from leeward side of a barchan dune. |
| 70 to 74 | Samples from different sand piles. |
| 75 | Sample from windward side of a barchan dune. |
| 76 | Sample from leeward side of the above barchan. |
| 77 | Sample from windward side of a barchan dune. |
| 78 | Sample from leeward side of the above barchan. |
| 79 to 104 | Samples from the crests of different barchan dunes. |

Appendix II- Percentages of weight retained on different sieves

=

=

| ================ | ======= | ====== | ====== | ====== | ====== | =====: | ====== | | ====== | |
|------------------|-----------|-------------|------------|--------|--------|--------|--------|-------|-------------|--|
| Sample Number | | | | | Numbe | | | | | |
| TANUDOT | 25 | 35 | 45 | 60 | 80 | 120 | 170 | 230 | PF | |
| | ====== | ====== | ====== | -===== | ====== | | | | ======= | |
| | | | | | | | | | | |
| 1 | 2.05 | .03 | 71.31 | 0.00 | 6.27 | 14.21 | 2042 | 3.07 | 10 | |
| 2 | 016 | | 14.87 | 0.00 | •22 | 53.21 | 7.75 | | | |
| 3 | 0.00 | 0.00 | 。06 | 0.00 | | 85.84 | | | 3.50 | |
| 4 | •01 | 0.00 | °10 | ·01 | | 91.89 | | | • 57 | |
| 5 | 0.00 | 0.00 | 007 | 0.00 | | 79.02 | | | ° 56 | |
| 6 | 0.00 | 0.00 | 014 | 0.00 | | 88.21 | | 7.16 | •77 | |
| 7 | 0.00 | 0.00 | 015 | 0.00 | .60 | 82.60 | 3.86 | 11.31 | °62 1°45 | |
| 8 9 | 0.00 | 0.00 | •23 | 0.00 | 1.35 | 82.64 | | 10.71 | •52 | |
| 10 | 0.00 | 0.00 | ۰09 | 0.00 | .48 | 86.56 | 4.12 | 8.72 | 0.00 | |
| 10 | 0.00 | 0.00 | .09 | 0.00 | .15 | 84.42 | 5.52 | 9.39 | .39 | |
| 12 | 0.00 | 0.00 | .46 | °01 | .91 | 91.95 | 1.99 | 3.30 | 1.34 | |
| 13 | 0.00 | 0.00 | 1.20 | • 05 | | | 11.32 | 24.73 | .89 | |
| 14 | 0.00 | 0.00 | 3.27 | 004 | 4.94 | 77.97 | 4.92 | 8.45 | .37 | |
| 15 | 0.00 | 0.00 | 026 | .06 | | | 6.03 | 13.01 | 。65 | |
| 16 | 0.00 | 0.00 | .19 | .02 | 。10 | 75.33 | 7.24 | 16.37 | .70 | |
| 17 | 0.00 | 0.00 | .13 | 0.00 | .10 | 74.97 | | 17.11 | .88 | |
| 18 | 0.00 | 0.00 | .09 | 0.00 | .22 | 93.42 | | •28 | • 46 | |
| 19 | 0.00 | 0.00 | .13 | 0.00 | 044 | 81.56 | | 15.74 | • 46 | |
| 20 | 0.00 | 0.00 | .16 | 0.00 | | 74.32 | | 18.05 | •45 | |
| 21 | 0.00 |).00 | .03 | ۰02 | •48 | 73.72 | 6.23 | 18.82 | •68 | |
| 22 | 0.00 | 3.00 | •45 | 0.00 | | 76.88 | 5.66 | 16.20 | • 55 | |
| 23 | 3.24 6.45 | 0.00 | 3.86 | •04 | | 56.76 | 5.23 | 24.30 | 6.42 | |
| 24 | 0.00 | °08 | 2.47 | .01 | .95 | 38.51 | 42.68 | 8.19 | .63 | |
| 25 | 0.00 | • 03 | 0.00 | • 05 | 0.00 | 80.79 | 5.02 | 13.69 | .38 | |
| 26 | • 02 | 。01 0。00 | • 06 | 0.00 | 0.00 | 74.65 | 7.80 | 16.47 | .98 | |
| 27 | 0.00 | 0.00 | 017 | 0.00 | | 65.90 | 9.95 | 22.97 | .85 | |
| 28 | - | 0.00 | • 05 | 0.00 | | 78.93 | 5.91 | 13.60 | 1.12 | |
| 29 | •36 | 0.00 | •03 •42 | 0000 | 07 | 67.50 | 10.47 | 20.61 | 1.30 | |
| 30 | 0.00 | 0000 | | 0.00 | .29 | 63.68 | 8.61 | 22.35 | 4.24 | |
| 31 | •00 | • 00 | °16 °00 | 0.00 | 042 | 43.69 | 6.95 | 47.16 | 1.59 | |
| 32 | . 00 | .00 | .00 | • 00 | | 72.96 | 8.17 | 17.45 | 1.36 | |
| 33 | - | 0.00 | 0.00 | 00°0 | 0.00 | 76.39 | 7.80 | 15.19 | • 54 | |
| 34 | 000 | .00 | | .09 | 0.00 | | 6.39 | 15.33 | • 76 | |
| 35 | 0.00 | 0.00 | .55 | 0.09 | | 59.53 | 6.92 | 19.94 | 2.59 | |
| | | | | 0000 | 1.21 | 10.09 | 5.67 | 14.51 | 1.34 | |

²⁵⁶

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| Sample Number | | | | Me | esh Nu | nber | | | | |
|------------------|--------|-------|--------|--------|--------|-------|--------|----------------|-------|-------|
| TRUNDET. | 25 | 35 | 45 | - 60 | 80 | 120 | 170 | 230 | PF | |
| ========= | ====== | ===== | ====== | ====== | -==== | | ====== | ====== | | |
| 36 | | | | | | | | | | .===: |
| 37 | •01 | | .53 | • 06 | o 48 | 71.44 | 5.10 | 17.14 | 5.19 | |
| 38 | 0.00 | 0.00 | .05 | 0.00 | | 64.56 | 8.39 | 25.18 | | |
| 39 | 0.00 | | °08 | 0.00 | .37 | 72.09 | 6.73 | 19.46 | | |
| 40 | 0.00 | | | 0.00 | | 65.79 | 8.93 | 23.68 | | |
| 41 | 0.00 | 0.00 | • 05 | 0.00 | .36 | 80.14 | | 13.35 | | |
| 42 | 0.00 | 0.00 | ۰07 | 0.00 | .31 | 56.46 | 9.55 | 30.97 | 2.62 | |
| 43 | 0.00 | 0000 | .07 | 0.00 | .15 | 50.65 | 9.91 | 35.65 | 3.54 | |
| | 0.00 | 0.00 | 。07 | 0.00 | .42 | 72.44 | 8.27 | 17.57 | 1.20 | |
| 44 | 0.00 | 0.00 | ۰08 | 0.00 | | | | 20.58 | 1.36 | |
| 45 | 0.00 | 0.00 | .37 | 0.00 | .57 | 59,10 | 11.68 | 26.25 | 2.00 | |
| 46 | 0.00 | 0.00 | .07 | 0.00 | .12 | 70.37 | 9.29 | 18.08 | | |
| 47 | 0.00 | 0.00 | .02 | 0.00 | | | | 30.48 | | |
| 48 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 56.51 | 18.35 | 23.99 | | |
| 49 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 45.38 | 21 21 | 32.12 | 1.12 | |
| 50 | 0.00 | 0.00 | 0.00 | 0.00 | .05 | 58.65 | 1/ 58 | 24.96 | 1.25 | |
| 51 | 0.00 | 0.00 | 0.00 | 0.00 | .08 | 63.24 | | | 1.72 | |
| 52 | °01 | 0.00 | .02 | 0.00 | 0.00 | 62 68 | 12 04 | 21.42 21.59 | 1.83 | |
| 53 | 0.00 | 0.00 | .01 | .01 | -03 | 65.62 | 12 76 | | 1.73 | |
| 54 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 73.74 | | 19.72 | .82 | |
| 55 | .99 | 0.00 | .34 | .42 | 1.14 | 60.34 | 11010 | 14.02 | 1.11 | |
| 56 | 004 |).00 | 0.00 | .02 | | | | 18.05 | 11.46 | |
| 57 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 68.77 | 12059 | 15.70 | 2.84 | |
| 58 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 53.02 | | | 1.58 | |
| 59 | 0.00 | 0.00 | 0.00 | 0.00 | | 59.66 | | 20.26 | 4.24 | |
| 60 | 0.00 | 0.00 | 0.00 | 0.00 | | | 7.36 | 9.68 | .65 | |
| *61 | 1.94 | 0.00 | .06 | | | 72.56 | 9.47 | 16.05 | 1.88 | |
| 62 | 0.00 | 0.00 | .01 | · 08 | | 65.53 | 8.56 | 9.34 | 3.44 | |
| 63 | 0.00 | 0.00 | .01 | • 01 | | 88.53 | 4.48 | 5.32 | 1.49 | |
| 64 | 0.00 | 0.00 | 0.00 | 0.00 | | 91.63 | 3.72 | 3.32 | 1.29 | |
| 65 | 0.00 | 0.00 | | · 01 | 010 | 80.89 | 6.45 | 11.80 | .67 | |
| 66 | 0.00 | 0.00 | 0.00 | • 01 | | 84.00 | 5.85 | 8.15 | 1.23 | |
| 67 | 0.00 | 0.00 | • 01 | 0.00 | 05 | 75.94 | | | 2.23 | |
| 68 | 0.00 | | • 02 | 0.00 | | 81.42 | 4.86 | 12.67 | .88 | |
| 69 | | 0.00 | • 01 | 0.00 | 0.00 | 83.59 | 5.25 | 10.20 | .92 | |
| 70 | 0.00 | 0.00 | 0.00 | | 0.00 | 79.56 | 5.05 | 13.33 | 2.02 | |
| | 0.00 | 0.00 | °08 | 0.00 | •01 | 81。90 | 4.22 | 10.36 | 3.40 | |
| | | | | | | | | | | |

Mesh No. 7 10 14 18 Wt, retained 1.00 3.50 6.20 0.30

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| ~ | | | ľ | lesh Nu | umber | | | | | |
|----------------------------|---------|--------|--------|---------|-------|-------|---------|--|---------------------|--|
| Sample Number | 25 | 35 | 45 | 60 | 80 | 120 | 170 | 230 | PF | |
| ========================== | ======= | ====== | ====== | | | | | | 1970 Alexandreau | |
| | | | | | | | | | 2482222 | |
| 71 72 | 0.00 | 0.00 | | 0.00 | 0.00 | 85.37 | 4.44 | 8.56 | 1.60 | |
| 73 | 0.00 | 0.00 | | .07 | .26 | 78.48 | | 13.22 | 3.65 | |
| 74 | 0.00 | 0.00 | | 0.00 | .01 | 58.90 | 10.42 | 28.70 | 1.94 | |
| 75 | 0.00 | 0.00 | | 0.00 | 2.00 | 84.27 | 4.15 | | 8.33 | |
| | •07 | 0.00 | | 0.00 | | 82.76 | | 12.20 | .55 | |
| 76 | 001 | 0.00 | 02 | 0.00 | | 77.93 | | 12.51 | 2.25 | |
| 77 | 0.00 | 0.00 | .20 | 0.00 | | 70.86 | 8.03 | | 19.10 | |
| 78 | 0.00 | 0.00 | .16 | 0.00 | :02 | 74.70 | | 15.45 | 3.94 | |
| 79 | 0.00 | 0000 | .53 | 0.00 | | 76.29 | | 16.15 | 1.25 | |
| 80 | 0.00 | 0.00 | 06 | 0.00 | 014 | 70.03 | | 22.71 | .72 | |
| 81 | • 0 2 | 0.00 | ۰08 | 0.00 | 。30 | 72.12 | | 19.91 | 1.90 | |
| 82 | 0.00 | 0.00 | .01 | 0.00 | 0.00 | 72.65 | | 18.49 | | |
| 83 | 0.00 | 0.00 | 0.00 | 0.00 | | 82.27 | 4.56 | 10.58 | 2.54 | |
| 84 | 0.00 | 0.00 | ٥02 | 0.00 | | 82.35 | | 10.89 | .94 | |
| 85 | 0.00 | 0.00 | .15 | 0.00 | | 77.73 | | 11.00 | 3.39 | |
| 86 | 0.00 | 0.00 | 0.00 | 0.00 | | 67.53 | | 23.64 | | |
| 87 | 0.00 | 0.00 | 0.00 | 0.00 | | 77.48 | | 15.33 | | |
| 88 | 0.00 | 0.00 | .86 | 0.00 | | 78.26 | | 13.44 | .76 | |
| 89 | 0.00 | 0.00 | .37 | .02 | | 85.61 | | 7.35 | .85 | |
| 90 | 0.00 | 0.00 | 1.37 | .12 | 1.37 | 78.08 | | 12.79 | 2.58 | |
| 91 | 002 | 0.00 | .23 | 0.00 | | 81.26 | | 11.40 | .91 | |
| 92 | 010 | 0.00 | .92 | 0.00 | | 68.32 | | | 3.25 | |
| 93 | 0.00 | 0.00 | .02 | 0.00 | | 82.36 | | 22.55 | 3.24 | |
| 94 | 0.00 | J.00 | 0.00 | 0.00 | | 74.02 | | 12.33 | .72 | |
| 95 | 0.00 | 0.00 | 0.00 | 0.00 | | 74.10 | | 16.05 | 3.13 | |
| 96 | 0.00 | 0.00 | 13 | .01 | | 80.44 | | 15.76 | 3.11 | |
| 97 | 0.00 | 0.00 | .01 | 0.00 | | 78.74 | | 12.84 | 1.83 | |
| 98 | 0.00 | 0.00 | .05 | 0.00 | | 75.32 | 4.53 | 14.01 | 2.66 | |
| 99 | | | 0.00 | 0.00 | | | 0019 | 17.17 | .61 | |
| .00 | 0.00 | 0.00 | | .03 | | 83.01 | 4012 | and the second s | 1.68 | |
| .01 | | | | •01 | 000 | 80.81 | 3018 | 11.90 | 1.51 | |
| .02 | | 0.00 | 05 | | | 71.61 | 2 2 2 2 | 21.57 | ° 86 | |
| 03 | 0.00 | 2.00 | °03 | 0.00 | 01 | 85.84 | 2013 | 9.99 | .91 | |
| 04 | 2.05 | .03 | 72.42 | 0.00 | 6 27 | 14 21 | 4024 | 14.30 | 。75 | |
| | 0- | | LOTE | 0000 | 0021 | 14021 | 1.31 | 3.07 | .60 | |

Appendix III- Interpolated percentile values in phi units

| Sample Number | P-1 | P-3 | | TETCE | TUTTE | | | ======================================= |
|------------------|---|----------------|--------|--|---------|---------|---------|---|
| | | | P-5 | P-10 | P-15 | P-16 | P-20 | P-25 |
| | ======= | ====== | ====== | ====== | ====== | ======= | ======= | ============ |
| 1 | 1.100 | 1.160 | | | | | | |
| 2 | 1.155 | 1.273 | | | 1 . 270 | | | 1.320 |
| 3 | 2.540 | | | and the second sec | 1.499 | 2.516 | | 2.622 |
| 4 | 2.523 | 2.600 | | 2.680 | 2.713 | 2.719 | 2.739 | 2.762 |
| 5 | 2.550 | | | 2.655 | 2.686 | 2.692 | 2.711 | 2.732 |
| 6 | 2.542 | 2.614 2.599 | | 2.700 | 2.735 | 2.741 | 2.762 | 2.786 |
| 7 | 2.514 | 20099 | | 2.677 | 2.709 | 2.714 | 2.734 | 2.756 |
| 8 | 2.366 | | 2.614 | 2.668 | 2.704 | 2.710 | 2.733 | 2.757 |
| 9 | 2.526 | 2.542 | 2.579 | 2.637 | 2.676 | 2.682 | 2.707 | 2.733 |
| 10 | 2.560 | 2.587 | 2.619 | 2.669 | 2.703 | 2.708 | 2.729 | 2.752 |
| 11 | 2.333 | 2.618 | 2.649 | 2.697 | 2:729 | 2.735 | 2.755 | 2.777 |
| 12 | | 2.542 | 2.574 | 2.623 | 2.656 | 2.662 | 2.683 | 2.705 |
| 13 | 1.476 1.381 | 2.523 | 2.574 | 2.652 | 2.705 | 2.714 | 2.747 | 2.783 |
| 14 | 2011 C 10 | 1.490 | 2.212 | 2.521 | 2.570 | 2.579 | 2.610 | 2.643 |
| 15 | 2.542 | 2.606 | 2.640 | 2.692 | 2.728 | 2.734 | 2.756 | 2.780 |
| 16 | 2.556 | 2.622 | 2.656 | 2.710 | 2.746 | 2.752 | 2.774 | 2.799 |
| 17 | 2.569 | 2.633 | 2.666 | 2.719 | 2.754 | 2.760 | 2.782 | 2.805 |
| 18 | 2.547 | 2.599 | 2.627 | 2.669 | 2.698 | 2.703 | 2.721 | 2.741 |
| 19 | 2.527 | 2.592 | 2.626 | 2.679 | 2.715 | 2.721 | 2.743 | 2.767 |
| 20 | 2.563 | 2.628 | 2.662 | 2.715 | 2.751 | 2.757 | 2.780 | 2.804 |
| 21 | 2.534 | 2.604 | 2.641 | 2.698 | 2.736 | 2.743 | 2.766 | 2.793 |
| 22 | 2.520 | 2.589 | 2.626 | 2.683 | 2.721 | 2.727 | 2.751 | 2.777 |
| 23 | .500 | • 500 | 1.266 | 2.547 | 2.615 | 2.627 | 2.669 | 2.715 |
| 24 | .500 | 1.000 | 1.010 | 1.077 | 1.159 | 1.173 | 1.225 | 1.281 |
| 25 | 2.595 | 2.651 | 2.681 | 2.727 | 2.758 | 2.763 | 2.783 | 2.804 |
| 26 | 2.608 | 2.666 | 2.697 | 2.744 | 2.777 | 2.782 | 2.802 | 2.824 |
| 27 | 2.566 | 2.636 | 2.674 | 2.731 | 2.770 | 2.776 | 2.801 | 2.827 |
| 28 | 2.545 | 2.609 | 2.643 | 2.696 | 2.731 | 2.737 | 2.759 | 2.784 |
| 29 | 2.605 | 2.668 | 2.701 | 2.753 | 2.788 | 2.794 | 2.815 | 2.839 |
| 30 | 2.350 | 2.576 | 2.620 | 2.689 | 2.734 | 2.742 | 2.771 | 2.802 |
| 31 | 2.541 | 2.634 | 2.684 | 2.760 | 2.812 | 2 0 2 1 | 2 050 | 2.888 |
| 32 | 2.630 | 2.700 | 2.730 | 2.760 | 2.790 | 2.800 | 2 010 | 2 550 |
| | 20170 | 20170 | 20211 | 10/39 | 2-258 | 2 21 . | 2 271 | |
| 33 | -0017 | 20100 | 60177 | 10181 | 1.870 | 2 0 7 5 | 0 010 | |
| 34 | | 20227 | 60000 | 60044 | 1.145 | 71.2 | 2 7/0 | 0 |
| 35 | 2.243 | 2.538 | 2.579 | 2.642 | 2.684 | 2.691 | 2.718 | 2.747 |
| | | | | | | | | ======================================= |

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|-------------|--------------|---------|---------|----------|---------|-----------------------|---------|-----------|--|
| a | | | | Porc | entile | | 2222222 | ========= | |
| Sample | P-1 | P-3 | P-5 | P=10 | P=15 | P-16 | P-20 | | |
| Number | | | | | | | | P-25 | |
| | ========== | ======: | ======= | =======: | ======: | ======== | | | |
| | | | | | | | | | |
| 36 | 2.413 | | 2.611 | 2.674 | 2.716 | 2.724 | 2.750 | 2.779 | |
| 37 | 2.565 | | 2.675 | 2.733 | 2.772 | 2.779 | 2.804 | 2.830 | |
| 33 | 2.542 | 2.612 | 2.649 | | 2.744 | 2.750 | 2.774 | 2.800 | |
| 39 | 2.623 | 2.684 | 2.717 | 2.767 | 2.801 | 2.806 | 2.827 | 2.851 | |
| 40 | 2.543 | 2.607 | 2.640 | 2.693 | 2.728 | 2.734 | 2.756 | 2.780 | |
| 41 | 2.558 | 2.637 | 2.679 | 2.743 | 2.786 | 2.794 | 2.821 | 2.850 | |
| 42 | 2.588 | 2.666 | 2.707 | | 2.814 | 2.821 | 2.848 | 2.877 | |
| 43 | 2.539 | 2.609 | 2.646 | 2.703 | 2.741 | 2.748 | 2.772 | 2.798 | |
| 44 | 2.559 | 2.630 | 2.667 | 2.725 | 2.764 | 2.771 | 2.795 | 2.822 | |
| 45 | 2.503 | 2.589 | 2.634 | 2.704 | 2.751 | 2.759 | 2.789 | 2.821 | |
| 46 | 2.579 | 2.645 | 2.679 | 2.732 | 2.768 | 2.775 | 2.797 | 2.821 | |
| 47 | 2.618 | 2.687 | 2.724 | 2.780 | 2.818 | 2.825 | 2.849 | 2.874 | |
| 48 | 2.690 | 2.746 | 2.775 | 2.820 | 2.850 | 2.856 | 2.875 | 2.895 | |
| 49 | 2.686 | 2.749 | 2.782 | 2.834 | 2.869 | 2.875 | 2.896 | 2.920 | |
| 5 Ú | 2.630 | 2.694 | 2.729 | 2.781 | 2.817 | 2.823 | 2.845 | 2.870 | |
| 51 | 2.611 | 2.676 | 2.710 | 2.763 | 2.799 | 2.805 | 2.827 | 2.852 | |
| 52 | 2.636 | 2.697 | 2.729 | 2.779 | 2.813 | 2.819 | 2.840 | 2.863 | |
| 53 | 2.618 | 2.680 | 2.713 | 2.764 | 2.798 | 2.804 | 2.826 | 2.849 | |
| 54 | 2.653 | 2.705 | 2.733 | 2.775 | 2.804 | 2.809 | 2.827 | 2.846 | |
| 55 | 1.001 | 2.503 | 2.556 | 2.637 | 2.692 | 2.701 | 2.735 | 2.773 | |
| 56 | 2.614 | 2.675 | 2.707 | 2.757 | 2.791 | 2.796 | 2.817 | 2.840 | |
| 57 | 2.999 | 2.999 | 2.999 | 2.999 | 2.999 | 2.999 | 2.999 | 2.999 | |
| 58 | 2.815 | 2.847 | 2.864 | 2.890 | 2.907 | 2.910 | 2.921 | 2.933 | |
| 59 | 2.651 | 2.699 | 2.724 | 2.763 | 2.789 | 2.794 | 2.810 | 2.828 | |
| 60 | 2.636 | 2.691 | 2.720 | 2.765 | 2.796 | 2.801 | 2.820 | 2.841 | |
| 61 | -1.700 | -1.200 | | | 2.500 | 2.520 | 2,560 | 2. 600 | |
| 62 | 2.575 | 2.628 | 2.657 | 2.700 | 2.730 | 2.135 | 2.753 | 2.773 | |
| 63 | 2.619 | 2.665 | 2.689 | 2.726 | 2.752 | 2.756 | 2.772 | 2.789 | |
| 64 | 2.600 | 2.660 | 2.690 | 2 .720 | 2.760 | 2.770 | 2.790 | 2.800 | |
| 65 | 2.515 | 2.580 | 2.614 | 2.666 | 2.702 | 2.708 | 2.730 | 2.754 | |
| 66 67 | 2.608 | 2.666 | 2.696 | 2.743 | 2.775 | 2.780 | 2.800 | 2.821 | |
| 68 | 2.583 | 2.641 | 2.671 | 2.718 | 2.750 | 2.755 | 2.775 | 2.796 | |
| 69 | 2.660 | 2.700 | 2.730 | 2,770 | 2.800 | 2.820 | 2.820 | 2.830 | |
| 70 | 2.637 | 2.688 | 2.715 | 2.757 | 2.785 | 2.790 | 2.808 | 2.827 | |
| 10 | 2.594 | 2.650 | 2.680 | 2.725 | 2.756 | 2.761 | 2.780 | 2.801 | |
| man a state | | | | | | | | | |

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|--|-----------|----------|----------|---------|-------|----------------------------|-------|-------|--------|
| Sample | 0.1 | | | | | | | | |
| Number | P-1 | P-3 | P-5 | P-10 | P-15 | P-16 | P-20 | P-25 | |
| ======================================= | ========= | -======= | | | | | | | |
| | | | | | | | | | |
| 71 | 2.637 | 2.685 | 2.710 | 2.749 | 2.775 | 2.780 | 2.796 | 2.814 | |
| 72 | 2.552 | 2.616 | 2.650 | 2.702 | 2.737 | | 2.765 | 2.789 | |
| 73 | 2.654 | 2.714 | 2.746 | 2.796 | 2.829 | 2.834 | 2.855 | 2.878 | |
| 74 | 2.365 | 2.524 | 2.562 | 2.620 | 2.659 | 2.666 | 2.690 | 2.717 | |
| 75 | 2.554 | 2.614 | 2.646 | 2.695 | 2.729 | 2.734 | 2.755 | 2.778 | |
| 76 | 2.623 | 2.678 | 2.706 | 2.750 | 2.780 | 2.785 | 2.804 | 2.824 | |
| . 77 | 2.575 | 2.640 | 2.675 | 2.729 | 2.765 | 2.771 | 2.794 | 2.818 | |
| 78 | 2.578 | 2.640 | 2.674 | 2.725 | 2.759 | 2.765 | 2.787 | 2.810 | |
| 79 | 2.514 | 2.584 | 2.622 | 2.679 | 2.718 | 2.725 | 2.749 | 2.775 | |
| 80 | 2.578 | 2.644 | 2.678 | 2.732 | 2.768 | 2.774 | 2.797 | 2.822 | |
| 81 | 2.548 | 2.617 | 2.653 | 2.709 | 2.747 | 2.753 | 2.777 | 2.803 | |
| 82 | 2.635 | 2.691 | 2.720 | 2.765 | 2.796 | 2.801 | 2.820 | 2.841 | |
| 83 | 2.633 | 2.683 | 2.709 | 2.750 | 2.778 | 2.783 | 2.800 | 2.819 | |
| 84 | 2.624 | 2.676 | 2.703 | 2.745 | 2.773 | 2.778 | 2.795 | 2.815 | |
| 85 | 2.577 | | 2.670 | 2.719 | 2.753 | 2.759 | 2.779 | 2.802 | |
| 86 | 2.643 | 2.700 | 2.731 | 2.777 | 2.809 | 2.814 | 2.833 | 2.855 | |
| 87 | 2:650 | | 2.728 | 2.769 | 2.797 | 2.801 | 2.819 | 2.838 | |
| 88 | 2.055 | 2.502 | 2.544 | 2.610 | 2.654 | 2.662 | 2.689 | 2.719 | |
| 89 | 2.530 | 2.591 | 2.623 | 2.673 | 2.707 | 2.713 | 2.734 | 2.757 | |
| 90 | 1.467 | 2.510 | 2.552 | 2.617 | 2.660 | 2.668 | 2.695 | 2.725 | |
| 91 | 2.538 | 2.601 | 2.635 | 2.687 | 2.722 | 2.728 | 2.750 | 2.774 | |
| 92 | 1.494 | 2.558 | 2.601 | 2.668 | | 2.721 | 2.749 | 2.780 | |
| 93 | 2.616 | 2.669 | 2.696 | 2.739 | | 2.773 | 2.791 | 2.811 | |
| 94 | 2.622 | 20678 | 2.708 | 2.755 | | 2.791 | 2.811 | 2.832 | |
| 95 | 2.630 | 2.686 | 2.715 | 2.760 | 2.790 | 2.796 | 2.815 | 2.835 | |
| 96 | 2.577 | | 2.667 | 2.716 | 2.748 | 2.754 | 2.774 | 2.796 | |
| 97 | 2.626 | 2.679 | 2.707 | 2.751 | 2.780 | 2.785 | 2.803 | 2.823 | |
| 98 | 2.605 | 2.663 | 2.694 | 2.742 | 2.774 | 2.780 | 2.800 | 2.821 | |
| 99 | 2.624 | 2.675 | 2.702 | 2.744 | 2.772 | 2.776 | 2.794 | 2.813 | |
| 100 | 1.467 | 2.529 | 2.568 | 2.629 | 2.670 | 2.677 | 2.702 | 2.730 | |
| 101 | 2.604 | 2.665 | 2.697 | 2.746 | 2.780 | 2.786 | 2.806 | 2.829 | |
| 102 | 2.587 | 2.641 | 2.670 | 2.714 | 2.743 | 2.748 | 2.767 | 2.787 | |
| 103 | 2.615 | 2.668 | 2.697 | 2.740 | | 2.775 | 2.794 | 2.814 | |
| 104 | 1.050 | 1.120 | 1.170 | 1.220 | 1.260 | 1.270 | | 1.320 | |
| and the second | | | | | | | | | |

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| Sample | P-30 | P-35 | P=45 | | entile | | | |
|--------|---------|----------|--------|----------------|----------------|-------|---------|-------|
| Number | | | | P-50 | P=55 | P-65 | P-70 | P-75 |
| | ======= | ======== | ====== | ======== | ======= | | ======= | |
| 1 | 1.350 | | 1.400 | | 1.420 | | | |
| 2 | 2.671 | 2.717 | | | 2.886 | | 1. 490 | |
| 3 | 2.782 | 2.801 | 2.836 | | | 2.972 | | |
| 4 | 2.751 | 2.769 | 2.802 | | 2.869 | | 2.923 | |
| 5 | 2.808 | 2.828 | 2.865 | | 2.833 | 2.866 | 2.884 | |
| 6 | 2.775 | 2.793 | 2.827 | | 2.900 | 2.937 | 2.957 | 2.979 |
| 7 | 2.780 | 2.800 | 2.838 | | 2.859 | 2.893 | 2.911 | 2.931 |
| 8 | 2.757 | 2.779 | 2.820 | | 2.875 | 2.913 | 2.934 | 2.956 |
| 9 | 2.773 | 2.792 | 2.827 | | 2.860 | 2.901 | 2.923 | 2.947 |
| 10 | 2.797 | 2.815 | 2.849 | | 2.862 | 2.897 | 2.916 | 2.937 |
| 11 | 2.726 | 20744 | 2.049 | | 2.882 | 2.916 | 2.934 | 2.954 |
| 12 | 2.815 | 2.845 | 2.901 | | 2.813 | 2.848 | | 2.888 |
| 13 | 2.674 | 2.702 | 2.754 | | 2.955 | 3.081 | 3.297 | 3.505 |
| 14 | 2.801 | 2.821 | 2.859 | 2.779 | 2.805 | 2.857 | 2.885 | 2.915 |
| 15 | 2.821 | 2.841 | 2.879 | 2.877 2.898 | 2.895 | 2.932 | 2.952 | 2.974 |
| 16 | 2.827 | 2.847 | 2.884 | 2.902 | 2.916 | 2.954 | 2.974 | 2.996 |
| 17 | 2.758 | 2.775 | 2.805 | 2.820 | 2.920 | 2.957 | 2.977 | 2.998 |
| 18 | 2.789 | 2.809 | 2.847 | 2.865 | 2.834 | 2.865 | 2.881 | 2.899 |
| 19 | 2.826 | 2.846 | 2.884 | 2.903 | 2.884 | 2.921 | 2.942 | 2.964 |
| 20 | 2.816 | 2.838 | 2.878 | 2.898 | 2.921 | 2.959 | 2.979 | 3.025 |
| 21 | 2.800 | 2.822 | 2.862 | 2.882 | 2.917 | 2.958 | 2.980 | 3.055 |
| 22 | 2.756 | 2.795 | 2.866 | 2.901 | 2.901 | 2.942 | 2.963 | 2.987 |
| 23 | 1.332 | 1.378 | 1.466 | 2.500 | 2.935 | 3.089 | 3.510 | 3.584 |
| 24 | 2.823 | 2.840 | 2.873 | 2.889 | 2.552 | 2.660 | 2.718 | 2.781 |
| 25 | 2.844 | 2.862 | 2.896 | 2.912 | 2.905 | 2.938 | 2.955 | 2.974 |
| 26 | 2.851 | 2.873 | 2.914 | 2.933 | 2.929 | 2.963 | 2.981 | 3.015 |
| 27 | 2.805 | 2.826 | 2.863 | 2.881 | 2.953 | 2.994 | 3.180 | 3.436 |
| 28 | 2.860 | 2.880 | 2.917 | 2.935 | 2.899 | | 2.957 | 2.979 |
| 29 | 2.830 | | 2.905 | 2.929 | 2.953 2.952 | 2.989 | 3.106 | 3.342 |
| 30 | 2.920 | 2.949 | 3.052 | 3.411 | | 3.011 | 3.294 | 3.522 |
| 31 | 2 .8 60 | | 2.900 | 2 020 | 3.522 | | 3.616 | 3.652 |
| 32 | 2.298 | 2.309 | 2.329 | | 2.930 | 2.970 | 2.990 | 3.120 |
| 33 | 2.887 | 2.906 | 2:940 | 2.057 | 2.072 | 2.369 | 2.380 | 2.391 |
| 34 | | 2 • 845 | 2.888 | | 2.973 | | 3.349 | 3.524 |
| 15 | 2.773 | 2.797 | 2.842 | | 2.895 | 2.974 | | |
| | | | 20072 | .20000 | 20000 | 2.930 | 2.954 | 2.980 |

| Sample | | | | Perce: | ntile | | ======== | |
|----------|----------|---------|---------|---------|---------|-------------|----------------|----------------|
| Number | P-30 | P-35 | P-45 | P-50 | P-55 | P-65 | P-70 | P-75 |
| ======== | ======== | -=====: | ======= | ======= | ======= | | ======== | |
| 36 | 2.805 | 2.829 | 2.874 | 2.896 | 2.918 | 2 0 (2 | 2 007 | 0.000 |
| 37 | 2.854 | 2.877 | 2.918 | 2.938 | 2.958 | 2.962 3.007 | | 3.233 |
| 38 | 2.824 | 2.846 | 2.886 | 2.906 | 2.925 | 2.966 | 3.298 | 3.517 |
| 39 | 2.871 | 2.890 | 2.926 | 2.943 | 2.961 | | 2.988 | 3.172 |
| 40 | 2.801 | 2.821 | 2.858 | 2.876 | 2.894 | 2.996 | 3.223 | 3.502 |
| 41 | 2.877 | 2.901 | 2.947 | 2.969 | 2.991 | 2.931 | 2.951 | 2.973 |
| 42 | 2.904 | 2.928 | 2.974 | 2.996 | 3.205 | 3.423 | 3.533 | 3.582 |
| 43 | 2.822 | 2.843 | 2.884 | 2.904 | 2.923 | 3.536 | 3.581 | 3.630 |
| 44 | 2.845 | 2.868 | 2.909 | 2.929 | 2.949 | 2.964 | 2.986 | 3.115 |
| 45 | 2.850 | 2.877 | 2.926 | 2.951 | 2.949 | 2.990 | 3.120 | 3.348 |
| 46 | 2.843 | 2.864 | 2.902 | 2.920 | 2.939 | 3.203 2.977 | 3.420 | 3.533 |
| 47 | 2.898 | 2,919 | 2.960 | 2.979 | 2.999 | 3.396 | 2.997 3.523 | 3.225 |
| 48 | 2.914 | 2.931 | 2.964 | 2.979 | 2.995 | 3.218 | | 3.570 |
| 49 | 2.941 | 2.961 | 2.998 | 3.105 | 3.221 | 3.459 | 3.355 | 3.501 |
| 50 | 2.891 | 2.912 | 2.949 | 2.968 | 2.986 | 3.205 | 3.378 | 3.567 |
| 51 | 2.874 | 2.894 | 2.932 | 2.950 | 2.968 | 3.056 | 3.235 | 3.517 |
| 52 | 2.883 | 2.902 | 2.938 | 2.955 | 2.972 | 3.075 | 3.247 | 3.428 |
| 53 | 2.870 | 2.889 | 2.926 | 2.943 | 2.961 | 2.997 | 3.143 | 3.433 |
| 54 | 2.864 | 2.880 | 2.910 | 2.925 | 2.940 | 2.970 | 2.986 | 3.323 |
| 55 | 2.807 | 2.838 | 2.896 | 2.924 | 2.952 | 3.117 | 3.464 | 3.048 |
| 56 | 2.861 | 2.880 | 2.915 | 2.932 | 2.949 | 2.985 | 3.040 | 3.602 3.227 |
| 57 | 2.999 | 2.999 | 2.999 | 2.999 | 3.056 | 3.352 | 3.502 | 3.548 |
| 58 | 2.944 | 2.954 | 2.973 | 2.982 | 2.991 | 3.157 | 3.313 | 3.482 |
| 59 | 2.844 | 2.859 | 2.887 | 2.900 | 2.914 | 2.942 | 2.956 | 2.972 |
| 60 | 2.860 | 2.877 | 2.909 | 2.925 | 2,940 | 2.973 | 2,990 | 3.116 |
| 61 | 2 . 6 50 | 2.680 | 2.700 | 2.800 | 2.810 | 2.870 | 2.920 | 2.970 |
| 62 | 2.791 | 2.808 | 2.839 | 2.854 | 2.869 | 2.900 | 2.917 | 2.935 |
| 63 | 2.804 | 2.818 | 2.845 | 2.858 | 2.871 | 2.897 | 2,912 | 2.927 |
| 64 | 2.850 | 2.850 | 2 870 | 2.8.90 | 2. 910 | 2 930 | 2.960 | 2.980 |
| 65 | 2.776 | 2.796 | 2.833 | 2.851 | 2.869 | ¿.907 | 2.927 | 2.949 |
| 66 | 2.841 | 2.859 | 2.892 | 2.908 | 2.924 | 2.958 | 2.976 | 2.995 |
| 67 | 2.816 | 2.834 | 2.867 | 2.883 | 2,900 | 2.933 | 2.051 | 2 070 |
| 68 | 2.850 | 2.870 | 2,900 | 2,900 | 2.910 | 2.040 | 2 010 | 2 0 70 |
| 69 | 20844 | 2.860 | 2.890 | 2.904 | 2.919 | 2.949 | 2.965 | 2.982 |
| 70 | 2.820 | 2.837 | 2.869 | 2.885 | 2.901 | 2.933 | 2.951 | 2.969 |

| ===== | | ======= | ======== | | | | | | | |
|-------|------------------|---------|---|-------|-------|--------|-------|-------|---------|---|
| | Semmin | | | | Perc | entile | | | ======= | ======================================= |
| | Sample Number | P-30 | P-35 | P-45 | P-50 | P-55 | P-65 | D- 70 | 0.75 | |
| | numper. | | | | | r-35 | P-05 | P-70 | P-75 | |
| *==== | ======== | ======= | ======================================= | | | | | | | 1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1. |
| | | | | | | | | | | |
| | 71 | 2.830 | 2.845 | 2.873 | 2.887 | 2.900 | 2.928 | 2.943 | 2.959 | |
| | 72 | 2.810 | 2.830 | 2.867 | 2.885 | 2.903 | 2.940 | 2.960 | 2.981 | |
| | 73 | 2.898 | 2.917 | 2.952 | 2.969 | 2.986 | 3.284 | 3.505 | 3.554 | |
| | 74 | 2.741 | 2.763 | 2.804 | | 2.844 | 2.886 | 2.908 | 2.932 | |
| | 75 | 2.798 | 2.817 | 2.852 | 2.870 | 2.887 | 2.922 | 2.941 | 2.961 | |
| | 76 | 2.842 | 2.859 | 2.891 | 2.906 | 2.921 | 2.953 | 2.970 | 2.988 | |
| | 77 | 2.840 | 2.861 | 2.899 | 2.918 | 2.936 | 2.974 | 2.995 | 3.232 | |
| | 78 | 2.831 | 2.851 | 2.887 | 2.905 | 2.923 | 2.959 | 2.979 | 3.007 | |
| | 79 | 2.799 | 2.821 | 2.862 | 2.882 | 2.902 | 2.943 | 2.965 | 2.989 | |
| | 80 | 2.844 | 2.864 | 2.903 | 2.921 | 2.940 | 2.978 | 2.998 | 3.370 | |
| | 81 | 2.826 | 2.848 | 2.888 | 2.907 | 2.926 | 2.966 | 2.988 | 3.210 | |
| | 82 | 2.859 | 2.877 | 2.909 | 2.925 | 2.940 | 2.972 | 2.990 | 3.157 | |
| | 83 | 2.836 | 2.852 | 2.881 | 2.895 | 2.909 | 2.938 | 2.954 | 2.971 | |
| | 84 | 2.832 | 2.848 | 2.878 | 2.892 | 2.907 | 2.937 | 2.953 | 2.970 | |
| | 85 | 2.823 | 2.842 | 2.877 | 2.894 | 2.912 | 2.947 | 2.966 | 2.987 | |
| | 86 | 2.874 | 2.892 | 2.925 | 2.941 | 2.957 | 2.991 | 3.164 | 3.503 | |
| | 87 | 2.855 | 2.870 | 2.900 | 2.914 | 2.928 | 2.958 | 2.973 | 2.990 | |
| | 88 | 2.746 | 2.771 | 2.818 | 2.840 | 2.863 | 2.910 | 2.935 | 2.962 | |
| | 89 | 2.778 | 2.797 | 2.833 | 2.850 | 2.867 | 2.903 | 2.922 | 2.943 | |
| | 90 | 2.752 | 2.776 | 2.823 | 2.845 | 2.867 | 2.914 | 2.938 | 2.965 | |
| | 91 92 | 2.795 | 2.815 | 2.852 | 2.870 | 2.888 | 2.925 | 2.945 | 2.966 | |
| | 93 | 2.808 | 2.833 | 2.881 | 2.904 | 2.927 | 2.975 | 3.029 | 3.510 | |
| | 75 74 | 2.828 | 2.845 | 2.875 | 2.890 | 2.905 | 2.935 | 2.952 | 2.969 | |
| | 95 | 2.851 | 2.869 | 2.902 | 2.917 | 2.933 | 2.966 | 2.984 | 3.064 | |
| | 96 | 2.854 | 2.871 | 2.904 | 2.919 | 2.935 | 2.967 | 2.984 | 3.056 | |
| | 97 | 2.816 | 2.834 | 2.869 | 2.885 | 2.902 | 2.936 | 2.955 | 2.974 | |
| |) 8 | 2.841 | 2.858 | 2.889 | 2.904 | 2.919 | 2.950 | 2.967 | 2.985 | |
| | 99 | 2.841 | 2.859 | 2.893 | 2.910 | 2.926 | 2.960 | 2.978 | 2.998 | |
| | 10 | 2.830 | 2.846 | 2.876 | 2.890 | 2.905 | 2.934 | 2.950 | 2.967 | |
| 10 | | 2.755 | 2.778 | 2.821 | 2.842 | 2.863 | 2.906 | 2.929 | 2.954 | |
| 10 | | 2.850 | 2.869 | 2.904 | 2.921 | 2.938 | 2.974 | 2.993 | 3.273 | |
| 10 | | 2.805 | 2.822 | 2.854 | 2.869 | 2.884 | 2.915 | 2.932 | 2.951 | |
| 10 | | 2.832 | 2.849 | 2.880 | 2.895 | 2.910 | 2.941 | 2.958 | 2.976 | |
| 10 | | 10 240 | 1.380 | 1.410 | 1.420 | 1.440 | 1.480 | 1.490 | 2 3 50 | |
| | | | | | | | | | | |

| | | | | | V | | |
|----------|----------------|----------------|--------|---------|----------------|--------------------|---------------------|
| Sample | | | Per | centile |) | ====== | |
| Number | P-80 | P-84 | P-85 | P-90 | P=95 | P-97 | P-99 |
| | ====== | ======= | ====== | ====== | ======= | ======= | |
| 1 | 0.010 | 2 0 20 | 3 100 | 2 200 | 5 000 | 1 | |
| 2 | 2.810 | 3.050 | | | 3.800 | 4.210 | 4 670 |
| 3 | 2.966 | | 3.651 | 3.761 | | 4.005 | |
| 4 | 2.924 | 2.986 | 2.949 | | 3.599 | | 3.909 |
| 5 | 3.038 | | 3.392 | | 3.501 | | |
| 6 | 2.952 | | 2.977 | 3.176 | 3.706 | 3.795 | 3.963 |
| 7 | 2.981 | | 3.200 | | 3.604 3.742 | 3.713 3.855 | 3.920 |
| 8 | 2.974 | | 3.076 | | 3.659 | 3.747 | 4.011 3.912 |
| 9 | 2.960 | | 2.986 | 3.330 | 3.537 | 3.568 | 3.626 |
| 10 | 2.976 | 2.996 | | | 3.629 | 3.716 | 3.880 |
| 11 | 2.910 | | 2.936 | 2.970 | 3.400 | 3.687 | |
| 12 | 3.554 | | 3.611 | | 3.789 | | 3.988 |
| 13 | 2.949 | 2.980 | | 3.365 | 3.610 | 3.699 | 3.867 |
| 14 | 2.998 | | | 3.567 | 3.698 | 3.783 | 3.944 |
| 15 | 3.285 | 3.514 | | 3.610 | 3.731 | 3.809 | 3.957 |
| 16 | 3.342 | | 3.541 | | 3.750 | 3.831 | 3.984 |
| 17 | 2.918 | | 2.941 | 2.970 | 3.061 | 3.193 | 3.441 |
| 18 | 2.988 | | 3.515 | 3.591 | 3.703 | 3.776 | 3.914 |
| 19 | 3.383 | 3.528 | 3.541 | 3.612 | 3.719 | 3.788 | 3.918 |
| 20 | 3.457 | | 3.555 | 3.631 | 3.744 | 3.818 | 3.957 |
| 21 | 3.203 | | 3.523 | 3.600 | 3.716 | 3.791 | 3.932 |
| 22 | 3.666 | 3.741 | 3.762 | 3.882 | 4.008 | 4.024 | 4 • 054 |
| 23 | 2.850 | | | 3.269 | 3.628 | 3.731 | 3.927 |
| 24 | 2.995 | 3.297 | | | 3.679 | 3.753 | 3.893 |
| 25 | 3.324 | 3.520 | 3.535 | 3.623 | 3.754 | 3.838 | 3.998 |
| 26 | 3.538 | | 3.597 | 3.670 | 3.779 | 3.849 | 3.983 |
| 27 28 | 3.049 | | 3.474 | 3.594 | 3.742 | 3.837 | 4.003 |
| 29 | 3.523 3.598 | | 3.590 | 3.674 | 3.800 | 3.881 | 4.008 |
| 30 | 3.691 | 3.668 3.727 | 3.687 | 3.799 | 3.964 | 4.011 | 4.043 |
| 31 | 3.420 | | 3.737 | 3.795 | 3.881 4.020 | 3.937 | 4.014 |
| 32 | 2.404 | | 2.419 | | 2.467 | 4 < 230 2 • 485 | 4 ° 6 30 2 ° 741 |
| 33 | 3.587 | 3.644 | 3.660 | 3.752 | 2.407 | 3.977 | 4.029 |
| 34 | 3.536 | | 3.618 | 3.721 | 3.874 | 3.973 | 4.029 |
| 35 | 3.126 | | 3.514 | 3.616 | 3.765 | 3.863 | 4.029 |
| | | 20100 | 20227 | 20010 | 20102 | 50005 | 10007 |

1

Appendix III- continued

| *===== | ===== | | | | | | | | |
|--|---------|---------|---------|----------|---------------|----------------|-----------|---|------|
| ====================================== | | | Pe | rcentil | ======== e | ========= | ======== | ======================================= | ==== |
| Sample Number | P-80 | P-84 | P-85 | P-90 | P=95 | P-97 | P-99 | | |
| | | | | | | | | | |
| | ======= | ======; | ======: | ======== | ========= | | -======== | ======================================= | = |
| 36 | | | | | | | | | |
| 37 | 3.546 | 3.635 | | | 4.001 | 4.017 | 4.049 | | |
| 33 | 3.571 | 3.621 | 3.635 | | 3.833 | | 4.014 | | 1000 |
| | 3.508 | 3.562 | | 3.662 | 3.789 | | 4.006 | | |
| 39 | 3.558 | | 3.623 | 3.705 | 3.826 | 3.905 | | | |
| 40 | 2.997 | | 3.472 | 3.602 | 3.760 | | | | |
| 41 | 3.637 | | 3.702 | 3.783 | 3.903 | | | | |
| 42 | 3.685 | 3.735 | 3.748 | 3.828 | 3.947 | | | | |
| 43 | 3.419 | 3.539 | 3.554 | 3.644 | 3.777 | | | | |
| 44 | 3.523 | 3.577 | 3.591 | 3.677 | 3.804 | | 4.010 | | |
| 45 | 3.590 | | 3.656 | 3.739 | 3.862 | | 4.021 | | 1252 |
| 46 | 3.501 | 3.564 | 3.582 | 3.683 | | 3.931 | 4.022 | | |
| 47 | 3.623 | | 3.685 | 3.763 | 3.878 | 3.952 | 4.023 | | |
| 48 | 3.553 | | 3.613 | 3.689 | 3.802 | 3.875 | 4.003 | | |
| 49 | 3.613 | 3.656 | 3.667 | 3.735 | 3.835 | 3.900 | 4.007 | | |
| 50 | 3.573 | | 3.638 | 3.720 | 3.842 | 3.921 | 4.017 | | |
| 51 | 3.541 | 3.597 | | 3.703 | 3.836 | 3.923 | 4.019 | | |
| 52 | 3.541 | | 3.611 | 3.699 | | 3.916 | 4.017 | | |
| 53 | 3.506 | | 3.567 | 3.645 | 3.761 | | 3.977 | | |
| 54 | | | 3.502 | 3.600 | | 3.839 | 4.003 | | |
| 55 | | | | 4.004 | 4.027 | 4.042 | 4.003 | | 186 |
| 56 | | | | 3.691 | 3.871 | 3.088 | 4.070 | | |
| 57 | 3.600 | | 3.659 | | | 3.918 | 4.052 | | |
| 58 | 3.573 | | 3.667 | | | 4.011 | 4.014 | | |
| 59 | 2.990 | 3.101 | 3.163 | | 3.656 | 3.753 | 3.936 | | |
| 60 | 3.379 | 3.532 | 3.551 | 3.656 | | 3.0914 | | | |
| 61 | 3.550 | | 3.760 | | | 4.050 | 4.019 | | |
| 62 | 2.955 | | 2.979 | 3.127 | | 3.787 | 4.400 | | |
| 63 | 2.944 | | 2.964 | 2.989 | | 3.682 | 4.012 | | |
| 64 | 3.000 | | | 3.540 | | | 4.008 | | |
| 65 | | 2.995 | | 3.438 | | 3.770 | 3,940 | | 1.10 |
| 66 | 3.178 | 3.380 | | 3.606 | | 3.803 | 4.006 | | |
| 67 | 2.999 | 2.999 | 2.999 | 2,999 | | 3°931 3°352 | 4.024 | | |
| 68 | 2.000 | 3.050 | 3.130 | 3.530 | | 3.800 | 3.502 | | |
| 69 | | | 3.507 | 3.626 | | 3.917 | 4.000 | | |
| 70 | 2.990 | | 3.345 | 3,630 | | | 4.021 | | |
| | U.S. | | | 20020 | 50011 | 4.004 | 4.031 | | |

| Sample | | | | Perce | ntile | | | ======================================= |
|--------|---------|---------|--------|---------|----------|-------|----------------|---|
| Number | P-80 | P-84 | P-85 | P-90 | P-95 | P-97 | P-99 | |
| | ======= | ======= | ====== | ======= | ======== | | | |
| 71 | 2.977 | | | | | | | |
| 72 | 3.128 | | | | 3.713 | 3.849 | 4.014 | |
| 73 | | | | 3.693 | 3.911 | 4.006 | 4.039 | |
| 74 | 3.607 | | | 3.748 | 3.865 | 3.940 | 4.020 | |
| 75 | 2.959 | | | 3.429 | 4.017 | 4.032 | | |
| 76 | 2.984 | | 3.218 | 3.551 | 3.681 | 3.765 | | |
| 77 | 3.127 | | | 3.622 | 3.812 | 3.935 | | |
| 78 | 3.743 | | | 4.023 | 4.044 | 4.058 | 4.083 | |
| | 3.443 | | | 3.734 | 3.937 | 4.008 | 4.041 | |
| 79 | 3.254 | | | 3.631 | 3.771 | 3.861 | 4.007 | |
| 80 | 3.534 | | | 3.661 | 3.767 | 3.835 | 3.965 | |
| 81 | 3.524 | 3.583 | 3.599 | 3.694 | 3.834 | 3.925 | 4.020 | |
| 82 | 3.505 | 3.566 | 3.582 | 3.680 | 3.825 | 3.920 | 4.019 | |
| 83 | 2.990 | 3.175 | 3.283 | 3.597 | 3.815 | 3.957 | | |
| 84 | | 3.127 | 3.209 | 3.542 | 3.698 | 3.799 | | |
| 85 | | 3,383 | 3.455 | 3.643 | 3.881 | 4.004 | 4.037 | |
| 86 | | 3.612 | 3.626 | 3.710 | 3.833 | | 4.015 | |
| 87 | | 3.501 | 3.516 | 3.601 | 3.728 | 3.810 | 3.966 | |
| 88 | 2.992 | 3.301 | 3.416 | 3.581 | 3.719 | 3.809 | 3.978 | |
| 89 | 2.966 | 2.987 | 2.992 | 3.491 | 3.772 | 3.950 | 4.029 | |
| 90 | 2.995 | 3.280 | 3.373 | 3.574 | 3.717 | 3.810 | | |
| 91 | 2.990 | 3.305 | 3.449 | 3.645 | 3.874 | 4.002 | 3.986 | |
| 92 | 3.580 | 3.644 | 3.661 | 3.764 | | | 4.035 | |
| 93 | | 3.164 | 3.273 | 3.559 | | 3.786 | 4°035 3°954 | |
| 94 | 3.435 | 3.562 | 3.583 | 3.707 | 3,891 | 4.001 | | |
| 95 | 3.412 | 3.557 | 3.578 | 3.703 | 3.888 | 4.001 | 4.034 | |
| 96 | 2.997 | 3.350 | 3.463 | | 3.786 | 3.899 | 4.034 | |
| 97 | 3.127 | 3.514 | 3.536 | 3.663 | 3.851 | 3.973 | 4.019 | |
| 98 | | 3.522 | 3.535 | | 3.728 | 3.803 | 4.030 | |
| 99 | | 3.107 | 3.225 | | 3.757 | 3.877 | 3.944 | |
| 100 | | 3.151 | 3.281 | | 3.754 | | 4.016 | |
| 101 | | 3.573 | 3.586 | | 3.773 | 3.865 | 4.013- | |
| 102 | 2.971 | 2.989 | 2.994 | 3.522 | 3.683 | 3.846 | 3.983 | |
| 103 | 2.996 | 3.381 | 3.500 | 3.588 | 3.718 | 3.788 | 3.985 | |
| 104 | | | 2.680 | 2.8 60 | 3.200 | 3.802 | 3.962 | |
| | | | | | 20200 | 3.460 | 4,900 | |

| Appendix | IV- | Mean grair | 1 5 | ize values | (phi units) | as |
|----------|-----|------------|-----|------------|-------------|----|
| | | estimated | by | different | formulae | |

| Sample Number | Mzl | Mz2 | Mz3 | Mz4 | Mz |
|------------------|---|---|---|---|------------------|
| | ======================================= | ======================================= | ======================================= | ======================================= | |
| 1 | 1. 4100 | 2. 1650 | 1 03 22 | | |
| 1 2 3 | 2.8450 | 3.0743 | 1.9133 2.9978 | 1. 7560 | 1. 7830 |
| | 2.8530 | 2.8530 | 2.8530 | 2.7663 | 2.7859 |
| 4 | 2 . 8179 | 2.8179 | 2.8179 | 2.9045 | 2.9055 |
| | 2 • 8829 | 3.0285 | 209800 | 2.8179 | 2 • 8655 |
| 5 6 | 2.8436 | 2.1436 | 2.8436 | 2 • 9 8 3 8 | 209780 |
| 7 | 2.8572 | 2.8934 | 2.8813 | 2.8769 | 2.8984 |
| 8 | 2.8406 | 2.8406 | | 2.9618 | 2.9406 |
| 9 | 2.8449 | 2.8449 | 2.8406 2.8449 | 2.9368 | 2.9036 |
| 10 | 2.8657 | 2.8657 | 2.8657 | 2.9069 | 2.8917 |
| 11 | 2.7969 | 2.7969 | 2.7969 | 2.9545 | 2.9228 |
| 12 | 2.9283 | 3.1567 | | 2.7969 | 2.8350 |
| 13 | 2.7798 | 2.7798 | 3.0806 | 3.0753 | 3.0752 |
| 14 | 2.8773 | 3.0135 | 2°7798 2°9681 | 2.8453 | 2.8062 |
| 15 | 2.8980 | 3.1333 | 3.0049 | 2.9784 | 2.9710 |
| 16 | 2.9024 | 3.1436 | | 3.0028 | 3.0050 |
| 17 | 2.8202 | 2.8202 | 3.0632 2.8202 | 3.0104 | 3.0127 |
| 18 | 2.8659 | 3.1119 | 3.0299 | 2.8202 | 2.8251 |
| 19 | 2.9032 | 3.1434 | 3.0633 | 2.9737 | 2.9756 |
| 20 | 2.8983 | 3.1425 | 3.0611 | 3.0077 | 3.0118 |
| 21 | 2.8822 | 3.1187 | 3.0399 | 3.0049 2.9861 | 3.0119 |
| 22 | 2.9010 | 3.1842 | 3.0898 | 3.1197 | 2.9880 |
| 23 | 2.5002 | 2.0442 | 2.1962 | 2.1795 | 2.9637 |
| 24 | 2 . 8895 | 3.0305 | 2.9835 | 2.9921 | 1.0437 |
| 25 | 2.9127 | 3.1517 | 3.0720 | 3.0214 | 2°9857 3°0255 |
| 26 | 2.9339 | 3.1807 | 3.0984 | 3.0736 | |
| 27 | 2.8816 | 3.0605 | 3.0009 | 2.9872 | 3.0820 |
| 28 | 2.9352 | 3.1850 | 3.1017 | 3.0661 | 2.9882 |
| 29 | 2.9290 | 3.2055 | 3.1133 | 3.1085 | 3.0803 |
| 30 | 3.4114 | 3.2744 | 3.3201 | | 3.1059 |
| 31 | 2.9200 | 3, 1750 | 3, 0900 | 3.3009 | 3.2763 |
| 32 | 2.3394 | 2.3394 | 2.3394 | 3,0560 | 3. 0760 |
| 33 | 2.9571 | 3.2351 | 3.1424 | 2.3394 | 2.3394 |
| 34 | 2.9096 | 3.1720 | | 3.1470 | 3.1428 |
| 35 | 2.8637 | 3.0889 | 3.0845 | 3.0290 | 3.0612 |
| | 200001 | 200003 | 3.0138 | 2.9698 | 2.9726 |

Appendix IV- continued

| Sample Number | Mzl | Mz2 | Mz3 | Mz4 | Mz |
|------------------|---|---------|---------|---------|----------|
| ========= | ======================================= | | | | |
| | | | | | |
| 36 | 2.8963 | 3.1796 | 3.0852 | 3.0329 | 3.058 |
| 37 | 2.9388 | 3.2006 | 3.1133 | 3.1081 | 3.102 |
| 38 | 2.9063 | 3.1565 | 3.0731 | 3.0175 | 3.035 |
| 39 | 2.9100 | 3.1800 | 3.0900 | 3.0520 | 3.0841 |
| 40 | 2.8765 | 3.0464 | 2.9898 | 2.9850 | 2.986 |
| 41 | 2.9696 | 3.2412 | 3.1507 | 3.1813 | 3.176 |
| 42 | 2.9961 | 3.2784 | 3.1843 | 3.2164 | 3.2370 |
| 43 | 2.9042 | 3.1439 | 3.0640 | 3.0121 | 3.025 |
| 44 | 2.9292 | 3.1741 | 3.0925 | 3.0596 | 3.0715 |
| 45 | 2.9510 | 3.2009 | 3.1176 | 3.1332 | 3.124 |
| 46 | 2.9207 | 3.1700 | 3.0869 | 3.0357 | 3.0594 |
| 47 | 2.9795 | 3.2486 | 3.1589 | 3.1889 | 3.1828 |
| 48 | 2.9796 | 3.2284 | 3.1454 | 3.1520 | 3.1549 |
| 49 | 3.1059 | 3.2656 | 3.2124 | 3.2288 | 3.2284 |
| 50 | 2.9680 | 3.2242 | 3.1388 | 3.1482 | |
| 51 | 2.9504 | 3.2014 | 3.1177 | 3.1053 | 3.1469 |
| 52 | 2.9555 | 3.2076 | 3.1236 | 3.1132 | 3.1092 |
| 53 | 2.9436 | 3.1796 | 3.1009 | 3.0736 | 3.1171 |
| 54 | 2 . 9256 | 3.1317 | 3.0630 | 3.0305 | 3.0788 |
| 55 | 2.9243 | 3.2725 | 3.1565 | 3.1677 | 3.0383 |
| 56 | 2.9328 | 3.1732 | 3.0931 | 3.0568 | 3.1330 |
| 57 | 3.0000 | 3.3234 | 3.2156 | 3.2475 | 3.0740 |
| 58 | 2.9675 | 3.2415 | 3.1502 | 3.1526 | 3.2463 |
| 59 | 2.9008 | 2.9477 | 2.9320 | 2.9947 | 3.1579 |
| 60 | 2.9253 | 3.1673 | 3.0866 | 3.0397 | 2.9739 |
| 61 | 2.8000 | 3.1100 | 3.0667 | 2.28 60 | 3.0540 |
| 62 | 2.8546 | 2.8546 | 2.8546 | 2.8785 | 2. 579 0 |
| 63 | 2.8583 | 2.8583 | 2.8583 | | 2.9108 |
| 64 | 2.8900 | 2. 9900 | 2.9570 | 2.8583 | 2.8993 |
| 65 | 2.8517 | 2.8517 | 2.0517 | 2.98 60 | 2.978 0 |
| 66 | 2.9088 | 3.0805 | | 2.9320 | 2.9120 |
| 67 | 2.8839 | 2.9963 | 3.0233 | 3.0153 | 3.0164 |
| 68 | 2, 9000 | 2.9300 | 2,9588 | 2.9883 | 2.9781 |
| 69 | 2.9049 | 3.1107 | 2. 9200 | 3. 0020 | 2.978 0 |
| 70 | 2.8856 | 2.9934 | 3.0421 | 3.0197 | 3.0241 |
| | 200000 | 207934 | 2.9574 | 3.0024 | 2.9972 |

| | ======================================= | | | | | |
|------------------|---|---------|------------------|---|---|------|
| Sample Number | Mzl | Mz.2 | Mz 3 | Mz4 | Mz | = |
| | ======================================= | | ============= | ======================================= | ======================================= | 2 == |
| 71 | 2.8870 | 2.8870 | 2 0 0 7 0 | 2 2 2 2 2 | | |
| 72 | 2.8854 | 3.1322 | 2.8870 3.0499 | 2.9832 | 2.9520 | |
| 73 | 2.9695 | 3.2457 | 3.1536 | 3.0104 | 3.0157 | |
| 74 | 2.8000 | 2.9500 | 2.9000 | 3.1837 | 3.1684 | |
| 75 | 2.8700 | 2.9186 | | 2.4500 | 2.6760 | |
| 76 | 2.9064 | 3.0955 | 2°9024 3°0324 | 2.9714 | 2.9495 | |
| 77 | 2.8000 | 3.0000 | | 3.0185 | 3.0219 | |
| 78 | 2.9055 | 3.1695 | 2.9333 | 2.9660 | 2.9910 | |
| 79 | 2.8826 | 3.1233 | 3.0815 | 3.0352 | 3.0408 | |
| 80 | 2.9216 | 3.1767 | 3.0430 | 2.9918 | 2.9945 | |
| 81 | 2.4100 | 2.4550 | 3.0916 | 3.0318 | 3.0685 | |
| 82 | 2.9250 | | 2.4400 | 2.5420 | 2.5340 | |
| 83 | 2.8954 | 3.1837 | 3.0975 | 3.0442 | 3.0624 | |
| 84 | 2.8928 | 2.9792 | 2.9513 | 3.0069 | 2.9960 | |
| 85 | 2.8949 | 2.9526 | 2.9326 | 2.9931 | 2.9741 | |
| 86 | 2.9417 | 3.0715 | 3.0126 | 3.0096 | 3.0130 | |
| 87 | 209144 | 3.2133 | 3.1227 | 3.0936 | 3.1126 | |
| 88 | 2.8409 | 3.1516 | 3.0725 | 3.0228 | 3.0256 | |
| 89 | 2.8502 | 2.9819 | 2.9349 | 2.9429 | 2.9381 | |
| 90 | | 2.3502 | 2.8502 | 2.9432 | 2.9198 | |
| 91 | 2.8454 | 2.9745 | 2.9315 | 2.9455 | 2.9377 | |
| 92 | 2.8706 | 3.0170 | 2.9682 | 2.9889 | 2.9906 | |
| 93 | 2.9048 | 3.1829 | 3.0902 | 3.0350 | 3.0803 | |
| 94 | 2.8904 | 2.9689 | 2.9427 | 2.9941 | 2.9778 | |
| 95 | 2.9179 | 3.1770 | 3.0906 | 3.0433 | 3.0538 | |
| 96 | 2.9195 | 3.1765 | 3.0909 | 3.0444 | 3.0543 | |
| 97 | 2.8856 | 3.0523 | 2.9967 | 2.9968 | 2.9980 | |
| 98 | 2.9044 | 3.1499 | 3.0680 | 3.0255 | 3.0302 | |
| 99 | 2.9101 | 3.1512 | 3.0708 | 3.0172 | 3.0194 | |
| 100 | 2.8906 | 2.9422 | 2.9250 | 2.9980 | 2.9801 | |
| 105 | 2.3426 | 2.9140 | 2.8902 | 2.9479 | 2.9330 | |
| | 2.9217 | 3.1796 | 3.0936 | 3.0347 | 3.0627 | |
| 102 | 2.8693 | 2.8693 | 2.8693 | 2.9689 | 2.9308 | |
| 103 | 2.8955 | 3.0785 | 3.0175 | 3.0032 | 3.0060 | |
| 104 | 1.4200 | 1. 9500 | 1.7733 | 1.6660 | 1. 769-0 | |
| | | | | | | |

Appendix V- Standard deviation values (phi units) as estimated by different formulae

| | | | ================== | ================= | |
|-------------|----------------|--------------------------------|--------------------|---|---------|
| Sample | | | | | |
| Number | σι | <i>d</i> 2 | σ3 | σ4 | σ |
| | | | | | |
| | ============ | ============================== | ================= | ======================================= | |
| 1 | . 133 3 | | 1000 | | |
| 1 2 3 | .6092 | . 88 50 | . 836 4 | .8204 | . 74 40 |
| 3 | 01342 | • 5580 | •6711 | ·8777 | ·7146 |
| 4 | •1263 | .1336 | ·2134 | .2307 | .2280 |
| 5 | •1425 | •1258 | 01980 | •2137 | •1894 |
| 6 | °1425 °1294 | •2875 | · 3041 | •3177 | ·2721 |
| 7 | | •1288 | °2120 | ·2301 | ·2161 |
| 8 | ∘1471 ∘1585 | • 1826 | ·2621 | •3006 | • 2833 |
| 9 | | .1578 | ·2426 | .2742 | .2776 |
| 10 | .1366 | .1360 | ·2070 | .2224 | .2214 |
| 10 | .1310 | .1304 | .2136 | .2359 | .2456 |
| 12 | .1349 | .1343 | .1922 | .2047 | .2044 |
| | 。5352 | °4425 | °4053 | •3928 | •4016 |
| 13 | .2014 | °2005 | •3121 | • 3363 | • 3961 |
| 14 | .1437 | °2793 | .2999 | .3165 | .2686 |
| 15 | .1464 | .3811 | °3533 | .3438 | ° 3024 |
| 16 | .1429 | °3835 | °3559 | .3464 | · 3093 |
| 17 | o1170 | .1165 | 01241 | .1254 | •1334 |
| 18 | .1453 | .3906 | •3585 | • 3477 | ° 2740 |
| 19 | .1635 | ·3854 | •3527 | •3418 | |
| 20 | ·1945 | •3995 | • 3669 | •3559 | • 3091 |
| 21 | °1551 | .3910 | .3606 | • 3502 | • 3298 |
| 22 | •6434 | .5571 | 06941 | .7201 | • 3003 |
| 23 | ·1106 | .8702 | .4097 | .7415 | • 7263 |
| 24 | .1262 | .2667 | .2845 | .3037 | • 0371 |
| 25 | 01414 | o3691 | 03447 | • 3362 | · 2510 |
| 26 | o4511 | •4038 | • 3693 | • 3578 | • 2978 |
| 27 | 01444 | .3226 | • 3277 | • 3409 | • 3538 |
| 28 | •3721 | • 3907 | • 3617 | 03518 | • 2822 |
| 29 | 。5331 | •4627 | •4349 | | • 3392 |
| 30 | • 5656 | .4533 | •4080 | • 4 2 5 1 | · 4215 |
| 31 | . 21 4 8 | .3750 | .3820 | °.3930 °.3889 | · 4255 |
| 32 | 0776 | .0772 | 00174 | 0772 | · 3500 |
| 33 | •4860 | •4093 | • 3787 | .3683 | • 0773 |
| 34 | •3837 | .4291 | •4025 | • 3932 | • 3776 |
| 35 | •1727 | •3971 | • 3784 | • 3735 | • 3681 |
| | | | | 20100 | •3173 |

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| Samp | le | | | | |
|------|--------|--------|--|---|---------|
| Numb | | σ2 | 03 | σ4 | σ |
| | | | | | |
| | | | and and any see the first set up, the set of the | Ann | |
| 36 | °3359 | •4554 | •4383 | .4318 | •3902 |
| 37 | .5086 | .4211 | .3860 | .3742 | .3809 |
| 38 | °2751 | .4056 | •3757 | .3654 | •3423 |
| 39 | 。2222 | .3700 | .3805 | .3852 | .3571 |
| 40 | .1430 | .3122 | .3257 | .3452 | .2809 - |
| 41 | .5423 | .4471 | .4089 | .3961 | .4237 |
| 42 | ₀5576 | •4566 | •4161 | •4026 | •4297 |
| 43 | 02344 | •3955 | • 3690 | •3599 | • 3302 |
| 44 | °3900 | .4029 | •3736 | • 3636 | •3528 |
| 45 | •5276 | .4410 | •4065 | .3948 | °4130 |
| 46 | 。2986 | .3949 | .3723 | .3643 | o3401 |
| 47 | 。5153 | 。4233 | .3864 | .3741 | 。4007 |
| 48 | •4483 | .3721 | .3417 | .3314 | .3426 |
| 49 | .4792 | .3904 | .3547 | .3428 | °3685 |
| 50 | °4795 | 。4005 | .3690 | .3583 | •3714 |
| 51 | .4268 | .3958 | .3685 | .3591 | .3583 |
| 52 | .4226 | .3885 | .3611 | .3517 | .3521 |
| 53 | •3509 | 03749 | •3461 | .3363 | • 3285 |
| 54 | .1497 | 。3225 | ·3145 | .3166 | .2762 |
| 55 | .6141 | .5709 | 。5084 | 。4915 | 。5007 |
| 56 | .2861 | .3763 | 。3645 | .3598 | .3344 |
| 57 | •4066 | .3234 | .2899 | .2789 | .3029 |
| 58 | •4476 | 。4058 | .3867 | .3797 | .3541 |
| 59 | .1069 | .1533 | .2179 | .2418 | .2297 |
| 60 | ·2035 | •3656 | •3483 | •3420 | • 3080 |
| 61 | . 2741 | 。 5900 | 1.022 3 | 1. 1222 | 1.1692 |
| 62 | 01199 | 01194 | 。2047 | .2233 | .2103 |
| 63 | .1023 | .1019 | 01641 | .1776 | ·1713 |
| 64 | 。1333 | · 2200 | · 263 C | .2870 | , 2505 |
| 65 | 01442 | .1436 | .2327 | 。2551 | °2625 |
| 66 | ·1288 | 。3000 | 。3177 | .3273 | o 2902 |
| 67 | .1289 | .2408 | .2784 | .3026 | • 2606 |
| 68 | .9630 | 。7750 | .6920 | .6704 | o7319 |
| 69 | .1148 | .3202 | .3248 | 。3350 | .2690 |
| 70 | .1247 | .2320 | .2974 | .3309 | .2856 |

==

| Sample Number | σl | σ2 | σ3 | σ4 | σ |
|------------------|--|------------------|-------------------|----------------|----------------|
| | | | | | |
| 71 | 。1070 | ·1066 | ·2053 | .2269 | ·2431 |
| 72 | .1428 | .3889 | °3855 | .3834 | .3181 |
| 73 | 。5005 | ·4108 | .3748 | 。3627 | •3887 |
| 74 | .3333 | 。4000 | 。7833 | .9167 | 。9637 |
| 75 | ·1356 | .1837 | .2485 | .2822 | °2612 |
| 76 | ·1212 | · 3098 | •3224 | •3345 | °2835 |
| 77 | .2148 | ° 3000 | •2879 | • 3 2 9 6 | · 3495 |
| 78 | .1459 | 。4038 | •3933 | .3889 | • 3495 |
| 79 | .1581 | •3982 | • 3732 | • 3645 | •3187 |
| 80 | •4060 | 。4017 | .3657 | .3537 | •3310 |
| . 81 | °1111 | °1450 | .2210 | .3204 | 02637 |
| 82 | •2345 | ·3824 | •3587 | 。3504 | • 3252 |
| 83 | .1126 | .1958. | .2654 | .2982 | • 2668 |
| 84 | o1151 | 01744 | .2379 | .2651 | ·2456 |
| 85 | .1364 | •3124 | • 3397 | • 3544 | • 3050 |
| 86 | 。4797 | .3989 | .3665 | °3556 | 。3474 |
| 87 | .1131 | •3498 | .3264 | .3184 | °2664 |
| 88 | ·1796 | •3199 | •3379 | •3586 | • 3043 |
| 89 | 01374 | .1368 | 02424 | °2655 | °2805 |
| 90 | .1779 | ·3062 | .3296 | .3477 | °3015 |
| 91 | 01427 | .2885 | .3319 | .3641 | • 3020 |
| 92 | 。5406 | o4613 | ·4298 | .4189 | .3946 |
| 93 | .1174 | .1954 | .2492 | °2787 | 。2482 |
| 94 | .1718 | °3854 | .3718 | .3665 | o3332 |
| 95 | .1636 | .3804 | .3679 | •3630 | ·3281 |
| 96 | .1321 | .2982 | .3185 | °3395 | .2769 |
| 97 | .1195 | 。3644 | °3555 | .3517 | ·2917 |
| 98 | .1306 | .3712 | • 3422 | • 3324 | • 2939 |
| 99 | .1142 | .1653 | •2425 | • 2793 | ° 2575 |
| 100 | .1661 | .2369 | •2980 | .3327 | · 3015 |
| 101 102 | •3288 | .3935 | •3598 | .3485 | • 3250 |
| 102 | 1209 1204 | • 1204 | •2137 | • 2341 | ° 2511 |
| 103 | . 7630 | ° 3029 • 6800 | • 3062 • 64 76 | 。3243 。6388 | 。2539 。5879 |
| 10 1 | 41030 | .0000 | 004 10 | 0000 | 0.0010 |

Appendix VI- Skewness values as estimated by different formulae

•

| | | ================= | | | |
|------------------|-----------------|-------------------|----------------|------------------|--|
| Sample Number | Skl | Sk2 | Sk3 | Sk | |
| | | | | | |
| 1 | 0000 | .8 531 | 1.2316 | .8458 | |
| 2 | .1882 | .4108 | 3837 | .1226 | |
| 3 | 0.0000 | 0.0000 | 1.9637 | .2713 | |
| 4 | 0.0000 | 0.000 | 1.8911 | .2666 | |
| 5 | 0.0000 | 。5064 | 1.0245 | .5314 | |
| 6 | 0.0000 | 0.0000 | 2.1256 | ·2811 | |
| 7 | 0.0000 | .1978 | 1.7607 | .3840 | |
| 8 | 0.0000 | 0.0000 | 1.7685 | °2583 | |
| 9 | 0000 | 0000 | 1.7181 | °2547 | |
| 10 | 0.0000 | 0.0000 | 2.0988 | .2796 | |
| 11 | 0.0000 | 0.0000 | 1.4178 | .2307 | |
| 12 | .2160 | • 5159 | 。5721 | •4663 | |
| 13 | 0.0000 | 0.0000 | •6565 | .0941 | |
| 14 | 0.0000 | 。4875 | 1.0462 | .5199 | |
| 15 | 0.0000 | .6174 | •7765 | •5842 | |
| 16 | 0.0000 | .6288 | .7983 | •5970 | |
| 17 | 0.0000 | 0.0000 | ° 2095 | .0562 | |
| 18 | 0.0000 | •6296 | •7661 | •5926 | |
| 19 | .0119 | .6230 | •7466 | • 5839 | |
| 20 | .0260 | .6112 | •7377 | • 5727 | |
| 21 | 0.0000 | .6048 | .7397 | .5678 | |
| 22 | • 2486 | • 5083 | 4734 | •1579 | |
| 23 24 | 4689 | 5240 | -2.1913 | 6754 | |
| | 0.0000 | • 5287 | 1.0900 | •5558 | |
| 25 26 | 。0071 。1980 | .6472 | ·8475 | .6196 | |
| 20 | | ·6109 | .7246 | • 5702 | |
| 28 | 0.0000 | • 5544 | .9647 | • 5606 | |
| 20 | | .6391 | .8082 | .6071 | |
| 30 | ∘2336 -∘1411 | •5976 -•3022 | • 7860 | • 5695 | |
| 31 | .0550 | 6800 | 2833 | 2583 .5260 | |
| 32 | 0.0000 | 0.0000 | | | |
| 33 | .2389 | .6789 | 0.0000 | 0.0000 | |
| 34 | .1460 | .6115 | 。8723 。8029 | 。6502 。5834 | |
| 35 | 0.0000 | .5669 | °8029 °7774 | ° 5834 ° 5437 | |
| ~ | 0.0000 | 0.0000 | 01114 | 07451 | |

- -

| Sample Number | Skl | Sk2 | Sk3 | Sk | |
|------------------|----------------|--------------|---------------|--------------------|--|
| =============== | ============== | ============ | ============= | ================== | |
| 36 | .1100 | .6221 | 。9004 | °6061 | |
| 37 | °2352 | .6215 | .7493 | •5831 | |
| 38 | °0803 | .6167 | .7719 | • 5828 | |
| 39 | ° 0 900 | •7297 | 1.2027 | •7098 | |
| 40 | 0.0000 | 。5440 | 1.0383 | .5616 | |
| 41 | °2471 | ₀6075 | o7190 | • 5665 | |
| 42 | °2581 | •6181 | •7255 | • 5 7 6 3 | |
| 43 | · 0526 | •6059 | •7771 | •5749 | |
| 44 | o1561 | 。6076 | •7611 | •5737 | |
| 45 | ·2264 | • 5663 | •6740 | • 5 2 5 4 | |
| 46 | °1027 | .6310 | •8506 | .6066 | |
| 47 | .2432 | •6356 | 。7596 | •5965 | |
| 48 | .2189 | 。6683 | .8311 | •6353 | |
| 49 | .1382 | 。4091 | • 5208 | .3977 | |
| 50 | 。2257 | .6395 | .7935 | .6052 | |
| 51 | ·1899 | .6342 | .8170 | .6043 | |
| 52 | .1927 | .6489 | .8363 | .6195 | |
| 53 | .1427 | .6295 | 。7835 | •5953 | |
| 54 | .0222 | .6392 | .9717 | .6293 | |
| 55 | •2636 | .6100 | 06437 | •5547 | |
| 56 | 。1009 | .6388 | 09487 | .6261 | |
| 57 | 02744 | 1.0000 | 1.3080 | 1.0000 | |
| 58 | ·2127 | .6750 | • 9566 | •6576 | |
| 59 | 0.0000 | • 3058 | 1.8905 | •4639 | |
| 60 | 0535 | .6618 | .9342 | 6436 | |
| 61 | -0.0150 | -0. 2627 | -2 . 2881 | - 0 .0186 | |
| 62 | 0.0000 | 0.0000 | 2.3544 | | |
| 63 | 0.0000 | 0.0000 | 2:0110 | · 2936 | |
| 64 | 0,0000 | 。4545 | -1.3864 | ·2743 | |
| 65 | 0.0000 | 0.0000 | 2.0421 | . 5045 | |
| 66 | 0.0000 | • 5723 | 1.1373 | °2762 °5944 | |
| 67 | 0.0000 | •4668 | 1.2827 | ° 5 2 9 7 | |
| 68 | 0, 0000 | · 260 0 | 08333 | | |
| 69 | 0.0000 | •6428 | 1.1072 | . 5417 | |
| 70 | 0.0000 | •4645 | 1.6947 | °6474 °5606 | |

| Sample Number | Skl | Sk2 | Sk3 | . Sk | |
|------------------|---------|--------|---------|---------|--|
| | | | | | |
| 71 | 0.0000 | 0.0000 | 3.0499 | •3241 | |
| 72 | 0.0000 | .6343 | 1.0162 | •6305 | |
| 73 | •2466 | •6723 | °8*88 | •6370 | |
| 74 | 。0250 | 。3750 | -2.1875 | 0398 | |
| 75 | 0.0000 | .2650 | 1.5998 | 04166 | |
| 76 | 0.0000 | .6104 | 1.1401 | .6246 | |
| 77 | ·0255 | .6111 | 1.9221 | .6632 | |
| 78 | 0037 | .6536 | •9908 | •6435 | |
| 79 | 0.0000 | .6044 | 。7886 | 。5755 | |
| 80 | o1746 | .6348 | •7506 | .5944 | |
| 81 | °0120 | .3103 | 2.0690 | 。4613 | |
| 82 | 0744 | .6766 | °9103 | 06532 | |
| 83 | 0.0000 | 04274 | 1.8751 | •5459 | |
| 84 | 0.0000 | 03429 | 1.7656 | •4809 | |
| 85. | 0.0000 | .5652 | 1.2195 | •5971 | |
| 86 | °2375 | •6808 | ₀8542 | 06494 | |
| 87 | 0.0000 | .6780 | 。8970 | 。6527 | |
| 88 | 0.0000 | 。4407 | 。9106 | 。4683 | |
| 89 | 0.0000 | 0.0000 | 2.5409 | 。3028 | |
| 90 | 0.0000 | °4214 | 。9455 | 04592 | |
| 91 | 0.0000 | ° 5075 | 1.3320 | •5640 | |
| 92 | 。2406 | .6027 | 。7673 | .5706 | |
| 93 | 0.0000 | o4014 | 1.5688 | •5072 | |
| 94 | •0302 | .6720 | 。9909 | .6591 | |
| 95 | .0267 | .6754 | 1.0045 | .6635 | |
| 96 | 0.0000 | 。5587 | 1.1449 | .5847 | |
| 97 | 0.0000 | .6735 | 1.0289 | .6646 | |
| 98 | 0.0000 | .6495 | .8124 | .6165 | |
| 99 | 0.0000 | •3120 | 2.0536 | 04777 | |
| 100 | 0.0000 | .3016 | 1.3462 | o4198 | |
| 101 | ·1300 | o6553 | .7972 | .6191 | |
| 102 | 0.0000 | 0.0000 | 2.5519 | .3033 | |
| 103 | 0.0000 | .6042 | 1.0311 | 。6079 | |
| 104 | °4 1 50 | .7794 | 1.1250 | . 76 66 | |

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Appendix VII- Kurtosis values as estimated by different formulae

| ======================================= | | | =========== | *************************************** |
|---|------------------|----------------|----------------|---|
| | Sample Number | Kul | Ku2 | Ku |
| ===================== | ======== | ============ | ============== | |
| | 1 | .0435 | | |
| | 2 | | . 508 5 | 5.9199 |
| | 2 | .1766 | 1.3186 | 1.2896 |
| | 2 4 | • 1506 | 2.0182 | 2.1872 |
| | 4 5 | • 2630 | 2.5456 | 2.1433 |
| | 6 | ° 1105 | °8411 | 2.2549 |
| | 7 | ∘1751 ∘1103 | 2.7801 | 2.2851 |
| | 8 | .1205 | 2.0879 | 2.3269 |
| | 9 | | 2.4230 | 2.0692 |
| | 10 | ∘1396 ∘1133 | 2.3725 | 2.0387 |
| | 11 | • 2630 | 2.7533 | 2.2688 |
| | 12 | | 2.0722 | 1.8571 |
| | 13 | • 3505 | .3729 | °6891 |
| | 14 | .1610 | 2.4860 | 2.1073 |
| | 15 | .1109 | .8940 | 2.2344 |
| | 16 | ·1098 | .4093 | 2.2272 |
| | 17 | .1064 | °4124 | 2.3004 |
| | 18 | • 2630 | .8640 | 1.1267 |
| | 19 | .1075 | .3788 | 2.2508 |
| | 20 | .1231 | .3702 | 1.9605 |
| | 21 | .1406 | .3807 | 1.7219 |
| | 22 | ·1141 | • 3934 | 2.1316 |
| | 23 | · 3254 | 1.4610 | 1.2938 |
| | 24 | • 3420 | 6.4878 | 3.5621 |
| | 25 | .1018 | .8697 | 2.3983 |
| | 26 | .1086 | .4312 | 2.2676 |
| | 27 | • 3242 | .3682 | .7436 |
| | 28 | • 1084 | .7019 | 2.3090 |
| | 29 | .2726 | 。4053 | . 8958 |
| | 30 | • 3241 | .4517 | .7650 |
| | 31 | 。3689 。1405 | ° 3205 | .6425 |
| | 32 | .2630 | .720 0 | 1.8230 |
| | 33 | · 3401 | •6544 | 1.0001 |
| | 34 | .2522 | °4035 | •7177 |
| | 35 | .1197 | 。4456 。4938 | °9814 |
| | | 01101 | 04730 | 2.0854 |

| ======================================= | | | and the second second | |
|---|------------------|---------------------------|---|---|
| | | | | ======================================= |
| Sample | Kul | Ku2 | 77 | |
| Number | TINT | ruz | Ku | |
| | | | | |
| ======================================= | ================ | ========================= | ======================================= | |
| 36 | 0010 | | | |
| 37 | ·2012 | •5256 | 1.2559 | |
| 38 | .3496 | .3754 | .6914 | |
| 39 | ·1941 | •4060 | 1.2585 | |
| 40 | •1485 | .7432 | 1.7623 | |
| 41 | • 1061 | .7926 | 2.3767 | |
| 42 | •3521 | • 3683 | ·6849 | |
| 43 | •3559 | •3573 | .6750 | |
| 44 | •1682 | °4290 | 1.4637 | |
| 45 | • 2766 | °4102 | 。8844 | |
| 46 | • 3442 | o3914 | •7063 | |
| 40 | • 2120 | °4610 | 1.1733 | |
| 48 | • 3541 | • 3624 | •6795 | |
| 49 | °3481 | .3798 | 。6955 | |
| 50 | · 3590 | •3483 | •6669 | |
| 51 | •3447 •3067 | • 3899 | •7049 | |
| 52 | • 3099 | 04221 | °8008 | |
| 53 | °2688 | •4172 | °7911 | |
| 54 | •1226 | .3964 | 。9058 | |
| 55 | ·3031 | • 5686 | 2.0508 | |
| 56 | •2067 | 02889 | •7274 | |
| 57 | •3734 | • 5463 | 1.2348 | |
| 58 | °3056 | • 3080 | .6318 | |
| 59 | 0969 | .4942 | •8226 | |
| 60 | °1542 | 2.0390 | 2.6464 | |
| 61 | 0327 | .4937 | 1.6289 | |
| 62 | .1895 | ° 0678 3°0089 | .3168 | |
| 63 | .2629 | 2.6655 | 2.4234 | |
| 64 | .1098 | 1.2955 | 2.2158 | |
| 65 | .1261 | | 2. 2996 | |
| 66 | .1007 | 2.6965 .8447 | 2.2345 | |
| 67 | .1020 | 00447 | 2.6079 | |
| 68 | 0921 | 3.0417 | 2.4546 | |
| 69 | .0892 | .6981 | 2 . 8395 | |
| 70 | 0931 | 1.5806 | 2.8744 | |
| | | 10000 | 2.9133 | |

| Sample Number | | Ku2 | Ku | |
|---|---|---------|---|---|
| | ======================================= | | ======================================= | |
| 71 | .0956 | 3.7044 | 2.8438 | |
| 72 | .0972 | .6212 | 2.6800 | |
| 73 | .3547 | .3608 | .6781 | |
| 74 | • 0584 | 3.8125 | 3.5064 | |
| 75 | .1070 | 1.8157 | | |
| 76 | .0938 | .7846 | 2.3159 | |
| 77 | 01330 | •5167 | 2.7692 | |
| 78 | .0976 | • 5638 | 1.2860 | |
| 79 | .1121 | • 4429 | 2.6265 | |
| 80 | .2949 | o 3546 | 2.2054 | |
| 81 | 0789 | 2.3793 | °8137 2°6776 | 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 |
| 82 | .1729 | • 4454 | | |
| 83 | .0898 | 1.8223 | 1.4309 2.9800 | |
| 84 | 0974 | 1.8528 | 2.6245 | |
| 85 | .0996 | .9388 | 2.6957 | |
| 86 | .3473 | .3823 | | |
| 87 | .0917 | · 4297 | .6977 | |
| 88 | 01248 | ° 4359 | 2.6842 | |
| 89 | .1134 | 3.1953 | 1.9844 2.5361 | |
| 90 | .1254 | .9026 | 1.9881 | |
| 91 | ° 1005 | 1.1467 | 2.6351 | |
| 92 | .3330 | .4245 | .7380 | |
| 93 | .0967 | 1.5590 | 2.5845 | |
| 94 | .1217 | .5334 | 2.0888 | |
| 95 | 01171 | 05414 | 2.1762 | |
| 96 | .0996 | .8749 | 2.5087 | |
| 97 | .0884 | .5690 | 2.9054 | |
| 98 | · 1012 | .3921 | 2.4016 | |
| 99 | 0928 | 2.1917 | 2.8047 | |
| 100 | .1176 | 1.5016 | 2.1654 | |
| 101 | ·2426 | .3674 | •9935 | |
| 102 | .1010 | 3.2064 | 2.5428 | |
| 103 | 0958 | 。6859 | 2.5749 | |
| 104 | .3140 | . 49 26 | .8077 | |
| | | | | |
| ======================================= | .====================================== | | ======================================= | ======================================= |
| | | | | |

Appendix VIII- Metric values of median (Md), standard deviation (QDa) and skewness (Ska) for use in diagrams of Buller and McManus (1972)

| Sample Number | Md (mm) | QDa(mm) | Ska |
|---|---------|---------|--------|
| ======================================= | | | |
| | | | |
| 1 2 | 0.375 | 0.079 | 0.057 |
| 2 | 0.139 | 0.035 | -0.012 |
| 3 | D.138 | 0.009 | |
| 4 | 0.142 | 0.009 | 0.000 |
| 5 6 | 0.136 | 0.009 | 0.002 |
| 6 | 0.139 | 0.009 | 0.000 |
| 7 | 0.138 | 0.010 | 0.001 |
| 8 | 0.140 | 0.010 | 0.001 |
| 9 | 0.139 | 0.009 | 0.000 |
| 10 | 0.137 | 0.009 | 0.001 |
| 11 | 0.143 | 0.009 | -0.001 |
| 12 | 0.131 | 0.029 | 0.003 |
| 13 | U.146 | 0.014 | -0.015 |
| 14 | 0.136 | 0.010 | 0.005 |
| 15 | 0.134 | | 0.005 |
| 16 | 0.134 | 0.010 | 0.001 |
| 17 | J. 142 | 0.009 | 0.000 |
| 18 | 0.137 | 0.008 | 0.001 |
| 19 | 0.134 | 0.010 | 0.001 |
| 20 | 0.134 | 0.010 | -0.001 |
| 21 | 0.136 | 0.012 | -0.002 |
| 22 | 0.134 | 0.010 | 0.000 |
| 23 | 0.177 | 0.035 | -0.016 |
| 24 | 0.134 | 0.134 | 0.102 |
| 25 | 0.133 | 0.008 | 0.001 |
| 26 | 0.131 | 0.009 | -0.001 |
| 27 | 0.136 | 0.025 | -0.015 |
| 28 | 0.131 | 0.009 | -0.000 |
| 29 | 0.131 | 0.046 | 0.014 |
| 30 | 0.094 | 0.028 | -0.016 |
| 31 | | 0.028 | 0.014 |
| 32 | 0.132 | 0.012 | -0.004 |
| 33 | 0.198 | 0.007 | 0.000 |
| 34 | 0.128 | 0.025 | -0.017 |
| | 0.133 | 0.021 | -0.017 |

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Appendix VIII- continued

| Sample Number | Md (mm) | QDa(mm) | Ska |
|---|---------|---------|--------|
| ======================================= | | | |
| 35 | 0.137 | 0.012 | |
| 36 | 0.134 | 0.012 | 0.001 |
| 37 | 0.130 | 0.020 | -0.008 |
| 38 | 0.133 | 0.027 | -0.016 |
| 39 | 0.130 | 0.017 | -0.006 |
| 40 | 0.136 | 0.026 | -0.017 |
| 41 | 0.128 | 0.010 | 0.001 |
| 42 | 0.125 | 0.028 | -0.017 |
| 43 | 0.135 | 0.028 | -0.017 |
| 44 | 0.131 | 0.015 | -0.005 |
| 45 | | 0.022 | -0.012 |
| 46 | 0.129 | 0.028 | -0.015 |
| 47 | 0.132 | 0.018 | -0.007 |
| 48 | 0.127 | 0.026 | -0.017 |
| 49 | 0.127 | 0.023 | -0.016 |
| 50 | 0.166 | 0.024 | -0.008 |
| 51 | 0.128 | 0.025 | -0.016 |
| 52 | 0.129 | 0.023 | -0.013 |
| 53 | 0.129 | 0.022 | -0.014 |
| | 0.130 | 0.020 | -0.011 |
| 54 | 0.132 | 0.009 | -0.002 |
| 55 | 0.132 | 0.032 | -0.018 |
| 56 | 0.131 | 0.017 | -0.008 |
| 57 | 0.125 | 0.020 | -0.020 |
| 58 | J.127 | 0.021 | -0.018 |
| 59 | 0.134 | 0.007 | -0.000 |
| 50 | 0.132 | 0.013 | -0.005 |
| 51 | 0.144 | 0.018 | 0.002 |
| 52 | 0.138 | 0.009 | |
| 53 | 0.138 | 0.007 | 0.001 |
| 54 | 0.136 | 0.008 | 0.000 |
| 55 | 0.139 | 0.010 | 0.000 |
| 56 | 0.133 | 0.009 | -0.001 |
| 57 | 0.136 | 0.009 | 0.001 |
| 58 | 0.135 | 0.007 | 0.000 |
| 9 | 0.134 | 0.007 | 0.000 |
| 0 | 0.135 | 0.008 | 0.000 |
| | | 0.000 | 0.001 |

Appendix VIII- continued

| Sample Number | Md (rım) | QDa(mm) | Ska |
|------------------|---|---------|--------|
| ============= | ======================================= | | |
| 71 | J.135 | 0.007 | 0.001 |
| 72 | 0.135 | 0.009 | 0.001 |
| 73 | 0.128 | 0.026 | -0.018 |
| 74 | 0.141 | 0.011 | -0.001 |
| 75 | 0.136 | 0.009 | 0.001 |
| 76 | 0.133 | 0.008 | 0.001 |
| 77 | 0.132 | 0.018 | -0.008 |
| 78 | 0.134 | 0.010 | -0.001 |
| 79 | 0.136 | 0.010 | |
| 80 | 0.132 | 0.022 | 0.000 |
| 81 | 0.133 | 0.018 | -0.013 |
| 82 | 0.132 | 0.014 | -0.008 |
| 83 | 0.135 | 0.007 | -0.005 |
| 84 | 0.135 | 0.052 | 0.001 |
| 85 | 0.135 | 0.009 | -0.045 |
| 86 | 0.130 | 0.025 | -0.001 |
| 87 | 0.133 | 0.007 | -0.017 |
| 88 | 0.140 | 0.012 | 0.000 |
| 89 | 0.139 | 0.009 | 0.000 |
| 90 | 0.139 | 0.009 | -0.001 |
| 91 . | 0.137 | 0.012 | 0.001 |
| 92 | 0.134 | | 0.000 |
| 93 | 0.134 | 0.029 | -0.017 |
| 94 | 0.132 | 0.007 | 0.001 |
| 95 | J. 132 | 0.010 | -0.002 |
| 96 | 0.135 | 0.010 | -0.002 |
| 97 | 0.134 | 0.008 | 0.000 |
| 98 | 0.133 | 0.008 | -0.001 |
| 99 | 0.134 | 0.009 | 0.001 |
| 100 | | 0.007 | 0.001 |
| 101 | 0.139 | 0.011 | 0.001 |
| 102 | 0.132 | 0.019 | -0.010 |
| 103 | 0.137 | 0.008 | 0.001 |
| 104 | 0.134 | 0.008 | 0.001 |
| | 0.385 | 0.088 | -0.053 |

B.